## SUPPORTING INFORMATION

A Classic, Azo-Dye Agglomeration System: Evidence for Slow, Continuous Nucleation, Autocatalytic Agglomerative Growth, Plus the Effects of Dust-Removal by Microfiltration on the Kinetics

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## S1 Derivation of the Kinetic Equations Employed in the Main Text

The kinetics derivation which follows refers back to Scheme 3 of the main text. The relevant kinetic equations, derived based on the mechanism provided in Scheme 3, are the following:

$$
\begin{equation*}
-\frac{d[\mathrm{~A}]}{d t}=\frac{d[\mathrm{~B}]}{d t}=\frac{1}{1 / n} \frac{d\left[\mathrm{~B}_{n}\right]}{d t}=k_{1}[\mathrm{~A}]+k_{2}[\mathrm{~A}][\mathrm{B}] \tag{S1}
\end{equation*}
$$

Since the concentration of water does practically not change during the reaction the constant [ $\mathrm{H}_{2} \mathrm{O}$ ] is absorbed into the apparent rate constants $k_{1}$ and $k_{2}$.
What is actually monitored is the absorbance at $475 \mathrm{~nm}, \mathrm{~A}_{475}$, assigned in the original 1978 publication ${ }^{1}$ to the agglomerated dye, $B_{n}$. By Beer's law we can write the following equations: What we need are expressions for $[\mathrm{A}]_{t},[\mathrm{~B}]_{t}$, and $[\mathrm{B}]_{\infty}$ in terms of $\mathrm{A}_{475}$ measurable.

$$
\begin{equation*}
\mathrm{A}_{475}=\varepsilon_{475} \mathrm{~b}\left[\mathrm{~B}_{\mathrm{n}}\right] \text {, but since }[\mathrm{B}]=1 /{ }_{\mathrm{n}}\left[\mathrm{~B}_{\mathrm{n}}\right] \text {, that is, }\left[\mathrm{B}_{\mathrm{n}}\right]=\mathrm{n}[\mathrm{~B}] \tag{S2a}
\end{equation*}
$$

$$
\begin{equation*}
\mathrm{A}_{475}=\varepsilon_{475} \mathrm{bn}[\mathrm{~B}], \text { or } \tag{S2b}
\end{equation*}
$$

$$
\begin{equation*}
[\mathrm{B}]_{t}=\frac{1}{n b \varepsilon_{475}}\left(\mathrm{~A}_{475}\right)_{t} \tag{S2c}
\end{equation*}
$$

and since $n[B]_{\infty}=\left[B_{n}\right]_{\infty}$ and for a reaction with single product by mass balance in eq 5 of Scheme 3 in the main text, $[B]_{\infty}=[A]_{0}$

$$
\begin{equation*}
[\mathrm{A}]_{o}=[\mathrm{B}]_{\infty}=\frac{1}{n b \varepsilon_{475}}\left(\mathrm{~A}_{475}\right)_{\infty} \tag{S2d}
\end{equation*}
$$

Next we need expressions for $[\mathrm{A}]_{0}$ and $[\mathrm{A}]_{t}$ in terms of $\mathrm{A}_{475}$ measurable. Our mass balance and initial reactant, $[\mathrm{A}]_{0}$, vs final product, $[\mathrm{B}]_{\infty}$, equations give us the needed results:

$$
\begin{align*}
& {[\mathrm{A}]_{\mathrm{o}}=[\mathrm{A}]_{t}+[\mathrm{B}]_{t}}  \tag{S3a}\\
& {[\mathrm{~A}]_{\mathrm{o}}=[\mathrm{B}]_{\infty} \text { so }} \tag{S3b}
\end{align*}
$$

$$
\begin{equation*}
[\mathrm{A}]_{t}=[\mathrm{B}]_{\infty}-[\mathrm{B}]_{t} \tag{S3c}
\end{equation*}
$$

Now combining eqs (S8c), (S7c) and (S7d) yields eq (S4):

$$
\begin{equation*}
[\mathrm{A}]_{t}=\frac{1}{n b \varepsilon_{475}}\left(\left(\mathrm{~A}_{475}\right)_{\infty}-\left(\mathrm{A}_{475}\right)_{t}\right) \tag{S4}
\end{equation*}
$$

We can now combine eq (S4) with eq (S1) to yield eqs (S5)

$$
\begin{equation*}
\frac{d[B]}{d t}=\frac{1}{n b \varepsilon_{475}} \frac{d\left(\mathrm{~A}_{475}\right)}{d t}=\frac{1}{n b \varepsilon_{475}} k_{1}\left[\left(\mathrm{~A}_{475}\right)_{\infty}-\left(\mathrm{A}_{475}\right)_{t}\right]+\left(\frac{1}{n b \varepsilon_{475}}\right)^{2} k_{2}\left(\mathrm{~A}_{475}\right)_{t}\left[\left(\mathrm{~A}_{475}\right)_{\infty}-\left(\mathrm{A}_{475}\right)_{t}\right] \tag{S5a}
\end{equation*}
$$

Eq (S5a) simplifies to eq (S5b) by substituting $\left(\mathrm{A}_{475}\right)$ for $\left(\mathrm{A}_{475}\right)_{t}$
$\frac{d\left(\mathrm{~A}_{475}\right)}{d t}=k_{1}\left[\left(\mathrm{~A}_{475}\right)_{\infty}-\left(\mathrm{A}_{475}\right)\right]+\frac{1}{n b \varepsilon_{475}} k_{2}\left(\mathrm{~A}_{475}\right)_{t}\left[\left(\mathrm{~A}_{475}\right)_{\infty}-\left(\mathrm{A}_{475}\right)\right]$
or to eq (S5c) by substituting $k_{2}^{\prime}=k_{2} / n b \varepsilon_{475}$

$$
\begin{align*}
\frac{d\left(\mathrm{~A}_{475}\right)}{d t} & =k_{1}\left[\left(\mathrm{~A}_{475}\right)_{\infty}-\left(\mathrm{A}_{475}\right)\right]+k_{2}^{\prime}\left(\mathrm{A}_{475}\right)_{t}\left[\left(\mathrm{~A}_{475}\right)_{\infty}-\left(\mathrm{A}_{475}\right)\right]  \tag{S5c}\\
& \text { where } k_{2}^{\prime}=k_{2}\left(\frac{1}{n b \varepsilon_{475}}\right)=k_{2} \frac{1}{\mathrm{C}_{1}} \\
& \mathrm{C}_{1}=\text { constant }=n b \varepsilon_{475} \text { or } k_{2}=\left(n b \varepsilon_{475}\right) k_{2}^{\prime}=\mathrm{C}_{1} k_{2}^{\prime}
\end{align*}
$$

Eq (S5c) looks exactly like the $\frac{d[B]}{d t}$ form of eq (S1), repeated below, for which the integrated rate equation is eq (S6)

$$
\begin{align*}
& \frac{d[\mathrm{~B}]}{d t}=k_{1}[\mathrm{~A}]+k_{2}[\mathrm{~A}][\mathrm{B}]  \tag{S1}\\
& {[\mathrm{B}]_{t}=[\mathrm{A}]_{\mathrm{o}}\left(1-\frac{k_{1}+k_{2}[\mathrm{~A}]_{\mathrm{o}}}{k_{2}[\mathrm{~A}]_{\mathrm{o}}+k_{1} e^{\left(k_{1}+k_{2}[\mathrm{~A}]_{\mathrm{o}}\right) t}}\right)} \tag{S6}
\end{align*}
$$

By analogy, the integrated rate equation for eq (S5b) is given eqs (S7a), (S7b), (S7c), and (S8):
$[\mathrm{B}]_{t}=\left(\frac{1}{n b \varepsilon_{475}}\right)\left(\mathrm{A}_{475}\right)_{t}=\frac{1}{\mathrm{C}_{1}}\left(\mathrm{~A}_{475}\right)_{t}$
$[\mathrm{A}]_{t}=\frac{1}{n b \varepsilon_{475}}\left(\left(\mathrm{~A}_{475}\right)_{\infty}-\left(\mathrm{A}_{475}\right)_{t}\right)=\frac{1}{\mathrm{C}_{1}}\left(\left(\mathrm{~A}_{475}\right)_{\infty}-\left(\mathrm{A}_{475}\right)_{t}\right)$
$[\mathrm{A}]_{\mathrm{o}}=[\mathrm{B}]_{\infty}=\frac{1}{n b \varepsilon_{475}}\left(\mathrm{~A}_{475}\right)_{\infty}=\frac{1}{\mathrm{C}_{1}}\left(\mathrm{~A}_{475}\right)_{\infty}$

The integration of eq (S5c) yields eq (S8):
$\left(\mathrm{A}_{475}\right)_{t}=\left(\mathrm{A}_{475}\right)_{\infty}\left(1-\frac{k_{1}+k_{2}^{\prime}\left(\mathrm{A}_{475}\right)_{\infty}}{k_{2}^{\prime}\left(\mathrm{A}_{475}\right)_{\infty}+k_{1} e^{\left(k_{1}+k_{2}^{\prime}\left(\mathrm{A}_{475}\right) \infty\right) t}}\right)$

Comparing of eq (S8) to eq (S6) reveals that using the integrated rate equation (S8) for the product formation in terms of absorbance yields $k_{2}^{\prime}$ instead of $k_{2}$ in the normal integrated rate equation (S6).

## References:

[^0]
[^0]:    ${ }^{1}$ Reeves, R. L.; Harkaway, S. A.; Klingbiel, R. T. Phase transition autocatalysis of the hydrolysis of some esters of azo dyes, J. Am. Chem. Soc. 1978, 100, 3879-3881.

