## Supporting Information

## New 4V-class and zero-strain cathode material for Na ion batteries

Jongsoon Kim ${ }^{1, \dagger}$, Gabin Yoon ${ }^{2,3,4 \dagger}$, Myeong Hwan Lee ${ }^{2,3}$, Hyungsub Kim ${ }^{5}$, Seongsu Lee ${ }^{5}$, and Kisuk Kang **2,3,4<br>${ }^{l}$ Department of Nanotechnology and Advanced Materials Engineering, Sejong University, 209 Neungdong-ro, Gwangjin-gu, Seoul, Republic of Korea<br>${ }^{2}$ Department of Materials Science and Engineering and ${ }^{3}$ Research Institute of Advanced Materials (RIAM), Seoul National University, 1 Gwanak-ro, Gwanak-gu, Seoul 151-742, Korea<br>${ }^{4}$ Center for Nanoparticle Research at Institute for Basic Science (IBS), Seoul National University, 1 Gwanak-ro, Gwanak-gu, Seoul 151-742, Korea<br>${ }^{5}$ Korea Atomic Energy Research Institute (KAERI), Daedeok-daero 989 Beon-Gil, Yuseonggu, Daejeon, Korea<br>${ }^{\dagger}$ These authors contributed equally to this paper.

Corresponding Author: Prof. Kisuk Kang

E-mail: matlgen1@snu.ac.kr

TEL: +82-2-880-7088


Supporting Figure S1 SEM image of $\mathrm{Na}_{3} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$.


Supporting Figure S2 Refined XRD pattern of $\mathrm{Na}_{3} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}\left(\mathrm{R}_{\mathrm{p}}=7.52 \%, \mathrm{R}_{\mathrm{I}}=8.53 \%, \mathrm{R}_{\mathrm{F}}=\right.$ $\left.7.39 \%, \chi^{2}=8.78 \%\right)$.


Supporting Figure S3 Charge/discharge curve of $\mathrm{Na}_{3} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$ from $2.0-4.5 \mathrm{~V}$ at $\mathrm{C} / 10$

 amounts in the structure

(b)

Supporting Figure S5 (a) Site energy of a single Na vacancy from $\mathrm{Na}_{3} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$ plotted as a type of Na site. (b) Volume change of the $\mathrm{Na}_{3} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$ structure upon the removal of all Na ions in each Na site.

| Atom | Multiplicity | x | y | z | $\mathrm{B}_{\text {iso }}$ | Occupancy |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P 1 | 12 | $0.3327(5)$ | $0.0826(4)$ | $0.2444(5)$ | $0.95(6)$ | 1 |
| V 1 | 4 | $0.0798(3)$ | $-0.0798(3)$ | $0.4202(3)$ | $0.2(13)$ | 1 |
| Na 1 | 4 | $0.0094(6)$ | $0.0094(6)$ | $0.0094(6)$ | $1.56(10)$ | $0.989(7)$ |
| Na 2 | 4 | $0.3901(8)$ | $0.3901(8)$ | $0.3901(8)$ | $1.56(10)$ | $0.997(3)$ |
| Na 3 | 4 | $0.7022(7)$ | $0.2022(7)$ | $0.2978(7)$ | $1.56(10)$ | $0.998(2)$ |
| O 1 | 12 | $0.2693(4)$ | $-0.0261(4)$ | $0.3488(4)$ | $1.03(5)$ | 1 |
| O 2 | 12 | $0.3711(4)$ | $0.0009(4)$ | $0.1112(4)$ | $0.92(4)$ | 1 |
| O 3 | 12 | $0.4506(3)$ | $0.1671(4)$ | $0.3065(4)$ | $1.19(5)$ | 1 |
| N 1 | 4 | $0.1956(3)$ | $0.1956(3)$ | $0.1956(3)$ | $0.88(5)$ | 1 |

Supporting Table T1 Atomic information of $\mathrm{Na}_{3} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$.

|  | $\mathrm{Na}_{3} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$ | $\mathrm{Na}_{2} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$ |
| :---: | :---: | :---: |
| $\mathrm{Na} 1-\mathrm{O}_{6}(\AA)$ | $2.60(3), 2.52(3)$ | $2.80(3), 2.58(3)$ |
| $\mathrm{V}-\mathrm{O}_{6}(\mathrm{~A})$ | $2.04(6)$ | $1.96(6)$ |

Supporting Table T2 Na1-O and V-O Bond lengths of $\mathrm{Na}_{3} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$ and $\mathrm{Na}_{2} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$.

|  | $\mathrm{Na}_{3} \mathbf{V}\left(\mathrm{PO}_{3}\right)_{3} \mathbf{N}$ <br> $(x, y, z)(\AA)$ | $\mathrm{Na}_{2} \mathbf{V}\left(\mathrm{PO}_{3}\right)_{3} \mathbf{N}$ <br> $(x, y, z)(\AA)$ | Displacement <br> $(x, y, z)(\AA)$ |
| :---: | :---: | :---: | :---: |
| V1 | $(0.761,8.832,4.035)$ | $(0.796,8.802,4.003)$ | $(0.035,-0.030,-0.032)$ |
| V2 | $(4.035,0.761,8.832)$ | $(4.003,0.796,8.802)$ | $(-0.032,0.035,-0.030)$ |
| V3 | $(8.832,4.035,0.761)$ | $(8.802,4.003,0.796)$ | $(-0.030,-0.032,0.035)$ |
| V4 | $(5.557,5.557,5.557)$ | $(5.594,5.594,5.594)$ | $(0.038,0.038,0.038)$ |

Supporting Table T3 Cartesian coordinates of four V ions in the unit cell of $\mathrm{Na}_{3} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$ and $\mathrm{Na}_{2} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$. The displacements vectors of V ions upon desodiation is also tabulated. Due to the symmetry of $\mathrm{Na}_{3} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$ and desodiated $\mathrm{Na}_{2} \mathrm{~V}\left(\mathrm{PO}_{3}\right)_{3} \mathrm{~N}$, the direction of V ion movement cancels out each other, resulting in the negligible vector sum of net V ion displacements.

