Supporting Information

Mechanistic Insights into Surface Chemical Interactions between Lithium Polysulfides

and Transition Metal Oxides

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Synthesis of metal oxides:

The metal oxides of Mn, Fe, Co and Ni were synthesized with a general solvothermal method. Typically, 0.7 mmol of the corresponding metal acetate was dissolved in 35 mL of ethanol-water (10:1 v/v) mixed solution with continuous stirring for 10 min. The solution was then transferred to a 50 mL Teflon-lined stainless steel autoclave and heated at 160 $^{\circ}$ C for 12 h. After cooling to room temperature, the precipitate was collected by centrifuging and washing with water for three times. The final product was dried at 60 $^{\circ}$ C and ground for future use.

XPS study of interactions between LPS and oxides:

Metal oxide powder was uniformly dispersed in ethanol by sonication. The mixture was then drop-casted onto Al foil to form a film. The film was cut into a suitable size and immersed in a 0.01 M Li_2S_6 solution for 24 h to allow sufficient interaction with LPS. The Li_2S_6 solution was prepared by dissolving stoichiometric amounts of sulfur and lithium sulfide in a 1,3-dioxolane/dimethoxyethane (DOL/DME, 1:1 v/v) mixed solvent. After interaction, the metal oxide film was retrieved and transferred to the XPS chamber using a vacuum transfer vessel.

Material characterizations:

XRD was performed with a Rigaku SmartLab X-ray diffractometer with Cu K α radiation (λ =1.5418 Å). SEM images were taken on a Hitachi SU8230 SEM microscope. XPS was performed on a PHI VersaProbe II Scanning XPS Microprobe with Al K α monochromatic X-ray source.

Computational details:

We used the Vienna ab initio simulation package $(VASP)^{1-4}$ for all periodic boundary calculations. Projector augmented plane wave (PAW) method⁵⁻⁶ together with the PBE exchange-correlation functional⁷ were employed to describe the electron-ion interactions. We used the PBE + *U* method following Dudarev's approach⁸ to add on-site potentials to the *d* electrons of transition metals to describe the electronic states of transition metal oxides properly. $U_{eff} = U - J$ parameters of 2 and 3 eV were used for Mn₃O₄ and Co₃O₄ to reproduce the experimental band gaps of bulk metal oxides. A cutoff of 450 eV was chosen for the plane wave basis set in all calculations. A 3 × 3 × 3 Monckhorst-Pack type k-point grid was chosen

for the optimization of bulk Mn_3O_4 and Co_3O_4 . A Gaussian smear was used and the σ value was chosen to be 0.1 eV. The energy convergence criterion was set to be 10^{-4} eV per unit cell and the force convergence criterion of 0.01 eV Å⁻¹ was used for all structure optimization. As shown in Table S2 and S3, the calculated bulk properties of transition metal oxides agree well with experimental results.

Previous study⁹ has shown that the (100) surface is the most stable surface of Co₃O₄ in terms of surface energy. More specifically, the (100) surface consisting of 4 five-coordinate Co(III) centers and 2 two-coordinate Co(II) centers is the most stable surface. For Mn₃O₄, previous computational study suggests that the (001) surface is the most stable surface.¹⁰ Thus, we studied the absorption of Li₂S_x (x = 2-6) on Co₃O₄(100) and Mn₃O₄(001) surfaces. A vacuum slab of about 15 Å was inserted between the surface slab. The cell parameter is 23.12 Å × 8.12 Å for Co₃O₄(100) and 8.25 Å × 8.18 Å × 24.51 Å for Mn₃O₄(001). Standard Monkhorst-Pack k-point meshes of 1 × 3 × 3 and 3 × 3 × 1 were used for Co₃O₄(100) and Mn₃O₄(001), respectively. The bottom two metal-oxide layers of Co₃O₄ and Mn₃O₄ were fixed at the bulk position during geometry optimization. For the calculation of Li₂S_x, a supercell of 15 Å × 15 Å × 15 Å and a 1 × 1 × 1 Monkhorst-Pack k-point mesh were used. The binding energy (BE) was calculated as BE = E_{total} – E_{ads} – E_{surf}, where E_{total} is the total energy of the absorbed system, E_{ads} is the energy of the adsorbate (Li₂S_x) in vaccum and E_{surf} is the energy of the optimized bare surface.

We used Gaussian 09 software package¹¹ to calculate the change of the free energy of the two reactions shown in Figure S5 and S6. A pruned grid having 99 radial shells and 590 angular points per shell, called "ultrafine" grid in Gaussian 09, was used for the non-analytic integral evaluations. We used the PBE functional along with the Lanl2DZ pseudopotential and basis set¹² for Cu and 6-31G(d)¹³⁻¹⁴ for other atoms in the geometry optimization and frequency analysis. The calculated vibrational frequencies were used for the computation of molecular partition functions to evaluate thermal contributions to the free energy at 298.15 K by employing the ideal gas, rigid rotator, harmonic oscillator approximation.¹⁵ Single point calculations were performed at the optimized structures with the Lanl2DZ pseudopotential and basis set for Cu and the 6-311+G(2df,p) basis set¹⁴ for other atoms for more reliable energetics. Since the direct calculation of the free energy of solids is not that straight forward, experimental formation free energies (Table S4) of CuO(s), Cu₂O(s), Li₂O(s), and Cu(g), and Li(g) were used to calculate the free energy changes of proposed reactions 1 and 2 according to the thermodynamic cycles in Figure S5 and S6. The structures of Li₂S₆, Li₂S₈, Li₂S₂O₃, and $Li_3[Cu(S_2O_3)_2]$ are shown in Figure S7 and their calculated solvation free energies are shown in Table S5. The solvation free energies were estimated with SMD solvation $model^{16}$ with diethyl ether as the solvent, since the parameters of DME and DOL are not implemented in Gaussian.

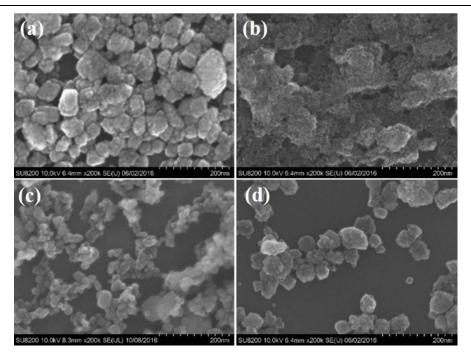


Figure S1. SEM images of (a) Co_3O_4 , (b) Fe_2O_3 , (c) Mn_3O_4 and (d) CuO.

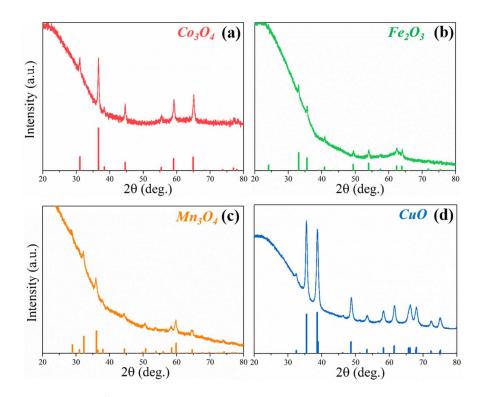


Figure S2. XRD of (a) Co_3O_4 , (b) Fe_2O_3 , (c) Mn_3O_4 and (d) CuO.



Figure S3. Picture of the vacuum vessel for XPS sample transfer.

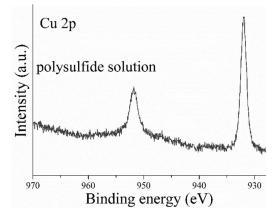


Figure S4. Cu 2p XPS spectra of the dried LPS solution after interacting with CuO.

$$6\operatorname{CuO}(s) + 3\operatorname{Li}_2S_6(\operatorname{sol}) \xrightarrow{\Delta G_1} 3\operatorname{Cu}_2O(s) + \operatorname{Li}_2S_2O_3(\operatorname{sol}) + 2\operatorname{Li}_2S_8(\operatorname{sol}) \xrightarrow{} -6\Delta_jG(\operatorname{CuO}) \xrightarrow{} -3\Delta_sG(\operatorname{Li}_2S_6) \xrightarrow{} 3\Delta_jG(\operatorname{Cu}_2O) \xrightarrow{} \Delta_sG(\operatorname{Li}_2S_2O_3) \xrightarrow{} \Delta_sG(\operatorname{Li}_2S_8) \xrightarrow{} 6\operatorname{Cu}(s) + 3O_2(g) + 3\operatorname{Li}_2S_6(g) \xrightarrow{} \Delta G_1^{\operatorname{gas}} 6\operatorname{Cu}(s) + 3/2O_2(g) + \operatorname{Li}_2S_2O_3(g) + 2\operatorname{Li}_2S_8(g)$$

Figure S5. The thermodynamic cycle used to calculate the change of free energy for reaction 1.

$$Cu_{2}O(s) + 4Li_{2}S_{2}O_{3}(sol) \xrightarrow{\Delta G_{2}} 2Li_{3}[Cu(S_{2}O_{3})_{2}](sol) + Li_{2}O(s)$$

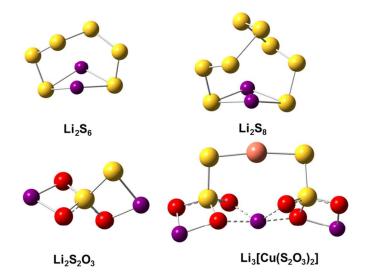
$$\downarrow -\Delta_{f}G(Cu_{2}O) \downarrow -4\Delta_{s}G(Li_{2}S_{2}O_{3}) \qquad \uparrow 2\Delta_{s}G(Li_{3}[Cu(S_{2}O_{3})_{2}]) \qquad \uparrow \Delta_{f}G(Li_{2}O)$$

$$2Cu(s) + 1/2O_{2}(g) + 4Li_{2}S_{2}O_{3}(g) \qquad 2Li_{3}[Cu(S_{2}O_{3})_{2}](g) + 2Li(s) + 1/2O_{2}(g)$$

$$\downarrow 2\Delta_{f}G(Cu(g)) \qquad \uparrow -2\Delta_{f}G(Li(g))$$

$$2Cu(g) + 1/2O_{2}(g) + 4Li_{2}S_{2}O_{3}(g) \xrightarrow{\Delta G_{2}^{gas}} 2Li_{3}[Cu(S_{2}O_{3})_{2}](g) + 2Li(g) + 1/2O_{2}(g)$$
Figure S6. The thermodynamic cycle used to calculate the change of free energy for reaction

Figure S6. The thermodynamic cycle used to calculate the change of free energy for reaction 2.



 $\label{eq:Figure S7.} \ \text{Figure S7.} \ \text{DFT} \ \text{optimized structures of } Li_2S_6, \ Li_2S_8, \ Li_2S_2O_3, \ \text{and} \ Li_3[Cu(S_2O_3)_2].$

Solubility Product Constant (K _{sp} , 25 °C)			
MnS	FeS	CoS	CuS
3×10 ⁻¹¹	8×10 ⁻¹⁹	3×10 ⁻²⁶	8×10 ⁻³⁷

Table S1. Solubility product constants of sulfides of Mn, Fe, Co and Cu.

Table S2. Calculated and experimental properties of bulk Mn₃O₄

Properties	PBE	$PBE + U^a$	Expt.
a /Å	5.75	5.80	5.76^{b}
b /Å	5.76	5.80	5.76^{b}
c /Å	9.49	9.52	9.46 ^b
dMn ^{II} –O (Å)	2.00	2.03	2.07^{b}
dMn ^{III} –Oaxial (Å)	2.33	2.32	2.29^{b}
dMn ^{III} –Oequatorial (Å)	1.93	1.95	1.91 ^b
Mn^{II} magnetic moment (μB)	4.18	4.42	4.34 ^c
Mn ^{III} magnetic moment (µB)	3.51	3.73	3.45 ^c
Eg (eV)	0.96	1.30	1.91 ^{<i>d</i>}

^{*a*} A U – J value of 2.0 eV was used in the calculation.

 b Ref. ¹⁷.

^d Ref. ¹⁹.

Table S3. Calculated	and experimental	properties of bulk Co ₃ O ₄
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Properties	PBE	$PBE + U^a$	Expt.
unit cell parameter/Å	8.09	8.12	8.082^{b}
dCo ^{II} –O (Å)	1.92	1.95	1.928^{b}
dCo ^{III} –O (Å)	1.93	1.92	1.923^{b}
Atomic magnetic moment (µB)	2.25	2.61	3.26 ^c
E _g (eV)	0.18	1.48	1.60^{d}

^{*a*} A U - J value of 3.0 eV was used in the calculation. ^{*b*} Ref.²⁰.

^c Ref. ²¹. ^d Ref. ²².

^c Ref. ¹⁸.

	kJ mol ⁻¹	kcal mol ⁻¹
CuO(s)	-129.7	-31.0
Cu ₂ O(s)	-146.0	-34.9
Li ₂ O(s)	-561.2	-134.1
Li(g)	126.6	30.3
Cu(g)	297.7	71.2
^{<i>a</i>} Experimental data taken from ²³ .		

Table S4. Experimental standard molar Gibbs energies of formation for metal oxides and metal atoms at 298.15 K^a

Table S5. Calculated Gibbs free energies of solvation

	kcal mol ⁻¹
Li_2S_6	-12.7
Li_2S_8	-12.5
$Li_2S_2O_3$	-18.9
$Li_3[Cu(S_2O_3)_2]$	-28.7

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