

--- Supporting Information for ---

^{17}O NMR Investigation of Water Structure and Dynamics

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Terminology and Definitions

NMR spectra of half-integer nuclear spin quadrupolar nuclei can be used to determine the local structure around the quadrupolar nucleus of interest via chemical shift and quadrupolar information. ^{17}O MAS NMR spectra typically show a central transition ($1/2 \leftrightarrow -1/2$) peak subject to the second-order quadrupolar interaction that can be described by the quadrupolar coupling constant, C_Q , and the asymmetry parameter, η_Q .

$$C_Q = \frac{eV_{zz}Q}{h} \quad (1)$$

$$\eta_Q = \frac{(V_{xx} - V_{yy})}{V_{zz}} \quad (2)$$

Here e is the charge of an electron, Q is the quadrupolar moment intrinsic to the nucleus of interest, h is the Planck constant, and V_{mn} are eigenvalues of the electric field gradient (EFG) tensor, with V_{zz} being the largest component ($|V_{zz}| \geq |V_{yy}| \geq |V_{xx}|$).¹⁻⁴

Chemical shift anisotropy (CSA) can influence the NMR spectra of quadrupolar nuclei, such as ^{17}O . To assist in isolating the effects of the chemical shift tensor on the spectra experiments are performed at multiple magnetic fields. The increase in contribution due to CSA combined with the subsequent decrease in the effect of the quadrupolar interaction allows for less ambiguous determinations of the interaction tensors as the external magnetic field is increased. The discussion that follows will employ the IUPAC definitions for chemical shift interactions.⁵ The isotropic chemical shift is defined as the trace of the chemical shift tensor,

$$\delta_{iso} = \frac{1}{3}(\delta_{zz} + \delta_{yy} + \delta_{xx}) \quad (3)$$

where, δ_{zz} , δ_{yy} and δ_{xx} are the principal components of the second rank chemical shift tensor. The chemical shift tensor can be further described by the chemical shift anisotropy, ζ_δ and asymmetry parameter, η_δ ,

$$\zeta_\delta = \delta_{zz} - \delta_{iso} \quad (4)$$

$$\eta_\delta = \frac{\delta_{yy} - \delta_{xx}}{\zeta_\delta} \quad (5)$$

when adopting the Haeberlen convention⁵⁻⁷, where

$$|\delta_{zz}| \geq |\delta_{yy}| \geq |\delta_{xx}| \quad (6)$$

Quantum chemical calculations determine the nuclear shielding tensor rather than the chemical shift tensor,

$$\delta_{nn} = \sigma_{nn} - \sigma_{ref} \quad (7)$$

The dipolar coupling tensor will be describe herein using the dipolar coupling constant, D.

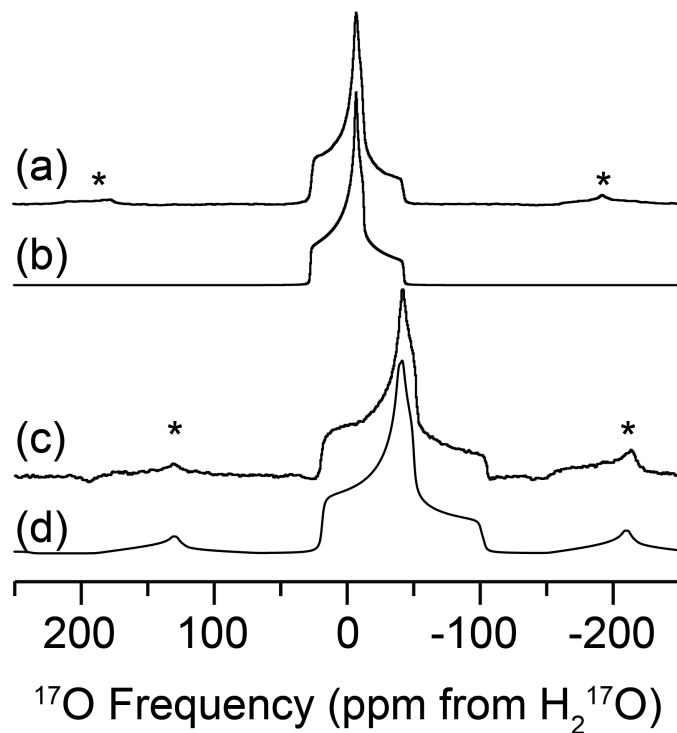


Figure S1. ^{17}O MAS NMR spectra and simulation of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$ at (a,b) 18.8 T ($\omega_{\text{OH}}/2\pi = 800$ MHz) and (c,d) 14.1 T ($\omega_{\text{OH}}/2\pi = 600$ MHz) at room temperature. Simulated NMR parameters: $C_Q = 6.9 \pm 0.2$ MHz, $\eta_Q = 0.98 \pm 0.05$, $\delta_{\text{iso}} = 21 \pm 1$ ppm. Asterisks (*) denote spinning sidebands.

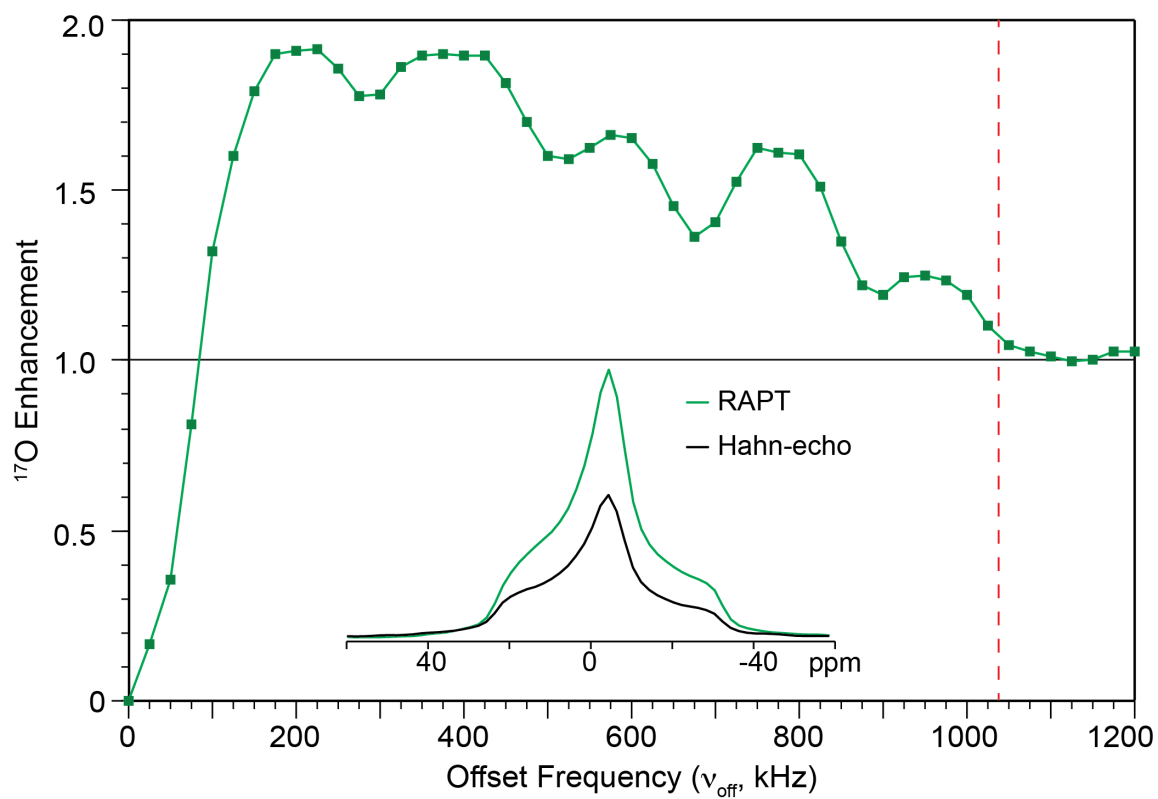


Figure S2. RAPT profile of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2^{17}\text{O}$. The edge frequency (ν_{edge}) is indicated by the dotted vertical line (red) and is related to the quadrupole coupling constant by the equation: $\nu_{\text{edge}} = 3C_Q/(2I(2I-1))$. Inset: RAPT enhancement with $\nu_{\text{off}} = 350$ kHz.

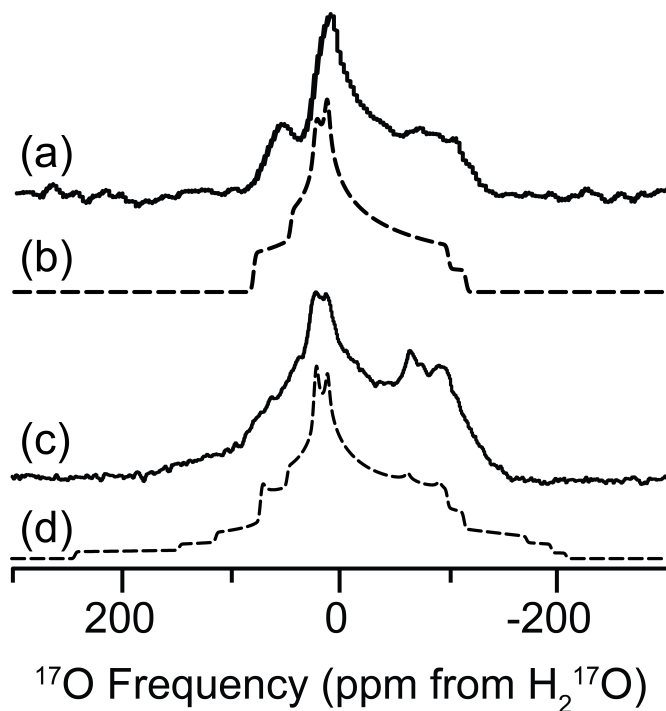


Figure S3: Stationary ^{17}O NMR spectra and simulation of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$ at 21.1 T ($\omega_{\text{OH}}/2\pi = 900$ MHz) and 270 K with (a,b) and without (c,d) continuous-wave ^1H decoupling ($\gamma B_1/2\pi = 100$ kHz). Simulated NMR parameters: (b) $C_Q = 6.9 \pm 0.2$ MHz, $\eta_Q = 0.98 \pm 0.02$, $\delta_{\text{iso}} = 21 \pm 1$ ppm, $\zeta_\delta = 25 \pm 5$ ppm, and $\eta_\delta = 0.25 \pm 0.25$; (c) identical to (b) with the addition of $D_{\text{O-H}} = 10 \pm 2$ kHz ($\eta=1$).

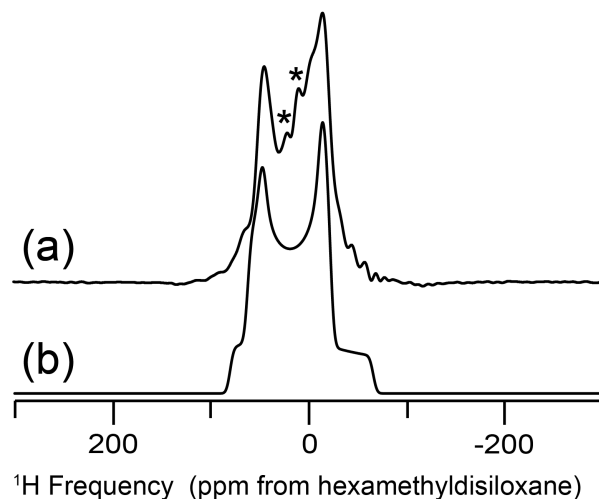


Figure S4. Stationary ^1H NMR (a) spectra and (b) simulation of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$ at 16.4 T ($\omega_{\text{OH}}/2\pi = 699$ MHz) Simulations with CSA parameters: $\delta_{\text{iso}} = 4 \pm 1$ ppm, $\zeta_\delta = -10 \pm 2$ ppm, $\eta_\delta = 0.9 \pm 0.2$, and dipole coupling constant, $D = 29 \pm 1$ kHz. Peaks indicated with asterisks (*) are from the rotor and stator background. Simulation is a verification of Carnevale *et al.*¹⁵

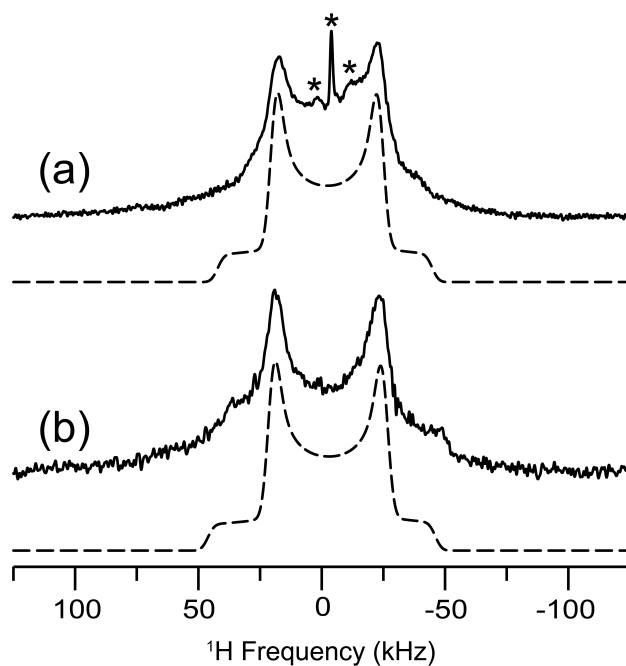


Figure S5. Stationary ^1H NMR spectra and simulations of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$ at 5 T ($\omega_{\text{OH}}/2\pi = 212.026$ MHz) at (a) 300 K and (b) 95 K. (a) Simulation (dashed) using with CSA parameters: $\zeta_\delta = -10 \pm 2$ ppm, $\eta_\delta = 0.9 \pm 0.2$, and dipole coupling constant, $D = 29 \pm 1$ kHz. (b) Simulation (dashed) using with CSA parameters: $\zeta_\delta = -18 \pm 2$ ppm, $\eta_\delta = 0.2 \pm 0.2$, and dipole coupling constant, $D = 31 \pm 1$ kHz. Peaks indicated with asterisks (*) are from the probe background.

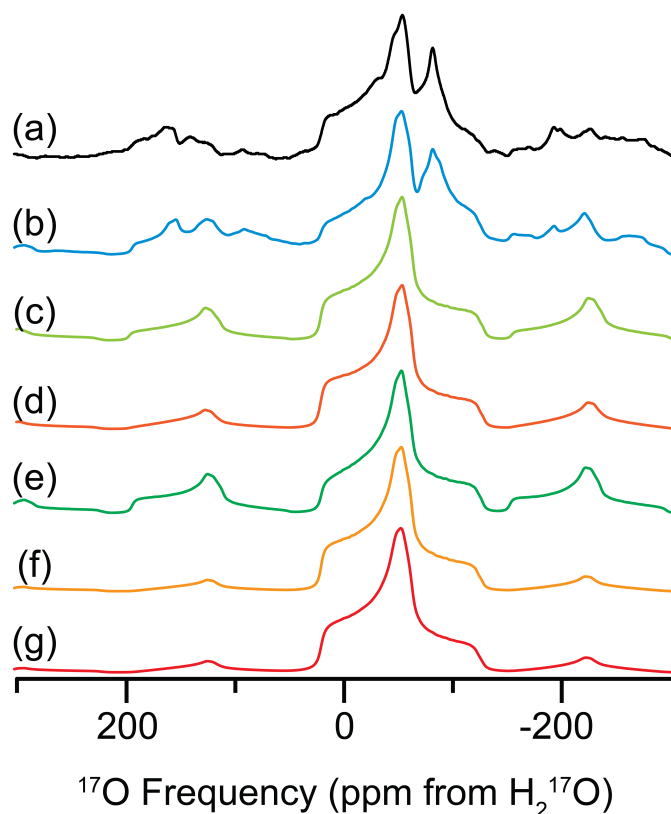


Figure S6. Experimental (a) and simulated (b-g) ^{17}O MAS spectra of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2^{17}\text{O}$ at 14.1 T ($\omega_{\text{OH}}/2\pi = 600$ MHz): (a) experimental spectrum of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2^{17}\text{O}$ at 105 ± 5 K without ^1H decoupling, (b) simulation of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2^{17}\text{O}$ in the rigid lattice limit, (c) simulation of MAS NMR spectrum of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{HD}^{17}\text{O}$ in the rigid lattice limit, (d) simulation of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{D}_2^{17}\text{O}$ in the rigid lattice limit, (e) simulation of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2^{17}\text{O}$ in the rigid lattice limit excluding the ^1H - ^1H dipole coupling; (f) simulation of $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2^{17}\text{O}$ in the rigid lattice limit excluding the ^{17}O - ^1H dipole coupling; (g) simulation of ^{17}O in the rigid lattice limit with 100 kHz ^1H decoupling.

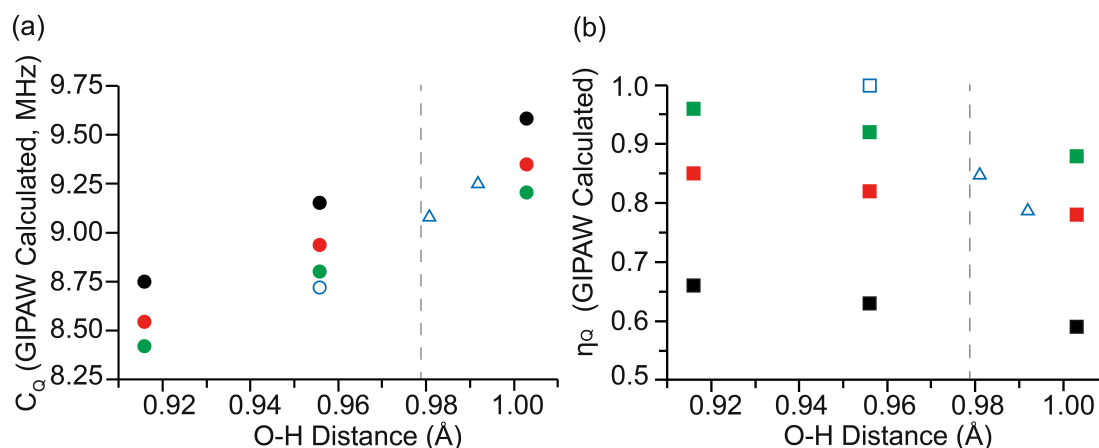


Figure S7. Plots of the refined structure calculations using GIPAW that relate the O-H distance to (a) calculated C_Q and (b) calculated η_Q . The black, red, and green filled points are grouped as the minimum, average, and maximum HOH angle, respectively according to Chiari *et al.*¹⁶ The open blue points represent NMR refined structures with fixed H—H distance of 1.62 ± 0.02 Å; the open blue circle/square represents

the best fit NMR refined structure that is near to the thermally corrected O-H distance.¹⁷ The dashed vertical line (grey) represents the O-H distance from the H-optimized GIPAW calculation.

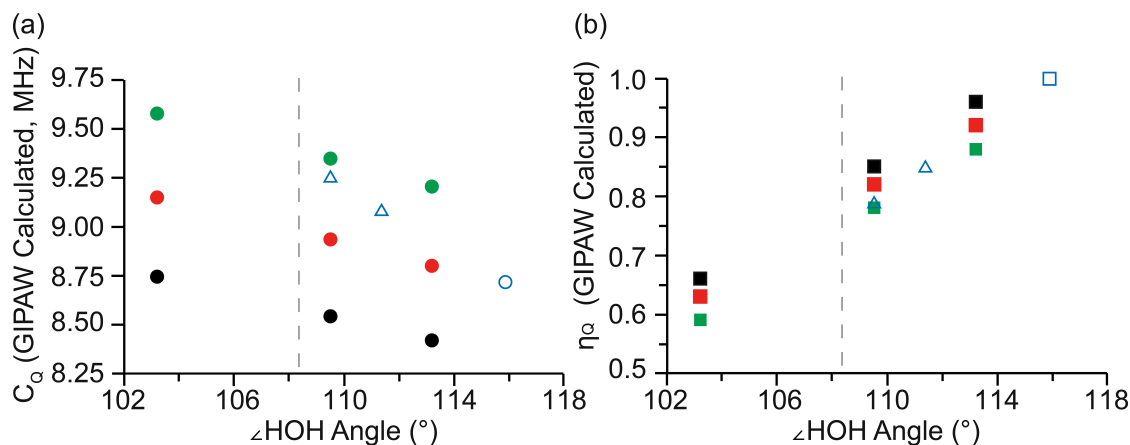


Figure S8. Plots of the refined structure calculations using GIPAW that relate the \angle HOH angle to (a) calculated C_Q and (b) calculated η_Q . The black, red, and green filled points are grouped as the minimum, average, and maximum O-H distance respectively according to Chiari *et al.*¹⁶ The open blue points represent NMR refined structures with fixed H---H distance of 1.62 ± 0.02 Å; the open blue circle/square represent the best fit NMR refined structure that is near to the thermally corrected O-H distance.¹⁷ The dashed vertical line represents the \angle HOH angle from the H-optimized GIPAW calculation.

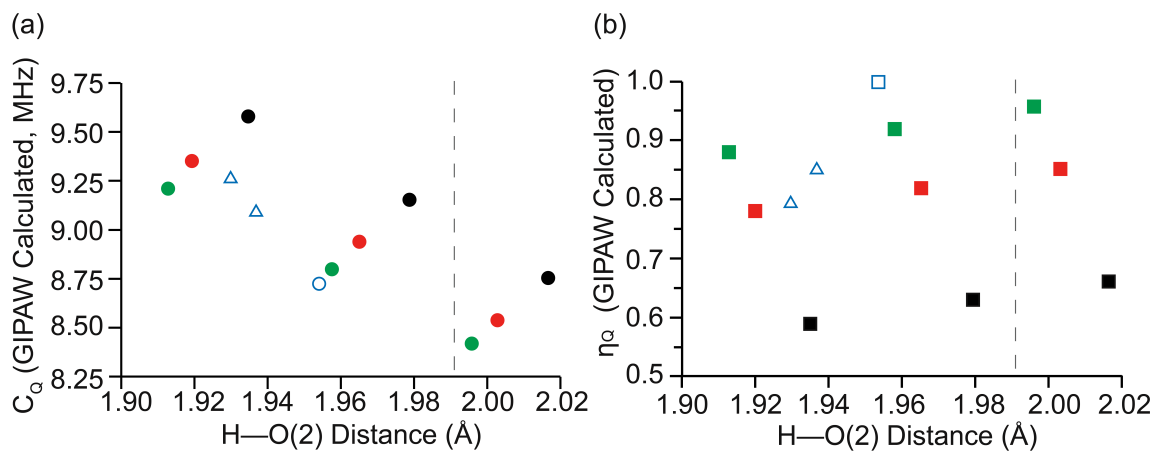


Figure S9. Plots of the refined structure calculations using GIPAW that relate the H—O(2) distance to (a) calculated C_Q and (b) calculated η_Q . The black, red, and green filled points are grouped as the minimum, average, and maximum \angle HOH angle respectively according to Chiari *et al.*¹⁶ The open blue points represent NMR refined structures with fixed H---H distance of 1.62 ± 0.02 Å; the open blue circle/square represents the best fit NMR refined structure that is near to the thermally corrected O-H distance.¹⁷ The dashed vertical line (grey) represents the H—O(2) distance from the H-optimized GIPAW calculation.

Table S1: Structural details and GIPAW calculated ^{17}O EFG parameters for $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$

Structure	O-H distance (Å)	\angle HOH angle (°)	H---H distance (Å)	H—O(2) distance (Å)	C_Q (MHz)	η_Q
H-opt neutron structure	0.979	108.4	1.588	1.991	9.163	0.76
1	0.916	103.2	1.436	2.017	8.747	0.66
2	0.916	109.5	1.496	2.003	8.545	0.85
3	0.916	113.2	1.529	1.996	8.421	0.96
4	0.956	103.2	1.498	1.979	9.151	0.63
5	0.956	109.5	1.561	1.965	8.936	0.82
6	0.956	113.2	1.596	1.958	8.802	0.92
7	1.003	103.2	1.572	1.935	9.58	0.59
8	1.003	109.5	1.638	1.920	9.348	0.78
9	1.003	113.2	1.675	1.913	9.205	0.88
10	0.992	109.5	1.620	1.930	9.256	0.79
11	0.956	115.9	1.620	1.954	-8.718	1.00
12	0.918	111.4	1.620	1.937	9.089	0.85

Table S2: GIPAW calculated ^{17}O EFG parameters for $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$

	C_Q (MHz)	η_Q	σ_{iso} (ppm)	ζ_δ (ppm)	η_δ	σ_{11} (ppm)	σ_{22} (ppm)	σ_{33} (ppm)
H-opt	9.163	0.76	254.99	20.307	0.230	267.479	262.808	234.683

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