

Supporting Information:

Example calculation for determining solid solubility using the MOSCED model with the Wilson G<sup>E</sup> equation

Solvent: 2-butanone

Solute: Benzimidazole

Temperature: 298 K

## 1. Obtain pure component data for solute and solvent

MOSCED Parameters	2-butanone (1)	Benzimidazole(2)
$\lambda$ (J/cm <sup>3</sup> ) <sup>0.5</sup>	14.74	16.21
$\tau$ (J/cm <sup>3</sup> ) <sup>0.5</sup>	6.64	4.22
$\alpha$ (J/cm <sup>3</sup> ) <sup>0.5</sup>	0	12.15
$\beta$ (J/cm <sup>3</sup> ) <sup>0.5</sup>	9.70	11.12
$q$	1	0.9
$v$ (cm <sup>3</sup> /mol)	90.2	92
$\Delta H^{fus}$ (kJ/mol)		22.7
$T^m$ (K)		444

## 2. Calculate infinite dilution activity coefficients using MOSCED

Calculation of  $\gamma_1^\infty$

$$R = 8.314 \frac{\text{J}}{\text{mol} \cdot \text{K}}$$

$$\alpha_1^T = \alpha_1 \left( \frac{293}{T} \right)^{0.8} = 0$$

$$\beta_1^T = \beta_1 \left( \frac{293}{T} \right)^{0.8} = 9.57$$

$$\tau_1^T = \tau_1 \left( \frac{293}{T} \right)^{0.4} = 6.6$$

$$POL_1 = q^4 \left( 1.15 - 1.15 \exp(-0.002337(\tau_1^T)^3) \right) + 1 = 1.56$$

$$\psi_1 = POL_1 + 0.002629\alpha_1^T\beta_1^T = 1.56$$

$$\xi_1 = 0.68(POL_1 - 1) + \left[ 3.24 - 2.4 \exp(-0.002687(\alpha_1\beta_1)^{1.5}) \right]^{\left( \frac{293}{T} \right)^2} = 1.23$$

$$aa_1 = 0.953 - 0.002314 \left( (\tau_1^T)^2 + \alpha_1^T\beta_1^T \right) = 0.85$$

$$d_{21} = \ln \left( \frac{v_1}{v_2} \right)^{aa_1} + 1 - \left( \frac{v_1}{v_2} \right)^{aa_1} = -0.00014$$

$$\ln \gamma_1^\infty = \frac{v_1}{RT} \left[ (\lambda_2 - \lambda_1)^2 + \frac{q_2^2 q_1^2 (\tau_2^T - \tau_1^T)^2}{\psi_2} + \frac{(\alpha_2^T - \alpha_1^T)(\beta_2^T - \beta_1^T)}{\xi_2} \right] + d_{21} = 0.36$$

$$\gamma_1^\infty = 1.43$$

$$\text{Calculation of } \gamma_2^\infty$$

$$\alpha_2^T = \alpha_2 \left( \frac{293}{T} \right)^{0.8} = 11.99$$

$$\beta_2^T = \beta_2 \left( \frac{293}{T} \right)^{0.8} = 10.97$$

$$\tau_2^T = \tau_2 \left( \frac{293}{T} \right)^{0.4} = 4.19$$

$$POL_2 = q^4 \left( 1.15 - 1.15 \exp(-0.002337(\tau_2^T)^3) \right) + 1 = 1.12$$

$$\psi_2 = POL_2 + 0.002629\alpha_2^T\beta_2^T = 1.47$$

$$\xi_2 = 0.68(POL_2 - 1) + \left[ 3.24 - 2.4 \exp\left(-0.002687(\alpha_2 \beta_2)^{1.5}\right) \right]^{(293/T)^2} = 3.16$$

$$aa_2 = 0.953 - 0.002314((\tau_2^T)^2 + \alpha_2^T \beta_2^T) = 0.62$$

$$d_{12} = \ln\left(\frac{v_2}{v_1}\right)^{aa_2} + 1 - \left(\frac{v_2}{v_1}\right)^{aa_2} = -7.4 \cdot 10^{-5}$$

$$\ln \gamma_2^\infty = \frac{v_2}{RT} \left[ (\lambda_1 - \lambda_2)^2 + \frac{q_1^2 q_2^2 (\tau_1^T - \tau_2^T)^2}{\psi_1} + \frac{(\alpha_1^T - \alpha_2^T)(\beta_1^T - \beta_2^T)}{\xi_1} \right] + d_{12} = 0.65$$

$$\gamma_2^\infty = 1.91$$

### 3. Calculate Wilson parameters from predicted infinite dilution activity coefficients

Solve the Wilson equation for two unknown interaction parameters.

$$\ln \gamma_1^\infty = 1 - \ln \Lambda_{12} - \Lambda_{21} = 0.36$$

$$\ln \gamma_2^\infty = 1 - \ln \Lambda_{21} - \Lambda_{12} = 0.65$$

Solving for  $\Lambda_{12}$  and  $\Lambda_{21}$  yields

$$\Lambda_{12} = 1.28$$

$$\Lambda_{21} = 0.396$$

### 4. Calculate solubility using Wilson equation and ideal solubility

Solve for  $x_2$  in

$$x_2 \gamma_2 = x_2^{ideal}$$

where

$$\ln \gamma_2 = -\ln(x_2 + \Lambda_{21}x_1) - x_1 \left( \frac{\Lambda_{12}}{x_1 + \Lambda_{12}x_2} - \frac{\Lambda_{21}}{\Lambda_{21}x_1 + x_2} \right) \text{ and}$$

$$x_2^{ideal} = \exp\left[ \frac{-\Delta H_{fus}}{RT_m} \left( \frac{T_m}{T} - 1 \right) \right]$$

$$x_2^{ideal} = 0.04854$$

Solution is  $x_2=0.027$  and  $\gamma_2=1.79$