Supporting Information

Thermal Conductivity of Methane Hydrate from Experiment and Molecular Simulation

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Compaction Pressure	Thermal Conductivity	Thermal Diffusivity	Data		
(MPa)	$(W/m\cdot K)$	(m^2/s)	points		
Data at 261.5 K, 4.68 I	MPa methane pressure		_		
37.59 ± 0.14	0.665 ± 0.013	$2.00E-07 \pm 5.69E-09$	17		
31.76 ± 0.15	0.679 ± 0.012	$1.96E-07 \pm 2.91E-09$	5		
25.03 ± 0.38	0.684 ± 0.012	$1.91E-07 \pm 6.41E-09$	16		
19.62 ± 0.04	0.669 ± 0.024	$2.03E-07 \pm 8.90E-09$	3		
13.24 ± 0.24	0.680 ± 0.020	$1.94E-07 \pm 5.66E-09$	4		
7.45 ± 0.02	0.676 ± 0.011	$1.93E-07 \pm 4.18E-09$	21		
43.74 ± 0.40	0.684 ± 0.006	$1.94E-07 \pm 4.97E-09$	4		
41.95 ± 0.31	0.695 ± 0.004	$1.96E-07 \pm 3.54E-09$	3		
2.50 ± 0.16	0.689 ± 0.008	$2.03E-07 \pm 1.53E-09$	3		
Data at 275.4 K, 4.62 MPa methane pressure					
26.88 ± 0.21	0.677 ± 0.011	$2.07E-07 \pm 6.05E-09$	3		

Table S1. Thermal conductivity and thermal diffusivity results for compacted methane hydrate as a function of compaction pressure and temperature. Thermal conductivity results are shown in Figure 5 and represent data taken during three out of four cycles of releasing and applying compaction pressure.

		Thermal		
Temperature	Methane Pressure	Conductivity	Thermal Diffusivity	Data
(K)	(MPa	$(W/m\cdot K)$	(m^2/s)	points
261.55 ± 0.01	(*See caption)	0.685 ± 0.011	$2.01E-07 \pm 5.76E-09$	91
275.40 ± 0.03	(*See caption)	0.679 ± 0.013	$2.08E-07 \pm 1.09E-08$	16
277.38 ± 0.01	6.30 ± 0.02	0.684 ± 0.002	$2.14E-07 \pm 1.36E-10$	2

Table S2. Thermal conductivity and thermal diffusivity results for compacted methane hydrate as a function of temperature. Thermal conductivity and thermal diffusivity results are shown in Figures 6 and 7, respectively. Data were taken over a range of compaction pressures from 2.5 to 43.7 MPa and include the data in Table S1 and the data in Table S6 that were collected at similar methane pressures (marked with #).

Pressure		100 %	90 %	80 %
(MPa)	Potential	Occupation	Occupation	Occupation
0.1	TIP4P-FQ	972.9 ± 4.2		948.8 ± 3.5
	SPC/E	944.2 ± 3.9		921.9 ± 4.5
9.5	TIP4P-FQ	974.7 ± 3.1	963.7 ± 6.3	950.5 ± 3.2
	SPC/E	945.1 ± 3.4	935.7 ± 6.2	922.9 ± 3.6
	TIP4P-Ew	939.9 ± 3.9	927.9 ± 5.7	917.1 ± 4.1
15	TIP4P-FQ	976.3 ± 3.5		951.8 ± 3.6
	SPC/E	945.7 ± 3.2		923.7 ± 3.8
30	TIP4P-FQ	978.7 ± 3.3		954.5 ± 3.8
	SPC/E	947.8 ± 4.1		925.0 ± 4.4
50	TIP4P-FQ	981.4 ± 3.8		956.7 ± 3.0
	SPC/E	950.2 ± 3.3		928.2 ± 3.3
100	TIP4P-FQ	984.0 ± 3.9		956.7 ± 4.2
	SPC/E	954.9 ± 3.8		932.8 ± 3.7

Table S3. Density results (kg/m³) for 8-unit cell systems at 276 K for 80 to 100% methane occupations.

Pressure		100%	90%	80%
(MPa)	Potential	Occupation	Occupation	Occupation
0.1	TIP4P-FQ	23.55 ± 0.034		23.55 ± 0.029
	SPC/E	23.79 ± 0.033		23.78 ± 0.039
9.5	TIP4P-FQ	23.54 ± 0.025	23.53 ± 0.051	23.54 ± 0.026
	SPC/E	23.78 ± 0.028	23.76 ± 0.052	23.77 ± 0.031
	TIP4P-Ew	23.83 ± 0.033	23.83 ± 0.049	23.82 ± 0.035
15	TIP4P-FQ	23.53 ± 0.028		23.53 ± 0.030
	SPC/E	23.78 ± 0.027		23.76 ± 0.032
30	TIP4P-FQ	23.51 ± 0.026		23.50 ± 0.031
	SPC/E	23.76 ± 0.034		23.75 ± 0.038
50	TIP4P-FQ	23.49 ± 0.030		23.49 ± 0.024
	SPC/E	23.74 ± 0.027		23.72 ± 0.028
100	TIP4P-FQ	23.46 ± 0.031		23.49 ± 0.034
	SPC/E	23.70 ± 0.031		23.68 ± 0.031

Table S4. Lattice parameters (Å) for 8-unit cell systems at 276 K for 80 to 100% methane occupations.

Pressure	Potential	100 %	90 %	80 %
(MPa)		Occupation	Occupation	Occupation
0.1	TIP4P-FQ	0.725 ± 0.016		0.754 ± 0.014
	SPC/E	0.526 ± 0.010		0.551 ± 0.011
9.5	TIP4P-FQ	0.711 ± 0.015	0.722 ± 0.020	0.742 ± 0.017
	SPC/E	0.517 ± 0.015	0.547 ± 0.013	0.561 ± 0.016
	TIP4P-Ew	0.562 ± 0.012	0.565 ± 0.011	0.588 ± 0.015
15	TIP4P-FQ	0.721 ± 0.013		0.743 ± 0.012
	SPC/E	0.528 ± 0.014		0.563 ± 0.015
30	TIP4P-FQ	0.733 ± 0.012		0.754 ± 0.011
	SPC/E	0.538 ± 0.010		0.557 ± 0.011
50	TIP4P-FQ	0.722 ± 0.018		0.767 ± 0.019
	SPC/E	0.537 ± 0.015		0.578 ± 0.017
100	TIP4P-FQ	0.741 ± 0.012		0.764 ± 0.015
	SPC/E	0.546 ± 0.011		0.573 ± 0.013

Table S5. Thermal conductivity results (W/m·K) for 8-unit cell systems at 276 K for 80 to 100% methane occupation.

Methane Pressure	Thermal Conductivity	Thermal Diffusivity	Data			
(MPa)	(W/m·K)	(m^2/s)	points			
Data at 261.54 ± 0.01 K						
10.06 ± 0.02	0.713 ± 0.004	$2.09E-07 \pm 4.68E-09$	2			
7.59 ± 0.00	0.669 ± 0.043	$2.25E-07 \pm 1.35E-08$	2			
$5.64 \pm 0.00 \text{ #}$	0.709 ± 0.008	$2.10E-07 \pm 6.63E-09$	7			
4.50 ± 0.01 #	0.703 ± 0.006	$2.12E-07 \pm 8.72E-09$	4			
$3.78 \pm 0.00 \text{ #}$	0.686 ± 0.009	$2.17E-07 \pm 9.97E-09$	4			
Data at 275.41 ± 0.0	02 K					
3.78	0.694	2.20E-07	1			
$5.59 \pm 0.01 \text{ #}$	0.684 ± 0.016	$2.20E-07 \pm 7.28E-09$	5			
7.47 ± 0.01	0.674 ± 0.010	$2.13E-07 \pm 5.31E-09$	3			
8.75 ± 0.00	0.666 ± 0.004	$2.16E-07 \pm 1.97E-09$	3			
12.43 ± 0.03	0.676 ± 0.004	$2.12E-07 \pm 2.33E-09$	4			
14.01 ± 0.04	0.678 ± 0.015	$2.12E-07 \pm 6.03E-09$	4			
Data at $277.40 \pm 0.01 \text{ K}$						
14.15 ± 0.04	0.664 ± 0.008	$2.15E-07 \pm 2.74E-09$	5			
12.58 ± 0.02	0.656 ± 0.001	$2.16E-07 \pm 1.21E-09$	3			
8.85 ± 0.01	0.662 ± 0.012	$2.16E-07 \pm 6.16E-09$	2			
7.54 ± 0.01	0.663 ± 0.011	$2.17E-07 \pm 5.14E-09$	3			
$6.30 \pm 0.02 ~\#$	0.684 ± 0.002	$2.14E-07 \pm 1.36E-10$	2			

Table S6. Thermal conductivity and thermal diffusivity results for compacted methane hydrate as a function of methane gas pressure and temperature. Thermal conductivity results are shown in Figure 11. Data were taken at a minimal compaction pressure of approximately 3 MPa. (Figure 11 also includes data from Table S1; the thermal conductivity results at 261.5 K averaged to give 0.680 ± 0.01 W/m·K. The data marked with a # were also used with the data in Table S2 in preparing Figures 6 and 7.)