

Supplementary Material

Deviations Between the
Experimental Pendant-Bubble
Dynamic Surface Tension Data
and the Diffusion-Controlled Model Fits

Three Features Suggesting the Possible Existence of Convective Currents at Time Scales Greater than 100 Seconds

- **Feature 1:** Whenever a significant percentage reduction in the dynamic surface tension takes place at time scales *smaller than 100 seconds*, there is good agreement between the experimental pendant-bubble dynamic surface tension (DST) data and the diffusion-controlled model fits.
- **Feature 2:** Whenever a significant percentage reduction in the dynamic surface tension takes place at time scales *greater than 100 seconds* (indicated by the **yellow regions**), there is relatively poor agreement between the experimental pendant-bubble DST data and the diffusion-controlled model fits.
- **Feature 3:** Whenever a significant reduction in the dynamic surface tension takes place at time scales *greater than 100 seconds* (indicated by the **yellow regions**), the experimental DST data reduces at a rate which is faster than that predicted by the diffusion-controlled model at long times (indicated by the **blue** colored ovals).

Percentage Reduction in the
Dynamic Surface Tension:

$$\frac{\gamma_{w/a} - \gamma(t)}{\gamma_{w/a} - \gamma_e} \times 100$$

$\gamma_{w/a}$ Water/air surface tension

$\gamma(t)$ Instantaneous surface tension at time t

γ_e Equilibrium surface tension

Surfactant:

Decanol

Equilibrium Adsorption

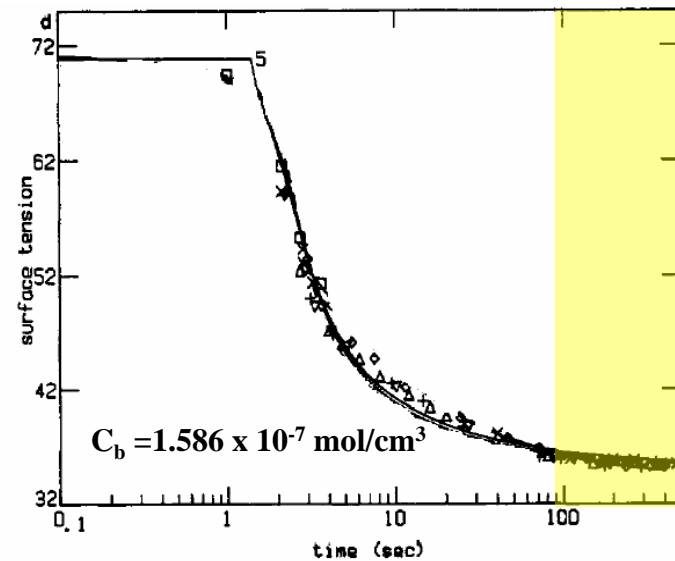
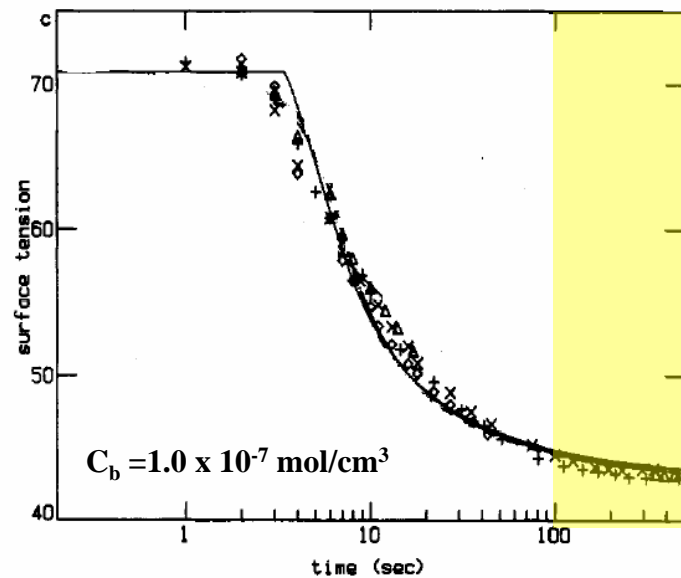
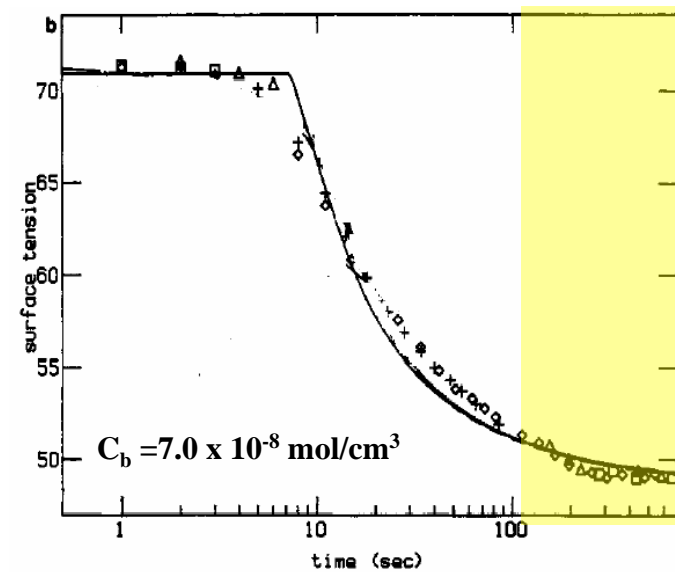
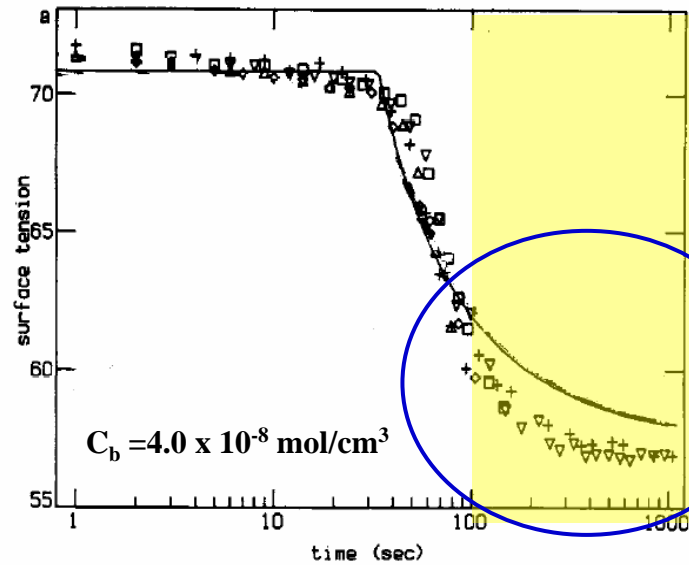
Model Used:

Phase Transition Model

Reference:

S-Y. Lin, K. Mckeigue, and C. Maldarelli,
Langmuir, 7, 1055-1066, 1991.

Adapted from Figure 3



Surfactant:

Decanol

Equilibrium Adsorption

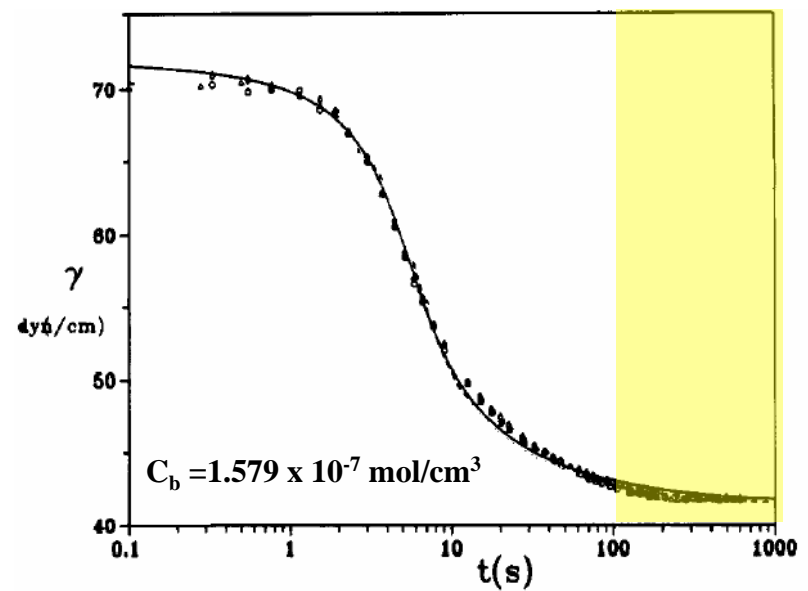
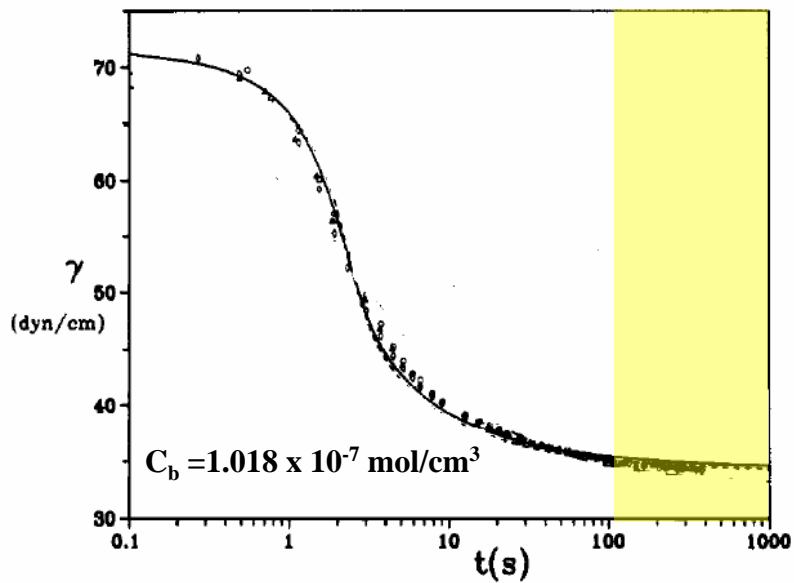
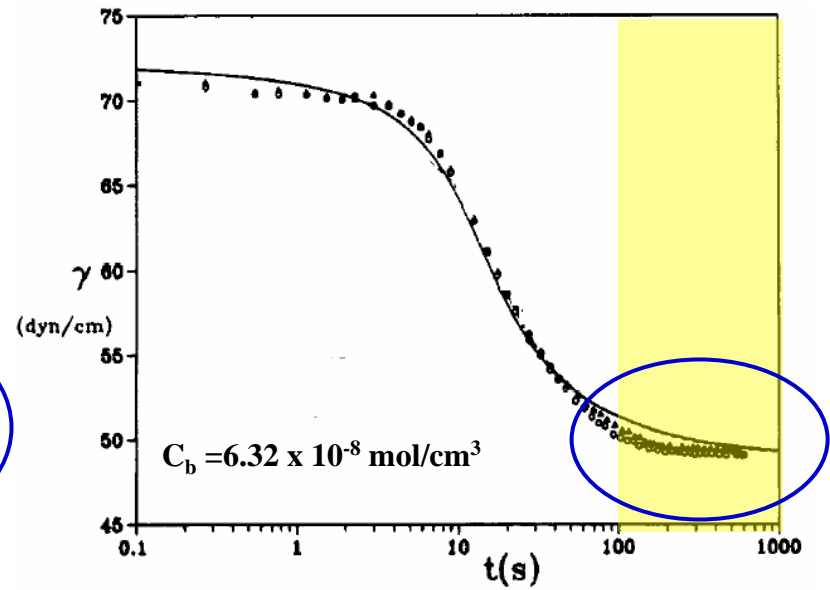
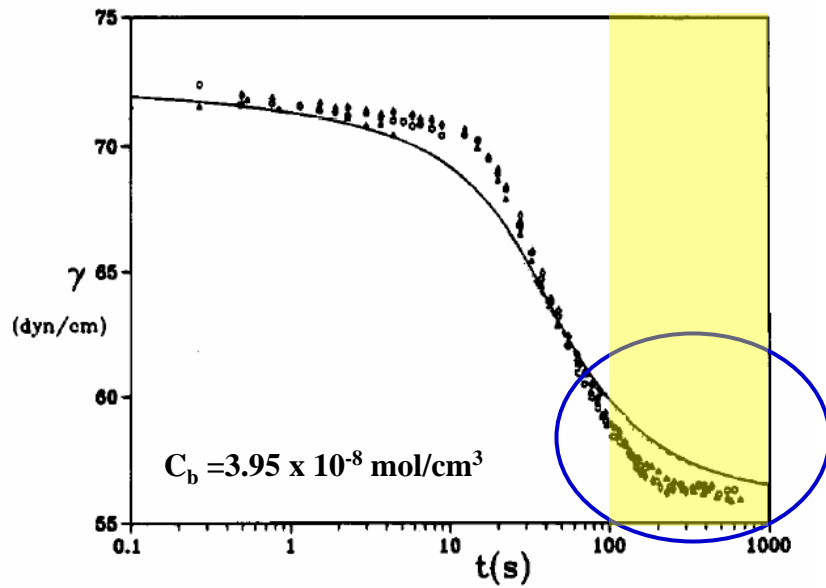
Model Used:

Generalized Frumkin Model

Reference:

S-Y. Lin, T-L. Lu, and W-B. Hwang,
Langmuir, 11, 555-562, 1995.

Adapted from Figure 3



Surfactant:

Nonanol

Equilibrium Adsorption

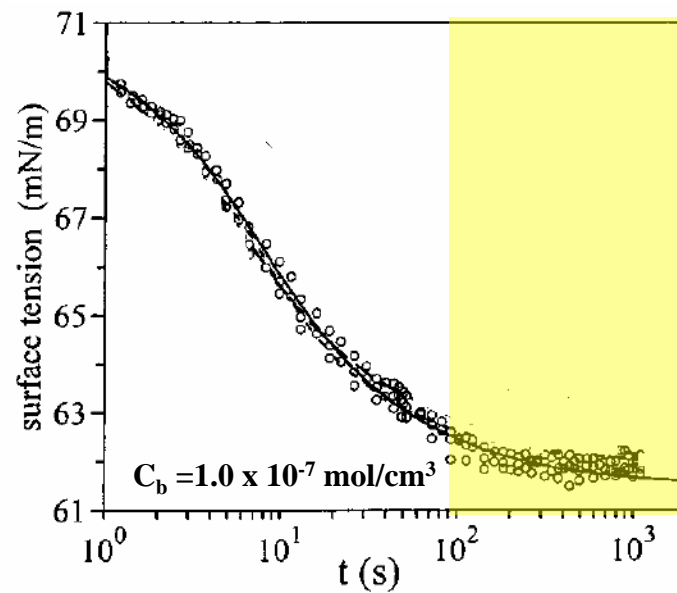
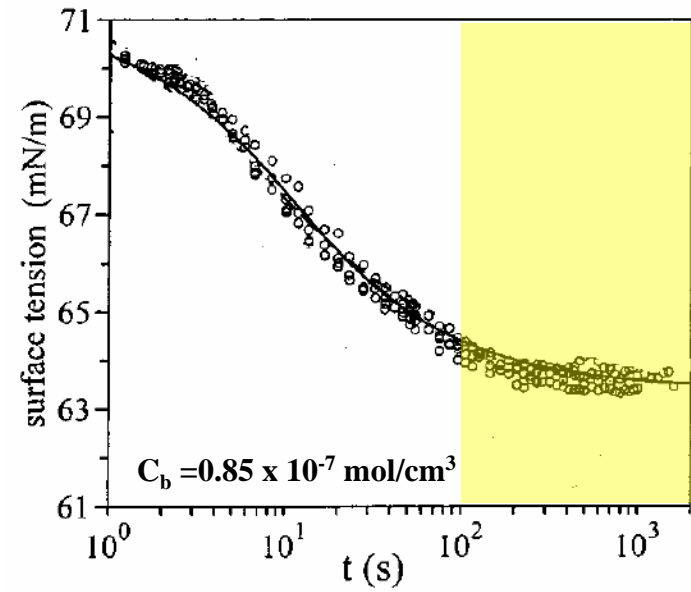
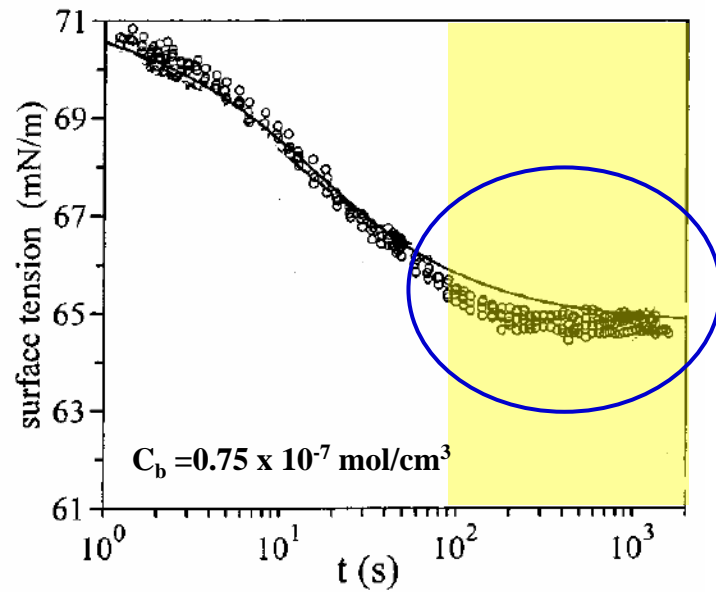
Model Used:

Generalized Frumkin Model

Reference:

Y-C. Lee, Y-B. Liou, R. Miller, H-S. Liu,
and S-Y. Lin, Langmuir, 11, 555-562,
1995.

Adapted from Figure 7



Surfactant:



Equilibrium Adsorption

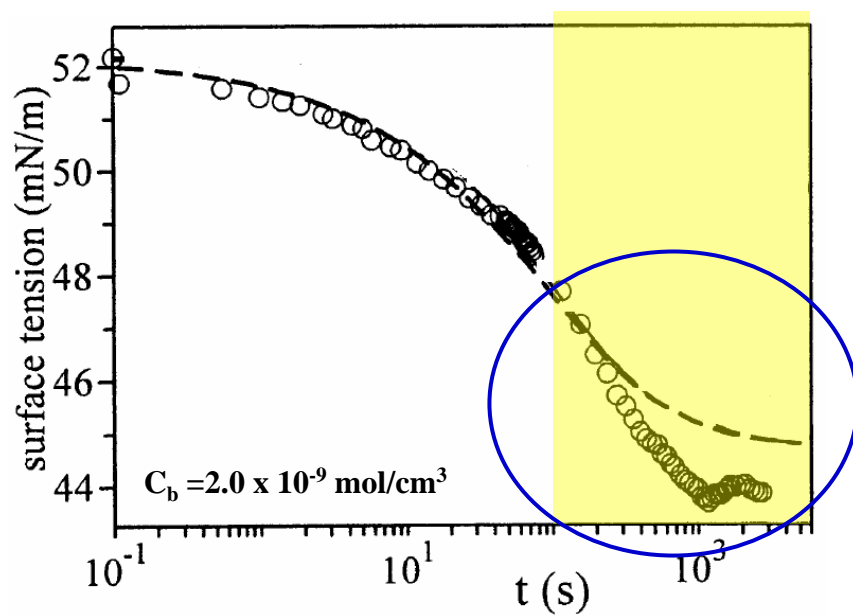
Model Used:

Generalized Frumkin Model

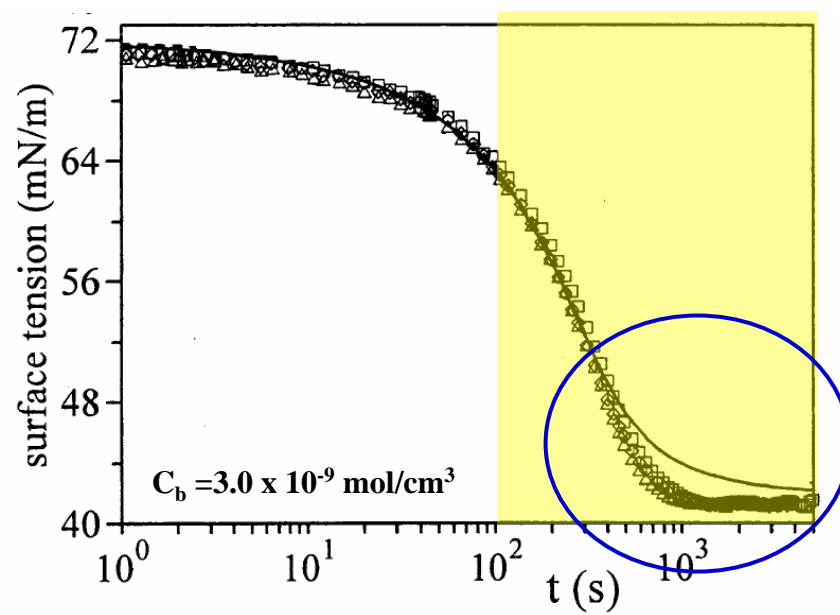
Reference:

Y-C. Lee, K. J. Stebe, H-S. Liu, and
S-Y. Lin, Colloids and Surfaces A:
Physicochem. Eng. Aspects, 220,
139-150, 2003.

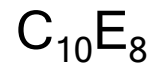
Adapted from Figure 5b



Adapted from Figure 10b



Surfactant:



Equilibrium Adsorption

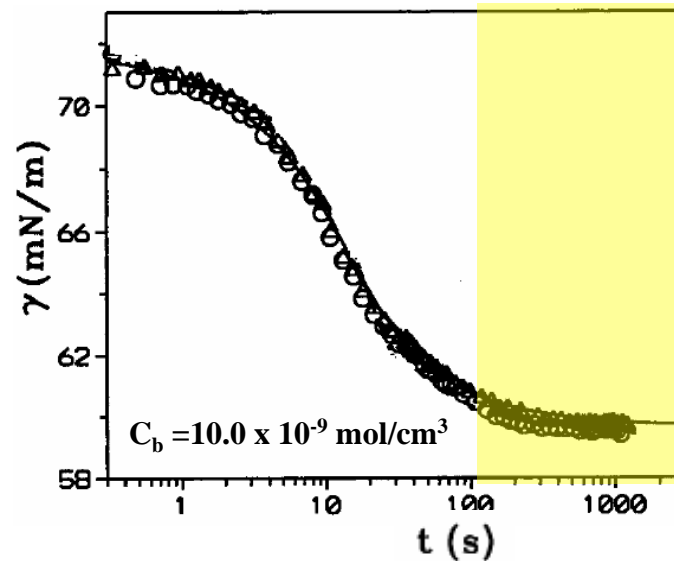
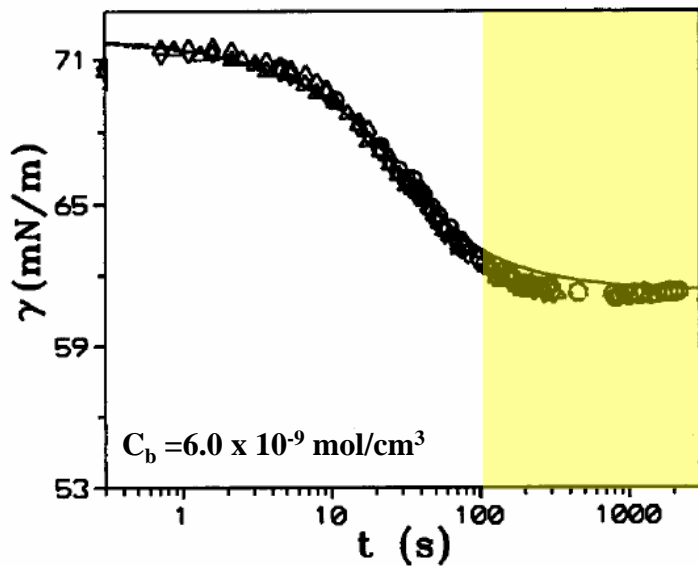
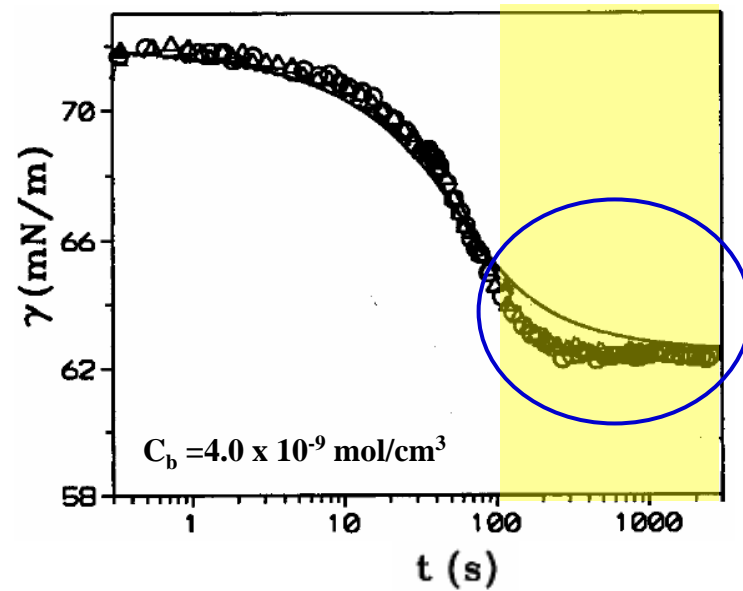
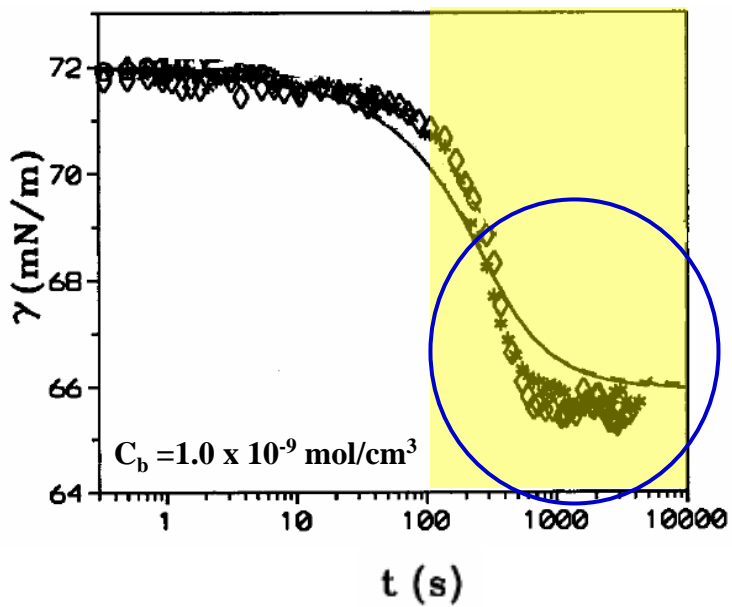
Model Used:

Generalized Frumkin Model

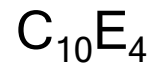
Reference:

H-C. Chang, C-T. Hsu, and S-Y. Lin,
Langmuir, 14, 2476-2484, 2003.

Adapted from Figure 2



Surfactant:



Equilibrium Adsorption

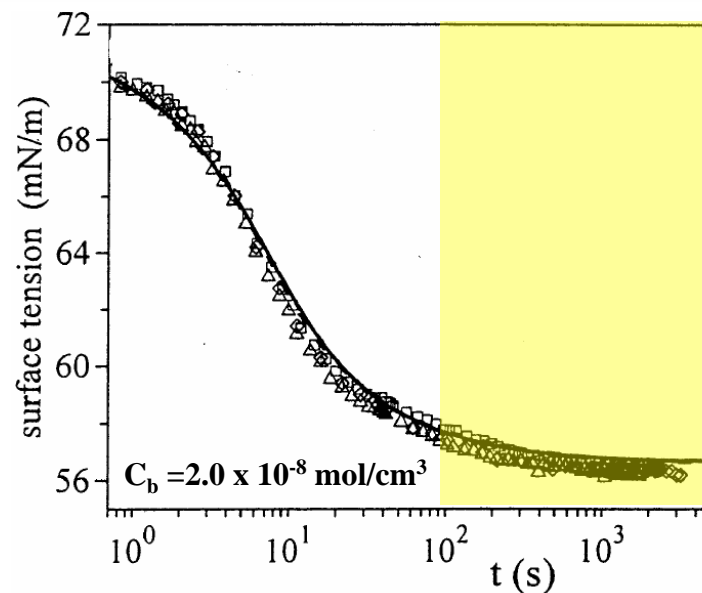
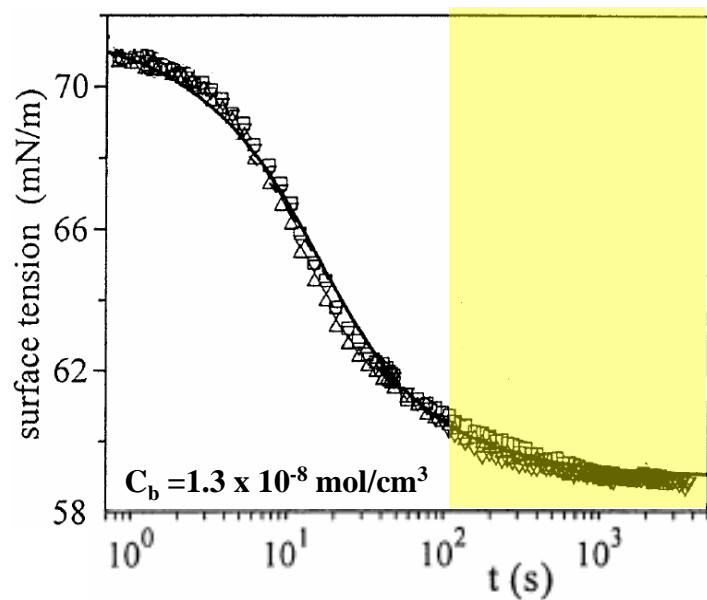
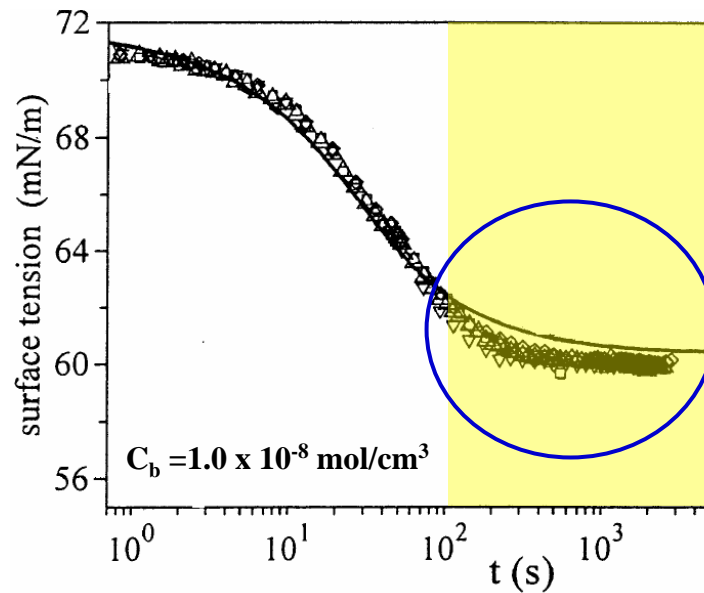
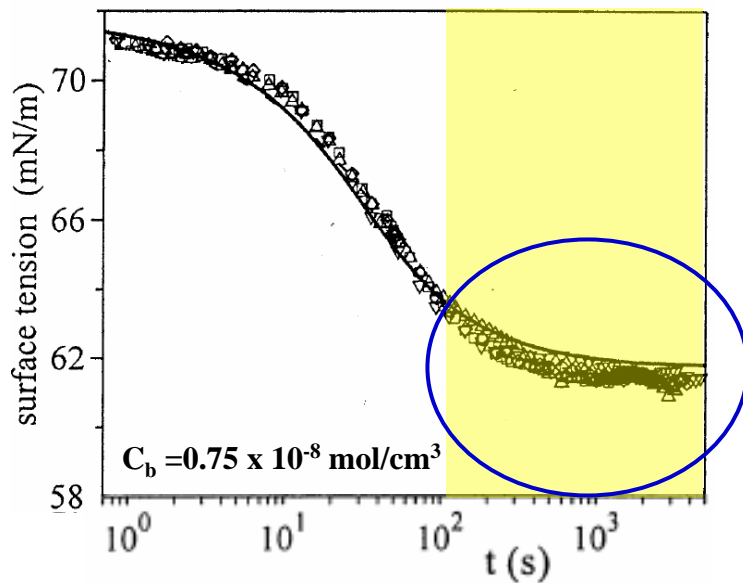
Model Used:

Generalized Frumkin Model

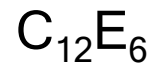
Reference:

Y-C. Lee, H-S. Liu, and S-Y. Lin,
Colloids and Surfaces A: Physicochem.
Eng. Aspects, 212, 123-134, 2003.

Adapted from Figure 8



Surfactant:
Equilibrium Adsorption



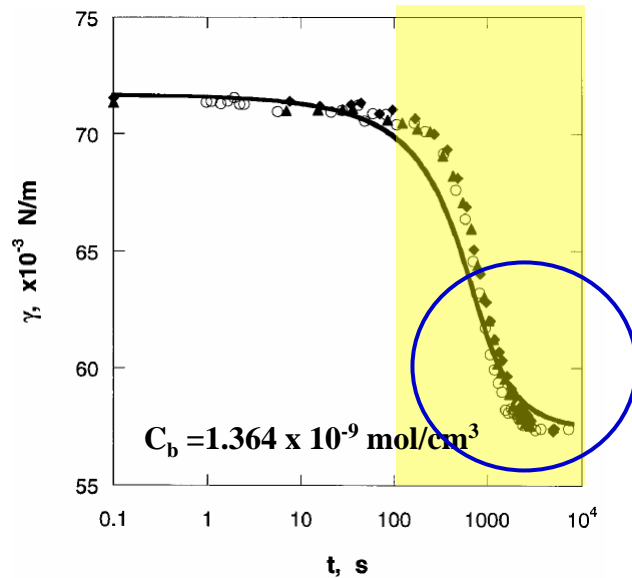
Model Used:

Frumkin Model

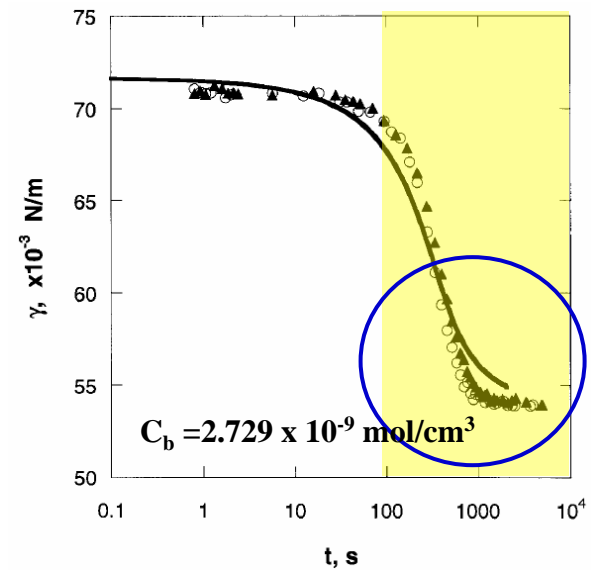
Reference:

R. Pan, J. Green, and C. Maldarelli,
Journal of Colloid and Interface Science,
205, 213-230, 1998.

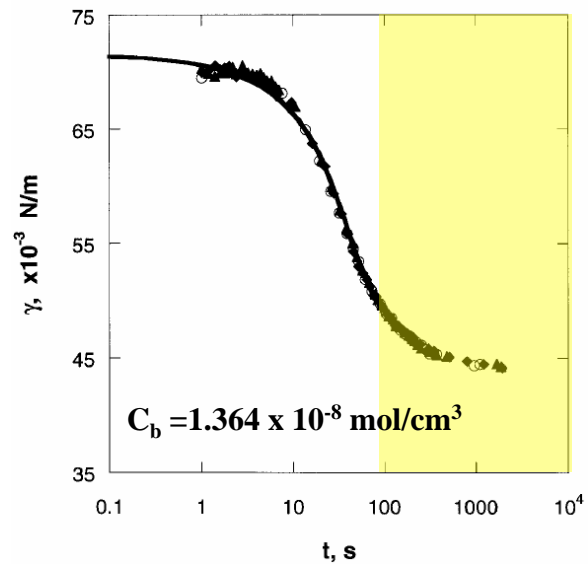
Adapted from Figure 11



Adapted from Figure 12



Adapted from Figure 13



Adapted from Figure 14

