Supporting Information

Microrheology with Fluorescence Correlation Spectroscopy

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Dynamic Light Scattering

Experimental Setup

In order to determine the diffusion coefficients of the tracer particles by an independent measurement dynamic light scattering experiment were carried out using a home-made apparatus equipped with a near-infrared diode laser from Schäfer und Kirchoff (SuK) company. The laser provides vertically polarized light at a wavelength of 831.5 nm with a power output of 80 mW (maximum of 60 mW on the sample). This laser wavelength lies far outside of the absorption bands of the tracer particles. Two avalanche diodes, SPCM-AQR-15 model from Perkin-Elmer company were used as detectors operated in the pseudo cross-correlation mode to suppress electronic artifact originating from the single detectors. The intensity correlation function $g_2(q,t)$ was calculated using a 5000/E/ALV hardware correlator. Here, q denotes the scattering vector and t the lag time covering a range from 0.2 ms up to 300 s. The experimental coherence factor, f=0.96, was determined using PS latex spheres (d=155 nm) in water (Duke Scientific). Using a circulating temperature bath the temperature at the sample position was kept fixed to 293.2 ± 0.1 K. Samples with solid concentration from $6.7\cdot10^{-3}$ wt% down to 4.6.10⁻⁴ wt% were measured in round Hellma cuvettes with a diameter of 20 mm. Samples were prepared by dilution from the stock solution of FluoSpheres® (FSP) provided by Molecular Probes, Inc.. The water used for dilution was filtered trough a 0.2 µm Millex®-HA filter (Millipore) beforehand. The refractive index $n_w=1.332$ and the viscosity $\eta_w=1.0015$ mPas of water at 293 K were taken from literature. Dynamic light scattering (DLS) spectra were taken

in 10° steps for scattering angles between θ =30° and 150°. Thus a scattering vector range from q=0.5210·10⁻³ nm⁻¹ to 1.944·10⁻³ nm⁻¹ is covered.

Data Evaluation

The Siegert relation $g_2(q,t) = 1 + f |g_1(q,t)|^2$ connects the intensity correlation function $g_2(q,t)$ to the electric field correlation function $g_1(q,t)$. The latter is directly related to the dynamic structure factor S(q,t) normalized to its value at t=0: $g_1(q,t) = S(q,t)/S(q,t=0)$. The z-averaged diffusion coefficient $\langle D \rangle$, the average bead hydrodynamic radius $\langle R_h \rangle$ and the width of the distributions, ΔD and ΔR_h , respectively, as a measure the polydispersity were determined using two different approaches: (1) CONTIN analysis [S1] and (2) cumulant which method, expands $\ln[g_1(q,t)]$ in a power series in t: $\ln[g_1(q,t)] = -K_1 \cdot t + (K_2/2) \cdot t^2 - \dots$ [S2] The first cumulant K_1 is related to the z-averaged diffusion coefficient by $K_1 = q^2 \langle D \rangle$. The second cumulant $K_2 = q^4 \langle \Delta D^2 \rangle$ measures the variance $\Delta D^2 = \langle (D - \langle D \rangle)^2 \rangle$ of the *D* distribution. The hydrodynamic radius $\langle R_h \rangle$ can be calculated using the Stokes-Einstein relation $\langle R_h \rangle = k_B T / (6\pi \eta_W \langle D \rangle)$, where $k_B = \text{Boltzmann}$ constant and T = temperature. The width $\langle \Delta R_h \rangle$ of the R_h distribution is given by $\Delta R_h/R_h = \Delta D/D = \sqrt{K_2/K_1}$. In Figure S1 the measured correlation functions are plotted as a function of time for some representative scattering angles. The solid lines show the result of a simultaneous fit of all spectra using the cumulant method with $\langle D \rangle$ and $\langle \Delta D^2 \rangle$ as only adjustable parameters. The q²-dependence expected for free diffusion is well preserved. Furthermore no dependence of the result on the particle concentration is observed. We obtain $\langle D \rangle = (3.4 \pm 0.2) \cdot 10^{-12} \text{ m}^2/\text{s}$ and $\Delta D / \langle D \rangle = 9\%$ which corresponds to a hydrodynamic radius of 3nm. In the insert of Figure S1 the R_h distribution obtained from the CONTIN analysis is shown for comparison. The result $\langle R_h \rangle = 64$ nm with a half-width-of-half-maximum of 11% corresponds well to the result obtained using the cumulant analysis.

References

- S1. Provencher, S.W. a) Comput. Phys. Commun. 1982, 27, 213-227. b) Comput. Phys. Commun. 1982, 27, 229-242.
- S2. Schärtl, W. Light Scattering from Polymer Solutions and Nanoparticle Dispersions; Springer: Berlin, 2007.

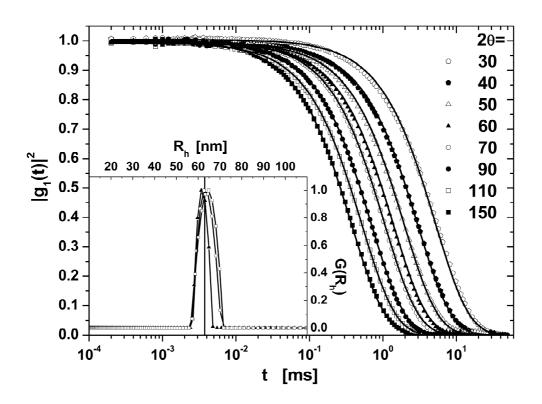


Figure S1: Correlation functions measured dynamic light scattering for the tracer beads in water for representative scattering angles (markers). The solid lines show the result of a simultaneous fit of all spectra using the cumulant analysis. For comparison the inset presents the distributions obtained for the hydrodynamic radius by applying the CONTIN method to the data taken at $2\theta=30^{\circ}$, 60° , 90° , 110° .