

## Supplementary Information

### Fast and accurate predictions of protein NMR chemical shifts from interatomic distances

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#### Hydrogen bonding term

The effects of hydrogen bonds originating on backbone  $H_N$  and O atoms are implemented in CamShift by assuming a correlation between chemical shift and hydrogen bond energy using results that were recently reported by David Baker and coworkers<sup>1</sup>. They determined the orientation and distance dependence of hydrogen bond dimerization energies using both quantum mechanical calculations and structural analysis for hydrogen bonds between side chain and backbone atoms<sup>1</sup>.

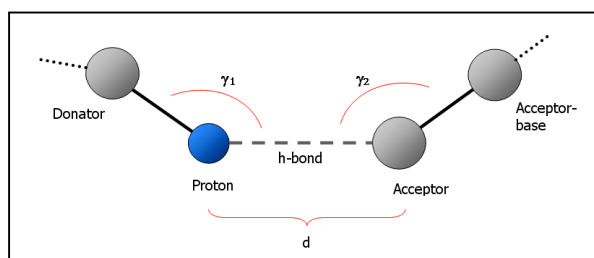


Figure S1. Geometric parameters used to model hydrogen bonding contributions to chemical shifts; hydrogen atoms (blue), heavy atoms (gray). The angles characterising the hydrogen bond geometry are denoted as  $\gamma_1$  and  $\gamma_2$  (corresponding to  $\theta$  and  $\psi$  in Ref<sup>1</sup>), and the hydrogen bond length is indicated as  $d$ .

The parameters that are used in the calculation of hydrogen bond energies are shown in Fig. S1. In the original study, data were calculated separately for different types of secondary structure elements<sup>1</sup>. For our purposes, we considered average values and fitted a single curve. We thus avoided having to subdivide the data used for training according to different secondary structure elements; a benefit in this procedure is that the chemical shift term remains differentiable and thus suitable for being used in restrained molecular dynamics simulations. Averages extracted from the data were fitted with a potential of the Lennard-Jones form

$$E(x) = p_1 \left( \left( \frac{p_2}{x} + p_4 \right)^r - \left( \frac{p_3}{x} + p_5 \right)^s \right) \quad (S1)$$

where  $E(x)$  denotes the energy corresponding to the parameter  $x$  (an angle or distance), and  $p_1$  through  $p_5$ ,  $r$ , and  $s$  are parameters determined by a Marquardt-Levenberg nonlinear least-squares fit.

|            | $p_1$     | $p_2$    | $p_3$     | $p_4$    | $p_5$    | $r$  | $s$   |
|------------|-----------|----------|-----------|----------|----------|------|-------|
| $\gamma_1$ | 15.0486   | -1.79469 | -1.79469  | 1.49398  | 1.49398  | 15.5 | 2.5   |
| $\gamma_2$ | 12.1514   | -1.12258 | -1.12258  | 1.30953  | 1.30953  | 15.5 | 3     |
| $D$        | -0.403531 | 13.9148  | -0.421725 | -3.08016 | 0.987251 | 3    | -16.5 |

Table S1. Values of the three parameters describing the backbone-backbone hydrogen bonding term in Eq. (S1), which are averaged over different types of secondary structure elements.

The chemical shift term for each of the three parameters is therefore

$$\delta_{hbond,x} = \alpha_{hbond,x} \left( p_{1,x} \left( \left( \frac{p_{2,x}}{x} + p_{4,x} \right)^r - \left( \frac{p_{3,x}}{x} + p_{5,x} \right)^s \right) \right) \quad (S2)$$

where  $x$  indicates  $\gamma_1$ ,  $\gamma_2$ , or  $d$ . The three different contributions are included in the CamShift equation with individual coefficients. The full chemical shift term for hydrogen bonds is therefore given by

$$\delta_{hbond} = \delta_{hbond,\gamma_1} + \delta_{hbond,\gamma_2} + \delta_{hbond,d} \quad (S3)$$

### Ring current term

CamShift implements the classic point-dipole method<sup>2</sup>

$$\delta_{ring} = \sum_i \alpha_{ring,i} \sum_{R(i)} \left[ \frac{1 - 3\cos^2(\theta)}{r^3} \right] \quad (S4)$$

where  $\theta$  is the angle between the vector normal to the ring plane and the vector connecting the ring centre and the target atom,  $r$  is the distance between that target atom and the ring centre (Fig. S2),  $i$  runs over the five different ring types (Phe, Tyr, His, Trp<sub>1</sub>, and Trp<sub>2</sub>, indicated by the corresponding amino acid three-letter code, with the latter two denoting the two different rings of tryptophan), and  $R(i)$  the set of all rings in a protein that are of type  $i$ .

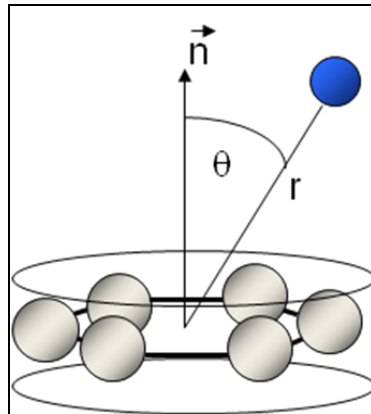


Figure S2: Illustration of the parameters used for the ring current term (Eq. S4). Atoms in the ring are shown as gray spheres and the query atom as a blue sphere at position  $\mathbf{r}$ ;  $\vec{n}$  is the normal vector to the ring plane and  $\theta$  the angle between  $\mathbf{r}$  and  $\vec{n}$ .

## Dihedral angle term

Dihedral angle contributions are fitted with a periodic function of the form

$$f(\theta) = p_1 \cos[3(\theta + p_4)] + p_2 \cos(\theta + p_5) + p_3 \quad (\text{S5})$$

where  $\theta$  indicates one among the three backbone dihedral angles  $\phi$ ,  $\psi$ , and  $\chi_1$ . The value of the parameters are given in Table S2.

|            |          | $p_1$      | $p_2$     | $p_3$     | $p_4$    | $p_5$    |
|------------|----------|------------|-----------|-----------|----------|----------|
| H $\alpha$ | $\phi$   | 0.3        | 0.4       | 0.0       | 0.1      | 3.0      |
|            | $\psi$   | -0.170287  | 0.278618  | 0.0609298 | 2.48692  | -3.07025 |
|            | $\chi_1$ | -0.0244394 | -0.137248 | 0.0560274 | -5.42115 | 2.27543  |
| C $\alpha$ | $\phi$   | 1.5        | -3.0      | 0.0       | 2.45     | -2.7     |
|            | $\psi$   | -0.4       | -1.5      | 0.7       | 4.8      | -8.4     |
|            | $\chi_1$ | 0.1        | 0.9       | 0.6       | -6.0     | 2.2      |
| H $_N$     | $\phi$   | -0.4       | -0.3      | 0.2       | 3.6      | -3.4     |
|            | $\psi$   | -0.104686  | 0.174676  | 0.0639679 | 3.51401  | -2.82811 |
|            | $\chi_1$ | 0.0343048  | 0.0448763 | 0.0406634 | 3.42026  | 4.15534  |
| N          | $\phi$   | -2.1       | -1.2      | 0.2       | 3.2      | -2.7     |
|            | $\psi$   | -1.4       | 2.2       | 0.3       | 4.2      | -2.5     |
|            | $\chi_1$ | 0.5        | 1.2       | -0.1      | 2.2      | 2.9      |
| C'         | $\phi$   | 0.9        | -2.9      | -1.2      | 2.4      | -2.5     |
|            | $\psi$   | -0.7       | -0.9      | 0.0       | 5.1      | -8.3     |
|            | $\chi_1$ | 0.1        | -0.5      | -0.1      | 19.9     | 11       |
| C $\beta$  | $\phi$   | 1.0        | 1.8       | 0.0       | 0.8      | 2.5      |
|            | $\psi$   | 0.5        | 2.0       | 0.8       | -0.6     | 2.6      |
|            | $\chi_1$ | -0.4       | 0.5       | 1.1       | 8.9      | 11       |

Table S2. Parameters used for the dihedral angle term (Eq. S5)

## Fitting of the CamShift parameters

Functions used to describe the hydrogen bonding (Eq. S1) were fitted with a Marquardt-Levenberg nonlinear least-squares fit, while the dihedral angle (Eq. S5) contributions were fitted using a combination of steepest descent and conjugate gradient minimization. The CamShift equation, which is a linear combination of these functions and of the distance-based terms described by Eq. 1 in the main text, was optimized by using a least-squares fit to find the set of coefficients that minimizes the deviations between predicted and experimental chemical shift values.

Distances along the backbone, which represent the dominant contribution to the chemical shifts, and all other contributions that are common among amino acids were fitted across the complete trainings data set (without glycine and proline residues) in order to minimize overfitting effects, while distances to side-chain atoms serve as residue-specific additional degrees of freedom to reduce the remaining differences between experimental and predicted chemical shifts. Since the fit includes many different side-chain atoms, the number of coefficients reported in Table S6 is significantly reduced on a per-residue basis. For glycine and proline residues we present separate sets of coefficients, since we found that because of their particular structural properties these two types of residues both disturb and suffer from coefficients optimized across all residue types.

### **Exclusion of distances with low variance-to-mean ratio**

The inclusion of near-constant distances (in particular between covalently bonded atoms) can cause instabilities in the fitting of the parameters in Eq. 1 in the main text. An iterative procedure was therefore used to exclude distances with limited variance in order to avoid such a behaviour. We first ranked all distances in the dataset of structures used for the fitting of the parameters according to their variance-to-mean ratios. We then started to iterate the fitting procedure in the following way: at each iteration, the top (i.e. the less variable) 10 distances were removed from the list and the chemical shift RMSD for a test set was calculated. The iterative elimination was repeated until a significant deterioration of the test set RMSD was observed. This procedure resulted in the exclusion of a number of distances ranging from 40 (for N atoms) to 100 (for H $\alpha$  atoms), and provided a stable predictor while keeping a high accuracy. Excluded distances are listed with a coefficient 0 in Table S6.

| CamShift           |      |       |            |           |            |                |      |      |
|--------------------|------|-------|------------|-----------|------------|----------------|------|------|
| PDB                | BMRB | Chain | C $\alpha$ | C $\beta$ | H $\alpha$ | H <sub>N</sub> | N    | C'   |
| 1iar               | 4094 | A     | 1.01       | 1.11      | 0.21       | 0.39           | 2.40 | 0.87 |
| 1bdo               | 4425 | A     | 1.31       | 1.30      | 0.24       | 0.45           | 2.49 |      |
| 1kmi               | 4472 | Y     | 1.10       | 1.21      | 0.23       | 0.62           | 2.87 |      |
| 1kqr               | 5275 | A     | 1.18       | 1.28      | 0.32       | 0.70           | 3.23 | 1.10 |
| 1mms               | 5513 | A     | 1.46       | 1.26      | 0.30       | 0.64           | 3.13 | 1.18 |
| 1fh9               | 7264 | A     | 1.21       | 1.37      |            | 0.60           | 3.07 | 1.28 |
| 2ihb               | 7272 | B     | 1.19       | 0.81      | 0.21       | 0.49           | 2.28 | 1.10 |
|                    |      |       |            |           |            |                |      |      |
| SPARTA             |      |       |            |           |            |                |      |      |
| PDB                | BMRB | Chain | C $\alpha$ | C $\beta$ | H $\alpha$ | H <sub>N</sub> | N    | C'   |
| 1iar               | 4094 | A     | 0.86       | 0.96      | 0.21       | 0.42           | 2.37 | 0.77 |
| 1bdo               | 4425 | A     | 0.99       | 1.08      | 0.25       | 0.41           | 2.48 |      |
| 1kmi               | 4472 | Y     | 0.97       | 1.02      | 0.26       | 0.63           | 2.57 |      |
| 1kqr               | 5275 | A     | 0.99       | 1.11      | 0.34       | 0.56           | 3.01 | 1.11 |
| 1mms               | 5513 | A     | 1.36       | 1.42      | 0.31       | 0.52           | 2.94 | 1.01 |
| 1fh9               | 7264 | A     | 1.04       | 1.30      |            | 0.63           | 2.75 | 1.25 |
| 2ihb               | 7272 | B     | 1.19       | 0.78      | 0.22       | 0.54           | 2.34 | 1.05 |
|                    |      |       |            |           |            |                |      |      |
| CamShift distances |      |       |            |           |            |                |      |      |
| PDB                | BMRB | Chain | C $\alpha$ | C $\beta$ | H $\alpha$ | H <sub>N</sub> | N    | C'   |
| 1iar               | 4094 | A     | 1.04       | 1.02      | 0.24       | 0.40           | 2.47 | 0.88 |
| 1bdo               | 4425 | A     | 1.38       | 1.30      | 0.25       | 0.50           | 2.54 |      |
| 1kmi               | 4472 | Y     | 1.12       | 1.28      | 0.26       | 0.66           | 2.84 |      |
| 1kqr               | 5275 | A     | 1.23       | 1.39      | 0.37       | 0.70           | 3.22 | 1.12 |
| 1mms               | 5513 | A     | 1.47       | 1.27      | 0.34       | 0.63           | 3.15 | 1.18 |
| 1fh9               | 7264 | A     | 1.23       | 1.41      |            | 0.63           | 3.08 | 1.32 |
| 2ihb               | 7272 | B     | 1.20       | 0.80      | 0.26       | 0.52           | 2.27 | 1.13 |
|                    |      |       |            |           |            |                |      |      |
| SHIFTX             |      |       |            |           |            |                |      |      |
| PDB                | BMRB | Chain | C $\alpha$ | C $\beta$ | H $\alpha$ | H <sub>N</sub> | N    | C'   |
| 1iar               | 4094 | A     | 0.98       | 1.18      | 0.24       | 0.43           | 2.71 | 1.02 |
| 1bdo               | 4425 | A     | 1.03       | 1.35      | 0.25       | 0.49           | 1.96 |      |
| 1kmi               | 4472 | Y     | 1.13       | 1.09      | 0.28       | 0.65           | 2.99 |      |
| 1kqr               | 5275 | A     | 1.13       | 1.23      | 0.36       | 0.59           | 3.01 | 1.11 |
| 1mms               | 5513 | A     | 1.47       | 1.38      | 0.32       | 0.60           | 2.92 | 1.20 |
| 1fh9               | 7264 | A     | 1.18       | 1.45      |            | 0.61           | 2.79 | 1.35 |
| 2ihb               | 7272 | B     | 1.16       | 0.92      | 0.23       | 0.54           | 2.11 | 1.05 |

Table S3.

Comparison between the predictions provided by SPARTA<sup>3</sup>, SHIFTX<sup>4</sup> and Camshift for a test set of seven proteins, which was previously used to compare SHIFTX and SPARTA. Chemical shift datasets were taken from the RefDB and re-referenced according to the method described by Zhang and coworkers<sup>5</sup>. All values are RMSDs in ppm.

| N               | H <sub>N</sub>  | H $\alpha$      | C $\alpha$      | C $\beta$       | C'              |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 3.01 $\pm$ 0.18 | 0.55 $\pm$ 0.04 | 0.28 $\pm$ 0.03 | 1.26 $\pm$ 0.10 | 1.28 $\pm$ 0.27 | 1.44 $\pm$ 0.55 |

Table S4.

Averages and standard deviations in ppm for ten randomly selected subsets of seven proteins extracted from the 28-protein test set.

|          |         | N    | H <sub>N</sub> | H $\alpha$ | C $\alpha$ | C $\beta$ | C'   |
|----------|---------|------|----------------|------------|------------|-----------|------|
| CamShift | All     | 2.87 | 0.58           | 0.26       | 1.21       | 1.22      | 1.15 |
|          | Helices | 2.26 | 0.49           | 0.21       | 1.05       | 0.94      | 1.10 |
|          | Strands | 3.29 | 0.61           | 0.30       | 1.21       | 1.40      | 1.17 |
|          | Coil    | 2.95 | 0.59           | 0.27       | 1.31       | 1.38      | 1.09 |
|          | Turns   | 3.44 | 0.73           | 0.29       | 1.35       | 1.41      | 1.24 |
|          |         |      |                |            |            |           |      |
| SPARTA   | All     | 2.70 | 0.56           | 0.27       | 1.06       | 1.15      | 1.10 |
|          | Helices | 2.18 | 0.51           | 0.21       | 1.01       | 0.88      | 1.04 |
|          | Strands | 2.80 | 0.53           | 0.33       | 1.01       | 1.37      | 1.18 |
|          | Coil    | 3.22 | 0.62           | 0.28       | 1.09       | 1.41      | 1.03 |
|          | Turns   | 3.19 | 0.63           | 0.30       | 1.13       | 1.17      | 1.18 |
|          |         |      |                |            |            |           |      |
| SHIFTX   | All     | 2.73 | 0.57           | 0.29       | 1.17       | 1.28      | 1.20 |
|          | Helices | 2.27 | 0.50           | 0.23       | 1.03       | 0.98      | 1.08 |
|          | Strands | 2.81 | 0.58           | 0.32       | 1.15       | 1.48      | 1.18 |
|          | Coil    | 3.18 | 0.58           | 0.27       | 1.19       | 1.51      | 1.25 |
|          | Turns   | 3.20 | 0.69           | 0.35       | 1.37       | 1.41      | 1.40 |

Table S5.

Comparison of the predictions of chemical shifts for the 7-protein test set detailed in Table S3 divided for secondary structure elements; units are in ppm. For comparison, we also report the overall results of the chemical shift values predicted by PROSHIFT<sup>6</sup> (<http://www.meilerlab.org/web/index.php>), which is another commonly used prediction method: 3.19 ppm (N), 0.60 ppm (H<sub>N</sub>), 0.33 ppm (H $\alpha$ ), 2.40 ppm (C $\alpha$ ), 2.62 ppm (C $\beta$ ) , 2.50 ppm (C').

## Constants for all amino acids

Category 1: Random coil values (in ppm)

| Amino acid | H $\alpha$ | C $\alpha$ | H $_N$ | N     | C'    | C $\beta$ | Ncorr <sup>1</sup> |
|------------|------------|------------|--------|-------|-------|-----------|--------------------|
| ALA        | 4.432847   | 52.26644   | 8.24   | 123.8 | 177.1 | 19        | -0.2               |
| ARG        | 4.35015    | 56.24026   | 8.23   | 120.5 | 176.5 | 30.3      | 1.45               |
| ASN        | 4.806587   | 53.30902   | 8.3    | 118.7 | 175.5 | 39        | 1.15               |
| ASP        | 4.725179   | 54.158222  | 8.34   | 120.4 | 177.2 | 40.8      | 1.18               |
| CYS        | 4.65       | 57.791772  | 8.32   | 118.6 | 175.1 | 41.8      | 2.43               |
| GLN        | 4.405826   | 56.062813  | 8.32   | 119.8 | 176.3 | 30.1      | 1.57               |
| GLU        | 4.364552   | 56.503798  | 8.42   | 120.2 | 176.1 | 29.7      | 1.8                |
| GLY        | 3.97       | 45.486533  | 8.33   | 108.8 | 173.6 | 0         | 1.07               |
| HIS        | 4.615947   | 55.660394  | 8.32   | 118.2 | 175.1 | 32        | 1.2                |
| ILE        | 4.193333   | 61.206185  | 8.05   | 119.9 | 176.8 | 37.5      | 4.14               |
| LEU        | 4.402746   | 54.957697  | 8.16   | 121.8 | 177.1 | 41.9      | 1.5                |
| LYS        | 4.36807    | 56.243301  | 8.29   | 120.4 | 176.5 | 32.3      | 1.55               |
| MET        | 4.461933   | 55.367     | 8.28   | 119.6 | 175.5 | 32.8      | 1.33               |
| PHE        | 4.430244   | 57.64624   | 8.3    | 120.3 | 175.8 | 39.3      | 1.25               |
| PRO        | 4.658447   | 63.066266  | 0      | 0     | 176   | 31.7      | 0.6                |
| SER        | 4.504638   | 58.144025  | 8.31   | 115.7 | 173.7 | 62.7      | 2.59               |
| THR        | 4.324869   | 62.54202   | 8.15   | 113.6 | 175.2 | 68.1      | 3.2                |
| TRP        | 4.412784   | 56.208648  | 8.15   | 121.3 | 175.8 | 28.3      | 1.64               |
| TYR        | 4.339301   | 57.33818   | 8.12   | 120.3 | 175.7 | 38.7      | 1.75               |
| VAL        | 4.086605   | 62.512466  | 8.03   | 119.2 | 177.1 | 31.7      | 3.83               |

<sup>1</sup>Correction applied to the chemical shifts of the nitrogen atom of residue i+1 if residue i is of the type listed in the first column

## Categories, functional forms, and parameters for all amino acids except GLY and PRO

|                                  |         | H $\alpha$                                                 | C $\alpha$ | H $_N$     | N          | C'         | C $\beta$  |
|----------------------------------|---------|------------------------------------------------------------|------------|------------|------------|------------|------------|
| Category 2: Backbone distances   |         | $f(d) = c \cdot d^\beta, \beta = 1$<br>c units: ppm/length |            |            |            |            |            |
| Atom                             | residue |                                                            |            |            |            |            |            |
| N                                | i-1     | 0.1049538                                                  | -0.5514491 | -0.7220064 | -0.9896088 | -0.0335257 | -0.2953833 |
| CA                               | i-1     | 0                                                          | -0.3171652 | 0.7184281  | 0          | -0.3228718 | -0.1623656 |
| HA                               | i-1     | 0.0867546                                                  | -2.2950958 | -1.2431488 | -3.3287317 | -0.3565204 | 0.4139583  |
| C                                | i-1     | 0                                                          | 5.0389158  | 0          | 10.747981  | 0          | -1.2077866 |
| O                                | i-1     | -0.3532599                                                 | -0.9486056 | 0          | -1.6351735 | -0.4007998 | 0.9900209  |
| N                                | i       | 0                                                          | 0          | 0          | -4.72E-10  | 0          | 3.6029795  |
| H                                | i       | -0.2327538                                                 | 3.9203989  | 1.40E-11   | -3.5391268 | -0.3422196 | -0.7672058 |
| CA                               | i       | 0                                                          | -1.95E-10  | 0          | -15.905456 | 0          | 0          |
| HA                               | i       | -5.37E-13                                                  | 7.88841    | 0.0647727  | -2.1882201 | 0          | 1.52206    |
| C                                | i       | 0                                                          | 6.2111825  | 0.356169   | 1.7859756  | -4.07E-11  | -5.7922812 |
| O                                | i       | 0.1744758                                                  | 3.6965816  | -0.5820469 | 4.2262422  | 0          | 1.2132408  |
| N                                | i+1     | 0                                                          | 0.8900045  | -0.4391426 | 1.0503018  | 0          | 1.1459425  |
| H                                | i+1     | 0.1487117                                                  | 1.0575798  | 0          | 4.1696025  | 0          | 0.9454372  |
| CA                               | i+1     | -0.0532967                                                 | 0.8431783  | 0.3153333  | -3.5151185 | -1.4947525 | -2.4331324 |
| HA                               | i+1     | 0.0388204                                                  | -0.0068419 | -0.0476424 | 0.7841273  | -0.1945234 | 0.1294023  |
| C                                | i+1     | 0.1117464                                                  | 0.5577506  | -0.0367456 | 0.0492691  | -0.8447972 | 0.1112132  |
| Category 3: Side-chain distances |         | $f(d) = c \cdot d^\beta, \beta = 1$<br>c units: ppm/length |            |            |            |            |            |
| Amino acid                       | Atom    |                                                            |            |            |            |            |            |



|     |      |            |            |            |            |            |            |
|-----|------|------------|------------|------------|------------|------------|------------|
| ALA | CB   | 0          | -3.4713212 | 0          | 0          | 0          | 1.06E-09   |
| ALA | 1HB  | 0          | 0          | 0          | 0          | 0          | 0          |
| ALA | 2HB  | 0          | 0          | 0          | 0          | 0          | 0          |
| ALA | 3HB  | 0          | 0          | 0          | 0          | 0          | 0          |
| ARG | CB   | 0          | 0          | 0          | 0          | 0          | -9.60E-12  |
| ARG | CG   | 0          | 1.1144674  | 0          | 0.8725275  | 0          | 0          |
| ARG | CD   | 0          | 0.8162443  | 0          | 0          | 0          | 0.2271032  |
| ARG | NE   | -0.0430368 | -2.8863841 | 0          | 0.0024325  | -0.2415749 | -2.3789452 |
| ARG | CZ   | 0          | 1.2386056  | 0          | 0          | 0          | -0.5131809 |
| ARG | NH1  | 0          | 0          | 0          | 0          | 0          | 0.688123   |
| ARG | NH2  | 0.0191117  | 0          | 0          | 0          | 0          | 0.688123   |
| ARG | 1HB  | 0.0714608  | -1.9456232 | 0.0085882  | -1.6105041 | 0.0172898  | 1.1794897  |
| ARG | 2HB  | 0.0714608  | -1.9456232 | 0.0085882  | -1.6105041 | 0.0172898  | 1.1794897  |
| ARG | 1HG  | -0.0239778 | -0.2422652 | -0.0352422 | -0.8101128 | 0.0405182  | -0.1239578 |
| ARG | 2HG  | -0.0239778 | -0.2422652 | -0.0352422 | -0.8101128 | 0.0405182  | -0.1239578 |
| ARG | 1HD  | -0.0087136 | 0.3207482  | 0.0121353  | -0.3670633 | -0.0337978 | -0.2067592 |
| ARG | 2HD  | -0.0087136 | 0.3207482  | 0.0121353  | -0.3670633 | -0.0337978 | -0.2067592 |
| ARG | HE   | -0.0095285 | 1.2349324  | -0.0173074 | -0.4236829 | 0.0948721  | 0.886851   |
| ARG | 1HH1 | 0          | 0          | 0          | 0          | 0          | 0          |
| ARG | 2HH1 | 0          | 0          | 0          | 0          | 0          | 0          |
| ARG | 1HH2 | 0          | 0          | 0          | 0          | 0          | 0          |
| ARG | 2HH2 | 0          | 0          | 0          | 0          | 0          | 0          |
| ASN | CB   | 0          | 0          | 0          | 0          | 0          | -4.15E-10  |
| ASN | CG   | -0.1831709 | -13.440288 | 0          | -2.0759051 | 0          | -2.2470142 |
| ASN | OD1  | -0.0327841 | 5.0124168  | -0.0625137 | -0.4411607 | -0.3516236 | 0          |
| ASN | ND2  | 0          | 4.1041014  | 0          | -0.0950434 | 0          | 1.7681132  |
| ASN | 1HB  | 0.100685   | 0.6762769  | 0.02455    | -1.2563696 | 0.138793   | 0          |
| ASN | 2HB  | 0.100685   | 0.6762769  | 0.02455    | -1.2563696 | 0.138793   | 0          |
| ASN | 1HD2 | 0          | 0          | 0          | 0          | 0          | 0          |
| ASN | 2HD2 | 0          | 0          | 0          | 0          | 0          | 0          |
| ASP | CB   | 0          | 6.5765072  | 0          | -3.8690467 | 0          | -2.41E-09  |
| ASP | CG   | 0          | -5.8322385 | -0.0110424 | 4.5435659  | 0          | 0.4223025  |
| ASP | OD1  | -0.1025933 | 1.641523   | -0.0778158 | -2.8572188 | -0.1968005 | -0.5720464 |
| ASP | OD2  | -0.0972178 | 1.6768363  | 0.0083144  | -2.6882814 | -0.1607423 | 0.7996824  |
| ASP | 1HB  | 0.1218923  | -1.778769  | 0.0294315  | -0.0839807 | 0.0088177  | 0          |
| ASP | 2HB  | 0.1218923  | -1.778769  | 0.0294315  | -0.0839807 | 0.0088177  | 0          |
| CYS | CB   | 0          | 0          | 0          | 0          | 0          | 1.10E-09   |
| CYS | SG   | 0          | 0          | -0.0071872 | -0.9895489 | -0.1222304 | 0          |
| CYS | 1HB  | 0          | 0          | -0.0085162 | -2.3032725 | -0.0245121 | 0          |
| CYS | 2HB  | 0          | 0          | -0.0085162 | -2.3032725 | -0.0245121 | 0          |
| CYS | HG   | 0          | 0          | 0          | 0          | 0          | -5.3074295 |
| GLN | CB   | 0          | 0          | 0          | -3.7525202 | 0          | -7.19E-12  |
| GLN | CG   | 0          | -0.4566143 | 0          | -4.0155098 | 0          | 17.326394  |
| GLN | CD   | 0          | 3.5883887  | 0          | 6.9017111  | 0          | -13.849589 |
| GLN | OE1  | -0.0259782 | -1.0240332 | -0.0870417 | -2.8876885 | 0.0138941  | 4.5666691  |
| GLN | NE2  | 0.0092093  | -1.0116499 | 0          | -2.0799035 | -0.0306656 | 3.9474494  |
| GLN | 1HB  | 0.0460137  | -2.1809066 | 0.0038255  | -0.538439  | -0.1263032 | 8.8285368  |
| GLN | 2HB  | 0.0460137  | -2.1809066 | 0.0038255  | -0.538439  | -0.1263032 | 8.8285368  |
| GLN | 1HG  | -0.0323311 | 0.7429182  | 0.0268177  | 0.4377085  | -0.0014186 | -8.8389784 |
| GLN | 2HG  | -0.0323311 | 0.7429182  | 0.0268177  | 0.4377085  | -0.0014186 | -8.8389784 |
| GLN | 1HE2 | 0          | 0          | 0          | 0          | 0          | 0          |
| GLN | 2HE2 | 0          | 0          | 0          | 0          | 0          | 0          |
| GLU | CB   | 0          | 0          | 0          | -0.3773162 | 0          | -6.36E-10  |
| GLU | CG   | 0          | -2.8934267 | 0          | -4.9704113 | 0          | 0          |
| GLU | CD   | 0          | 4.5000857  | 0          | 5.2939901  | 0          | -4.7840764 |
| GLU | OE1  | -0.0187235 | -1.3830948 | -0.1589678 | -2.1837438 | 0.0061113  | 1.3325745  |

|     |      |            |            |            |            |            |            |
|-----|------|------------|------------|------------|------------|------------|------------|
| GLU | OE2  | -0.0240431 | -1.3199339 | -0.1077505 | -1.8104882 | 0.1390527  | 1.1347852  |
| GLU | 1HB  | 0.0534452  | -1.2034429 | 0.1043308  | -1.1019617 | -0.0804855 | 0          |
| GLU | 2HB  | 0.0534452  | -1.2034429 | 0.1043308  | -1.1019617 | -0.0804855 | 0          |
| GLU | 1HG  | -0.0084319 | 1.0118245  | 0.0687767  | 0.4988155  | -0.0505778 | 1.2801966  |
| GLU | 2HG  | -0.0084319 | 1.0118245  | 0.0687767  | 0.4988155  | -0.0505778 | 1.2801966  |
| HIS | CB   | 0          | 1.8283033  | 0          | -16.929154 | 0          | -3.88E-10  |
| HIS | CG   | -0.1530754 | -2.6194459 | 0          | 2.4334007  | 0          | 0          |
| HIS | ND1  | 0          | -0.4199474 | 0          | -2.8866673 | 0          | 0          |
| HIS | CD2  | 0          | 0          | 0          | 0          | 0          | -3.6891183 |
| HIS | CE1  | 0          | 0          | 0          | 0          | 0          | 0          |
| HIS | NE2  | 0          | -4.9231018 | 0          | 0          | 0          | 0          |
| HIS | 1HB  | 0.0667815  | -4.5033366 | 0.0224923  | 2.8658186  | 0.0057744  | 0          |
| HIS | 2HB  | 0.0667815  | -4.5033366 | 0.0224923  | 2.8658186  | 0.0057744  | 0          |
| HIS | HD1  | 0          | 7.9189163  | -0.030249  | -0.7754716 | -0.0588564 | 2.6143485  |
| HIS | HD2  | 0          | 7.9189163  | -0.030249  | -0.7754716 | -0.0588564 | 2.6143485  |
| HIS | HE1  | 0          | -2.2028053 | -0.014255  | 3.2003381  | 0.0239427  | -1.5821813 |
| ILE | CB   | 0          | 0          | 0          | 0          | 0          | -1.13E-09  |
| ILE | CG1  | 0          | -1.6648856 | 0          | 0          | 0          | 28.041084  |
| ILE | CG2  | 0          | 0          | 0          | 0          | 0          | 0          |
| ILE | CD1  | 0          | 0          | 0          | 0          | 0          | 30.373639  |
| ILE | HB   | 0          | 1.2970047  | 0          | -4.7185183 | 0          | 22.654756  |
| ILE | 1HG1 | -0.0111565 | 0          | -0.0006385 | -0.5067059 | -0.1804216 | -33.38388  |
| ILE | 2HG1 | -0.0111565 | 0          | -0.0006385 | -0.5067059 | -0.1804216 | -33.38388  |
| ILE | 1HG2 | 0          | 0          | 0          | 0          | 0          | 0          |
| ILE | 2HG2 | 0          | 0          | 0          | 0          | 0          | 0          |
| ILE | 3HG2 | 0          | 0          | 0          | 0          | 0          | 0          |
| ILE | 1HD1 | 0          | 0          | 0          | 0          | 0          | 0          |
| ILE | 2HD1 | 0          | 0          | 0          | 0          | 0          | 0          |
| ILE | 3HD1 | 0          | 0          | 0          | 0          | 0          | 0          |
| LEU | CB   | 0          | 3.517946   | 0          | 0          | 0          | 1.72E-10   |
| LEU | CG   | 0          | 3.8861386  | -0.0712586 | -1.8316832 | 0          | 0          |
| LEU | CD1  | 0          | 0          | 0          | 0          | 0          | 0          |
| LEU | CD2  | 0          | 0          | 0          | 0          | 0          | 0          |
| LEU | 1HB  | 0.0024544  | -3.5176338 | 0.0203021  | -2.0087278 | -0.2383368 | 0          |
| LEU | 2HB  | 0.0024544  | -3.5176338 | 0.0203021  | -2.0087278 | -0.2383368 | 0          |
| LEU | HG   | 0          | -0.7096024 | 0.002288   | 0.0301227  | 0.1279977  | 0.5441892  |
| LEU | 1HD1 | 0          | 0          | 0          | 0          | 0          | 0          |
| LEU | 2HD1 | 0          | 0          | 0          | 0          | 0          | 0          |
| LEU | 3HD1 | 0          | 0          | 0          | 0          | 0          | 0          |
| LEU | 1HD2 | 0          | 0          | 0          | 0          | 0          | 0          |
| LEU | 2HD2 | 0          | 0          | 0          | 0          | 0          | 0          |
| LEU | 3HD2 | 0          | 0          | 0          | 0          | 0          | 0          |
| LYS | CB   | 0          | 0          | 0          | -6.3060844 | 0          | -3.19E-10  |
| LYS | CG   | 0          | -0.3613907 | 0          | 1.6582529  | 0          | -11.609509 |
| LYS | CD   | 0          | 1.4293193  | 0          | -0.5101093 | 0          | -0.1443795 |
| LYS | CE   | 0          | -2.1458839 | 0          | 0          | 0          | -0.7009138 |
| LYS | NZ   | 0          | 0.5528206  | 0          | 0          | -0.0459614 | 0.1855675  |
| LYS | 1HB  | 0.0464037  | -1.3608475 | -0.0065542 | 0.0779636  | -0.053668  | 0          |
| LYS | 2HB  | 0.0464037  | -1.3608475 | -0.0065542 | 0.0779636  | -0.053668  | 0          |
| LYS | 1HG  | -0.0259734 | 0.2360132  | -0.0174149 | -0.7856875 | 0.0015136  | 4.4708471  |
| LYS | 2HG  | -0.0259734 | 0.2360132  | -0.0174149 | -0.7856875 | 0.0015136  | 4.4708471  |
| LYS | 1HD  | -0.0118798 | -0.0534137 | 0.0076768  | 0.0678926  | 0.0212682  | -0.0182633 |
| LYS | 2HD  | -0.0118798 | -0.0534137 | 0.0076768  | 0.0678926  | 0.0212682  | -0.0182633 |
| LYS | 1HE  | 0.0022253  | 0.5994697  | -0.0125536 | -0.0203758 | -0.0098667 | 0.2455037  |
| LYS | 2HE  | 0.0022253  | 0.5994697  | -0.0125536 | -0.0203758 | -0.0098667 | 0.2455037  |
| LYS | 1HZ  | 0          | 0          | 0          | 0          | 0          | 0          |

|     |      |            |            |            |            |            |            |
|-----|------|------------|------------|------------|------------|------------|------------|
| LYS | 2HZ  | 0          | 0          | 0          | 0          | 0          | 0          |
| LYS | 3HZ  | 0          | 0          | 0          | 0          | 0          | 0          |
| MET | CB   | 0          | 0          | 0          | 0          | 0          | 1.68E-09   |
| MET | CG   | 0          | -0.6459234 | -0.6525533 | 0          | 0          | 0          |
| MET | SD   | -0.1636483 | 2.8351113  | 0.1364456  | 1.2823161  | -0.0427728 | -6.3588798 |
| MET | CE   | 0          | 0          | 0          | -0.5457662 | 0          | 0          |
| MET | 1HB  | 0.1377561  | -3.7815143 | 0.0148497  | -2.247036  | -0.045965  | 0          |
| MET | 2HB  | 0.1377561  | -3.7815143 | 0.0148497  | -2.247036  | -0.045965  | 0          |
| MET | 1HG  | -0.0084985 | 0.9431252  | 0.1833973  | -0.991317  | 0.079936   | 4.3040213  |
| MET | 2HG  | -0.0084985 | 0.9431252  | 0.1833973  | -0.991317  | 0.079936   | 4.3040213  |
| MET | 1HE  | 0          | 0          | 0          | 0          | 0          | 0          |
| MET | 2HE  | 0          | 0          | 0          | 0          | 0          | 0          |
| MET | 3HE  | 0          | 0          | 0          | 0          | 0          | 0          |
| PHE | CB   | 0          | 0          | -0.0108482 | -7.139512  | 1.6285523  | 7.67E-10   |
| PHE | CG   | 0          | 0          | 0          | 0          | 0          | 0          |
| PHE | CD1  | 0          | 0          | 0          | 0          | 0          | 0          |
| PHE | CD2  | 0          | 0          | 0          | 0          | 0          | 0          |
| PHE | CE1  | 0          | 0          | 0          | 0          | 0          | 0          |
| PHE | CE2  | 0          | 0          | 0          | 0          | 0          | 0          |
| PHE | CZ   | 0          | 0          | 0          | 0.9072064  | 0          | 0          |
| PHE | 1HB  | 0          | -0.3469764 | -0.032161  | -0.8021542 | -0.8248405 | 0          |
| PHE | 2HB  | 0          | -0.3469764 | -0.032161  | -0.8021542 | -0.8248405 | 0          |
| PHE | HD1  | 0          | 0          | 0          | 0          | 0          | 0          |
| PHE | HD2  | 0          | 0          | 0          | 0          | 0          | 0          |
| PHE | HE1  | 0          | 0          | 0          | 0          | 0          | 0          |
| PHE | HE2  | 0          | 0          | 0          | 0          | 0          | 0          |
| PHE | HZ   | 0          | 0          | 0          | 0          | 0          | 0          |
| SER | CB   | 0          | 1.7940727  | 0          | 0          | 0          | 4.04E-12   |
| SER | OG   | -0.1130518 | 0.7939235  | -0.5580253 | -8.0106234 | -3.3810222 | 0          |
| SER | 1HB  | 0.0652575  | -1.3559362 | -0.026532  | -1.3635124 | -0.07761   | -4.5539859 |
| SER | 2HB  | 0.0652575  | -1.3559362 | -0.026532  | -1.3635124 | -0.07761   | -4.5539859 |
| SER | HG   | -0.0087883 | 0          | 0.4586186  | 4.4828757  | 2.9825818  | 6.0879134  |
| THR | CB   | 0          | 0          | 0          | 8.1381237  | 0          | -7.14E-12  |
| THR | OG1  | -0.0535248 | -2.0076927 | 0.028154   | -4.6797542 | -0.6556241 | 1.2314574  |
| THR | CG2  | 0          | 2.80742    | 0          | 0          | 0          | 0          |
| THR | HB   | 0.0444565  | -1.8833967 | -0.0463287 | -6.9078573 | 0.4753306  | 0          |
| THR | HG1  | 0          | 0          | 0          | 0          | 0          | 0          |
| THR | 1HG2 | 0          | 0          | 0          | 0          | 0          | 0          |
| THR | 2HG2 | 0          | 0          | 0          | 0          | 0          | 0          |
| THR | 3HG2 | 0          | 0          | 0          | 0          | 0          | 0          |
| TRP | CB   | 0          | 0          | 0          | 0          | 0          | -1.64E-12  |
| TRP | CG   | 0          | 0          | 0          | 0          | 0          | 0          |
| TRP | CD1  | 0          | 0          | 0          | 0          | 0          | 0          |
| TRP | CD2  | 0          | 12.350985  | 0          | 0          | 0          | 0          |
| TRP | NE1  | 0          | 0          | 0          | 0          | 0          | 6.2259977  |
| TRP | CE2  | 0          | 0          | 0          | -7.9272257 | 0          | 0          |
| TRP | CE3  | 0          | 0          | 0          | 9.0887743  | 0          | 0          |
| TRP | CZ2  | 0          | 0          | 0          | -5.0425674 | 0          | -2.939783  |
| TRP | CZ3  | 0          | 0          | 0          | 0          | 0          | 0          |
| TRP | CH2  | 0          | 0          | 0          | 0          | 0          | 0          |
| TRP | 1HB  | 0.0092938  | -0.4214938 | 0.1033322  | -1.8068207 | -0.2268331 | 0          |
| TRP | 2HB  | 0.0092938  | -0.4214938 | 0.1033322  | -1.8068207 | -0.2268331 | 0          |
| TRP | HD1  | -0.2154728 | 12.502242  | -0.4010585 | -8.5114412 | 0.0953497  | 0.0297149  |
| TRP | HE1  | 0          | -11.943648 | 0.3700701  | 14.366154  | 0          | -5.3341363 |
| TRP | HE3  | -0.3873828 | 0          | -0.2975314 | -5.7956769 | 0          | -1.1800541 |
| TRP | HZ2  | 0          | -7.5751791 | 0          | 0          | 0          | 1.1527539  |

|     |      |           |            |            |            |            |            |
|-----|------|-----------|------------|------------|------------|------------|------------|
| TRP | HZ3  | 0         | 0          | 0          | 0          | 0          | 2.5990143  |
| TRP | HH2  | 0.3277147 | 3.8883626  | 0          | 0          | 0.0876171  | 0          |
| TYR | CB   | 0         | 0          | 0          | -10.697018 | 0          | 2.86E-13   |
| TYR | CG   | 0         | 2.9675601  | 0          | 5.0955463  | 0          | 0          |
| TYR | CD1  | 0         | 0          | 0          | 0          | 0          | 0          |
| TYR | CD2  | 0         | -1.6679126 | 0          | 0          | 0          | 0          |
| TYR | CE1  | 0         | 0          | 0          | 0          | 0          | 0          |
| TYR | CE2  | 0         | 0          | 0          | 0          | 0          | 0          |
| TYR | CZ   | 0         | 0          | 0          | 0          | 0          | 0          |
| TYR | OH   | 0.0158655 | -3.6715087 | 0          | -1.4610716 | 0          | -1.4619849 |
| TYR | 1HB  | 0         | 4.8082255  | -0.0116527 | 0.4579165  | -0.0937108 | -0.181595  |
| TYR | 2HB  | 0         | 4.8082255  | -0.0116527 | 0.4579165  | -0.0937108 | -0.181595  |
| TYR | HD1  | 0         | 0          | 0          | 0          | 0          | 0          |
| TYR | HD2  | 0         | 0          | 0          | 0          | 0          | 0          |
| TYR | HE1  | 0         | 0          | 0          | 0          | 0          | 0          |
| TYR | HE2  | 0         | 0          | 0          | 0          | 0          | 0          |
| TYR | HH   | 0         | 0          | 0          | 0          | 0          | 1.4251078  |
| VAL | CB   | 0         | 0          | 0          | -1.9792373 | 0          | -3.17E-12  |
| VAL | CG1  | 0         | 0          | 0          | 0          | 0          | 0.3495978  |
| VAL | CG2  | 0         | 0          | 0          | 0          | 0          | 0.3495978  |
| VAL | HB   | 0         | -0.752457  | -0.0188545 | -4.2789195 | -0.5444149 | 0          |
| VAL | 1HG1 | 0         | 0          | 0          | 0          | 0          | 0          |
| VAL | 2HG1 | 0         | 0          | 0          | 0          | 0          | 0          |
| VAL | 3HG1 | 0         | 0          | 0          | 0          | 0          | 0          |
| VAL | 1HG2 | 0         | 0          | 0          | 0          | 0          | 0          |
| VAL | 2HG2 | 0         | 0          | 0          | 0          | 0          | 0          |
| VAL | 3HG2 | 0         | 0          | 0          | 0          | 0          | 0          |

Category 4: Nonbonded I

$$f(d) = c d^{\beta}, \beta = -3$$

c units: ppm·length<sup>3</sup>

Atom

Sub category 4a: sp3 hybridized

|   |            |            |            |            |           |            |
|---|------------|------------|------------|------------|-----------|------------|
| C | -2.9677854 | -10.347271 | -5.3813248 | -70.57317  | 2.7653856 | -14.770212 |
| H | 0.6715652  | 3.4507071  | 1.4552245  | 34.697589  | 1.2320259 | 4.8983259  |
| N | -1.6214566 | -12.598247 | 2.5053915  | -88.714197 | 31.323841 | -14.856998 |
| O | 0.13518    | -3.566465  | 3.3033813  | 15.271538  | 31.172001 | -4.2014278 |
| S | 6.2758     | -101.81223 | -0.8774168 | 89.182573  | 0.4631502 | 25.322355  |

Sub category 4b: sp2 hybridized

|   |            |            |           |            |           |            |
|---|------------|------------|-----------|------------|-----------|------------|
| C | -0.2035104 | -9.754433  | -14.43259 | -43.345602 | -27.91772 | -1.6525552 |
| N | 1.2355083  | -9.6285342 | 17.498842 | 78.051259  | 40.257083 | 0.7468027  |
| O | 8.1829427  | -8.6495093 | 9.1407986 | 53.274593  | 24.047757 | -9.2063201 |

Category 5: Nonbonded II

$$f(d) = c d^{\beta}, \beta = 1$$

c units: ppm/length

Atom

Sub category 5a: sp3 hybridized

|   |            |           |            |            |            |            |
|---|------------|-----------|------------|------------|------------|------------|
| C | 0.0026981  | 0.0340218 | -0.006955  | -0.0305132 | -0.0149591 | 0.0439096  |
| H | -0.0035563 | -0.004969 | 0.0116062  | -0.1324914 | -0.0314517 | -0.0111027 |
| N | 0.0093801  | 0.0474206 | -0.0631763 | 0.3450078  | -0.0069307 | 0.0436933  |
| O | 0.0013892  | 0.0041549 | 0.0012358  | 0.085475   | -0.0624505 | -0.0125857 |
| S | -0.0326842 | 0.359245  | 0.0129472  | -0.3312136 | -0.0197605 | -0.0796109 |

Sub category 5b: sp2 hybridized

|   |            |           |            |           |            |            |
|---|------------|-----------|------------|-----------|------------|------------|
| C | -0.0060841 | 0.0254618 | 0.03526    | 0.0402185 | 0.0658226  | 0.0122074  |
| N | -0.0204519 | 0.0257897 | -0.0491208 | -0.255377 | -0.0809803 | -0.0353783 |
| O | -0.0380543 | 0.0448192 | -0.0283907 | -0.184789 | -0.1061224 | 0.0308797  |

Category 6: Aromatic rings

$$f(\theta, r) = c (1 - 3 \cos^2(\theta))/r^3, \text{ for parameters } \theta \text{ and } r \text{ see Fig. S2}$$

c units: ppm·length<sup>3</sup>

Ring type

|     |           |           |           |            |           |           |
|-----|-----------|-----------|-----------|------------|-----------|-----------|
| PHE | 0.0197106 | 0.0107214 | 0.0248126 | -0.0121893 | 0.0379475 | 0.0228755 |
|-----|-----------|-----------|-----------|------------|-----------|-----------|

|      |           |           |           |            |           |           |
|------|-----------|-----------|-----------|------------|-----------|-----------|
| TYR  | 0.0187376 | 0.0066462 | 0.0190884 | -0.0325441 | 0.0321684 | 0.0220022 |
| TRP2 | 0.0112872 | 0.0250235 | 0.0199792 | -0.0196035 | 0.0024794 | 0.0273681 |
| TRP1 | 0.0202472 | 0.0060401 | 0.0255547 | -0.0134924 | 0.0344568 | 0.0192496 |
| HIS  | 0.011913  | 0.0036752 | 0.0130313 | -0.0110219 | 0.0176256 | 0.0131036 |

Category 7: Dihedral angles

$f(\theta) = c(p_1 \cos(3(\theta + p_4)) + p_2 \cos(\theta + p_5) + p_3)$ , where  $\theta \in \{\phi, \varphi, \chi_1\}$ . For parameters  $p_1$  through  $p_5$  see Table S2  
c units: ppm; p units: dimensionless

Angle

|           |            |           |            |           |            |           |
|-----------|------------|-----------|------------|-----------|------------|-----------|
| $\phi$    | 0.3960648  | 0.4778015 | 0.1404857  | 0.1306177 | -0.0663646 | 0.637021  |
| $\varphi$ | 0.176954   | 0.3692802 | 0.2091438  | 0.1913853 | 0.0596866  | 0.7236717 |
| $\chi_1$  | -0.0277769 | 0.1878352 | -0.2363657 | 0.2126343 | 0.2778522  | 0.1438652 |

Category 8: Hydrogen bonds

$f(\theta) = c E(\theta)$ , where  $\theta \in \{d, \gamma_1, \gamma_2\}$ . For the function  $E(x)$  see Eq. S1 and Table S1.  
c units: ppm

| Origin | residue | Parameter  |            |            |            |            |            |            |  |
|--------|---------|------------|------------|------------|------------|------------|------------|------------|--|
| O      | i-1     | d          | -2.82E-08  | -5.15E-06  | -1.00E-07  | -7.527E-05 | 8.48E-06   | 3.302E-05  |  |
| O      | i-1     | $\gamma_1$ | -0.0005796 | 0.0014532  | -0.0012312 | -0.0180411 | 0.0039887  | -0.0016318 |  |
| O      | i-1     | $\gamma_2$ | 6.866E-05  | -0.0001394 | 0.0001251  | 0.0018755  | -0.0003917 | 0.0001679  |  |
| H      | i       | d          | -0.001389  | 0.0030283  | -0.0142872 | -0.0134281 | -0.0043336 | -0.006617  |  |
| H      | i       | $\gamma_1$ | 0.0001071  | 0.0010661  | 0.0044821  | 0.0003982  | -0.0004837 | 0.0007823  |  |
| H      | i       | $\gamma_2$ | -5.55E-07  | -0.0001326 | -0.0005106 | -0.0001003 | 5.464E-05  | -3.278E-05 |  |
| O      | i       | d          | 1.14E-06   | -2.569E-05 | -5.47E-06  | -8.44E-05  | -1.693E-05 | -1.792E-05 |  |
| O      | i       | $\gamma_1$ | 0.0003084  | -0.0002918 | 0.0002329  | 0.0065627  | -0.011352  | 0.001168   |  |
| O      | i       | $\gamma_2$ | -2.808E-05 | 3.277E-05  | -1.567E-05 | -0.0006374 | 0.0011653  | -0.0001242 |  |
| H      | i+1     | d          | -0.0017769 | -0.0052441 | 0.0011321  | -0.0155729 | -0.007736  | 0.001717   |  |
| H      | i+1     | $\gamma_1$ | 0.0008555  | 0.0034481  | 0.000172   | 0.0117728  | 0.005713   | -0.0008433 |  |
| H      | i+1     | $\gamma_2$ | -8.147E-05 | -0.0003803 | -9.97E-06  | -0.0012193 | -0.0005443 | 0.0001076  |  |

Category 9: Extra distances

$f(d) = c d^\beta$ ,  $\beta = 1$   
c units: ppm/length

| Atom 1 | res 1 | atom 2 | res 2 |            |            |            |            |            |            |
|--------|-------|--------|-------|------------|------------|------------|------------|------------|------------|
| H      | i     | HA     | i     | -0.2327538 | -0.7434611 | 0.0647727  | 15.413797  | 2.1192318  | -1.4816841 |
| H      | i     | C      | i     | 0.4706843  | -2.9678515 | 0.356169   | -0.5081131 | -0.3422196 | 1.2693928  |
| H      | i     | CB     | i     | 0.1105158  | 0.2527171  | 0.4513892  | 4.0841294  | -0.5979143 | -0.7672058 |
| C      | i-1   | HA     | i     | -0.245715  | -0.5493254 | -0.1247354 | 5.3175934  | 1.4109851  | 0.3143816  |
| C      | i-1   | C      | i     | 0.6633011  | -4.4043652 | -0.7657828 | -7.0572238 | -1.8892012 | 1.6552051  |
| C      | i-1   | CB     | i     | 0.1545141  | -0.6886219 | -0.1308588 | -0.3235057 | 0.6930224  | -1.2077866 |
| O      | i     | HA     | i     | 0.1744758  | -7.050432  | 0.1035089  | -2.3941224 | -1.3898243 | 0.3139368  |
| O      | i     | N      | i     | -0.4090631 | 2.5129779  | 0.6346263  | 4.2262422  | 1.715943   | -0.3510702 |
| O      | i     | CB     | i     | 0.0299336  | 0.5613173  | 0.0991565  | 1.1221295  | 0.1724717  | 1.2132408  |
| N      | i+1   | HA     | i     | 0.0455486  | -6.196119  | 0.1243992  | -5.4083632 | -0.2092066 | 0.6083014  |
| N      | i+1   | N      | i     | -0.2246819 | 0.5916958  | -0.0851907 | 1.0503018  | 1.2968193  | -2.2086765 |
| N      | i+1   | CB     | i     | -0.0349463 | 0.0887913  | -0.0992274 | -1.2712689 | -0.0724524 | 1.1459425  |
| O      | i-1   | HA     | i-1   | -0.1545062 | 0.9721613  | -0.4524309 | -1.1365341 | -0.5756206 | -0.5649802 |
| O      | i-1   | N      | i-1   | -0.2047421 | -0.0910651 | -0.4601405 | -1.2419222 | 0.2337042  | -0.2127165 |
| O      | i-1   | CB     | i-1   | -0.0351304 | 0.0416089  | 0.0069608  | -2.3622365 | 0.205132   | 0.0623775  |
| N      | i     | HA     | i-1   | -0.1740476 | 3.0052241  | 1.3906446  | -3.3287317 | 0.0626519  | -1.2720737 |
| N      | i     | N      | i-1   | -0.1117979 | 0.4661329  | 0.8949212  | -0.9896088 | 0.3919709  | 0.3149075  |
| N      | i     | CB     | i-1   | 0.0189609  | 0.0051997  | -0.0271163 | 2.1847223  | -0.1618808 | -0.104322  |
| CG     | i     | HA     | i     | 0.1288138  | -0.8250044 | 0.027143   | 0.6921567  | 0.0426615  | -0.3198625 |
| CG     | i     | N      | i     | -0.0763197 | -0.0433575 | 0.1319916  | 2.8791465  | -0.1113439 | 0.2268996  |
| CG     | i     | C      | i     | -0.1053257 | 0.0469574  | -0.0870101 | 1.8044619  | 0.0823026  | -0.1846964 |
| CG     | i     | C      | i-1   | 0.0026591  | -0.0793623 | -0.0520901 | 0.362815   | 0.0017187  | -0.0785277 |
| CG     | i     | N      | i+1   | 0.0421798  | -0.1619192 | 0.0506248  | -0.2754379 | 0.0777308  | 0.0512366  |
| CG     | i-1   | CA     | i     | 0.0042209  | -0.0016555 | 0.0111822  | -0.1476944 | -0.0103181 | 0.0103673  |
| CG     | i+1   | CA     | i     | 0.0009935  | 0.0177661  | -0.0039802 | 0.0286774  | -0.0373196 | 0.0036293  |
| CA     | i-1   | CA     | i+1   | -0.0904907 | 0.6891161  | -0.0285188 | -1.2469408 | 0.5263286  | 1.0992811  |

Category 10: Disulfide bond CYS

$f(d) = c d^\beta$ ,  $\beta = 1$   
c units: ppm/length

Atom 1      res 1      atom 2

S i S x 0.0115552 -2.8517004 -0.1060554 -1.4131442 -0.3708814 11.361261

### Additional parameters for GLY

|                                  |         | H $\alpha$                                                                                                         | C $\alpha$ | H $_N$     | N          | C'         | C $\beta$ |
|----------------------------------|---------|--------------------------------------------------------------------------------------------------------------------|------------|------------|------------|------------|-----------|
| Category 2: Backbone distances   |         | $f(d) = c d^\beta, \beta = 1$<br>c units: ppm/length                                                               |            |            |            |            |           |
| Atom                             | residue |                                                                                                                    |            |            |            |            |           |
| N                                | i-1     | 0.0663175                                                                                                          | -0.4879558 | -0.679174  | -0.7475809 | -0.0373979 | 0         |
| CA                               | i-1     | 0                                                                                                                  | -0.5317572 | 0.7014888  | 0          | -0.9441592 | 0         |
| HA                               | i-1     | 0.0805372                                                                                                          | -1.7137742 | -1.0601918 | -3.7811287 | -0.3017085 | 0         |
| C                                | i-1     | 0                                                                                                                  | 3.8804893  | 0          | 11.661072  | 0          | 0         |
| O                                | i-1     | -0.3009441                                                                                                         | -1.0573319 | 0          | -2.1254723 | -0.0635957 | 0         |
| N                                | i       | 0                                                                                                                  | 0          | 0          | -4.02E-10  | 0          | 0         |
| H                                | i       | -0.1629661                                                                                                         | 2.8169776  | 3.68E-11   | 15.246462  | 0.3813989  | 0         |
| CA                               | i       | 0                                                                                                                  | 1.91E-10   | 0          | -18.048166 | 0          | 0         |
| HA                               | i       | 3.39E-12                                                                                                           | 6.6313875  | 0.0135944  | 8.3760367  | 0          | 0         |
| C                                | i       | 0                                                                                                                  | 6.7846053  | 0.5119419  | 12.00611   | 9.83E-13   | 0         |
| O                                | i       | 0.0989333                                                                                                          | 3.9973166  | -0.95712   | 3.4703765  | 0          | 0         |
| N                                | i+1     | 0                                                                                                                  | -1.5019093 | -0.9095434 | 1.1213514  | 0          | 0         |
| H                                | i+1     | 0.1331114                                                                                                          | 0.7995692  | 0          | 3.9804866  | 0          | 0         |
| CA                               | i+1     | 0.0646256                                                                                                          | 1.0488699  | 0.447443   | -2.8770606 | -1.215509  | 0         |
| HA                               | i+1     | 0.0221346                                                                                                          | -0.0029701 | -0.0566733 | 0.6644562  | -0.2252219 | 0         |
| C                                | i+1     | 0.1054101                                                                                                          | 0.5482872  | -0.0732623 | -0.070327  | -0.9356821 | 0         |
| Category 3: Side chain distances |         | $f(d) = c d^\beta, \beta = 1$<br>c units: ppm/length                                                               |            |            |            |            |           |
| Amino acid                       | Atom    |                                                                                                                    |            |            |            |            |           |
| GLY                              | 2HA     | 0.059929                                                                                                           | -3.5303299 | 0.030421   | 1.3803243  | 0.4653395  | 0         |
| Category 4: Nonbonded I          |         | $f(d) = c d^\beta, \beta = -3$<br>c units: ppm-length <sup>3</sup>                                                 |            |            |            |            |           |
| Atom                             |         |                                                                                                                    |            |            |            |            |           |
| Sub category 4a: sp3 hybridized  |         |                                                                                                                    |            |            |            |            |           |
| C                                |         | -3.0168132                                                                                                         | -8.5977612 | -5.8425338 | -71.591195 | 2.8434093  | 0         |
| H                                |         | 0.6934661                                                                                                          | 3.4918232  | 1.4585048  | 34.950005  | 1.1159714  | 0         |
| N                                |         | -1.5118058                                                                                                         | -11.682521 | 1.0705717  | -84.79476  | 31.208091  | 0         |
| O                                |         | -0.0116203                                                                                                         | -2.7975315 | 2.986752   | 15.415656  | 33.073499  | 0         |
| S                                |         | 6.0126235                                                                                                          | -90.045535 | -0.9345985 | 92.216868  | 2.2352785  | 0         |
| Sub category 4b: sp2 hybridized  |         |                                                                                                                    |            |            |            |            |           |
| C                                |         | 0.0261763                                                                                                          | -4.6399331 | -12.228723 | -35.763162 | -23.299868 | 0         |
| N                                |         | 1.7596832                                                                                                          | -24.154797 | 17.096711  | 93.833337  | 45.921117  | 0         |
| O                                |         | 7.515325                                                                                                           | -8.1137498 | 8.5922145  | 52.818653  | 24.239118  | 0         |
| Category 5: Nonbonded II         |         | $f(d) = c d^\beta, \beta = 1$<br>c units: ppm/length                                                               |            |            |            |            |           |
| Atom                             |         |                                                                                                                    |            |            |            |            |           |
| Sub category 5a: sp3 hybridized  |         |                                                                                                                    |            |            |            |            |           |
| C                                |         | 0.0019265                                                                                                          | 0.0309129  | -0.0054204 | -0.0207984 | -0.0151925 | 0         |
| H                                |         | -0.0031884                                                                                                         | -0.0067515 | 0.0121696  | -0.1312018 | -0.0307875 | 0         |
| N                                |         | 0.0084885                                                                                                          | 0.0471441  | -0.0599493 | 0.3297395  | -0.0085599 | 0         |
| O                                |         | 0.0018812                                                                                                          | -0.0014212 | 0.0013845  | 0.0865619  | -0.0690416 | 0         |
| S                                |         | -0.032383                                                                                                          | 0.3254299  | 0.0090494  | -0.3311426 | -0.0239321 | 0         |
| Sub category 5b: sp2 hybridized  |         |                                                                                                                    |            |            |            |            |           |
| C                                |         | -0.0072228                                                                                                         | 0.0120399  | 0.0281911  | 0.0224532  | 0.052758   | 0         |
| N                                |         | -0.0251185                                                                                                         | 0.0727875  | -0.0591581 | -0.3550119 | -0.0906942 | 0         |
| O                                |         | -0.0346209                                                                                                         | 0.0412071  | -0.0269135 | -0.1633652 | -0.1020419 | 0         |
| Category 6: Aromatic rings       |         | $f(\theta, r) = c (1 - 3 \cos^2(\theta))/r^3$ , for parameters $\theta$ and $r$ see Fig. S2<br>c units: ppm/length |            |            |            |            |           |
| Ring type                        |         |                                                                                                                    |            |            |            |            |           |

|                             |                                                                                                                                                                                                                    |            |           |            |            |            |            |            |   |
|-----------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------|-----------|------------|------------|------------|------------|------------|---|
| PHE                         |                                                                                                                                                                                                                    |            |           | 0.0187097  | 0.0109849  | 0.0235628  | -0.0095191 | 0.0367113  | 0 |
| TYR                         |                                                                                                                                                                                                                    |            |           | 0.0190572  | 0.006835   | 0.0152577  | -0.034505  | 0.0291119  | 0 |
| TRP2                        |                                                                                                                                                                                                                    |            |           | 0.0116558  | 0.0225183  | 0.0224577  | -0.020596  | 0.0041195  | 0 |
| TRP1                        |                                                                                                                                                                                                                    |            |           | 0.0198815  | 0.0079561  | 0.0213769  | -0.0133618 | 0.0330346  | 0 |
| HIS                         |                                                                                                                                                                                                                    |            |           | 0.0116936  | 0.002803   | 0.0128327  | -0.0118153 | 0.0169792  | 0 |
| Category 7: Dihedral angles | $f(\theta) = c(p_1 \cos(3(\theta + p_4)) + p_2 \cos(\theta + p_5) + p_3)$ , where $\theta \in \{\phi, \varphi, \chi_1\}$ . For parameters $p_1$ through $p_5$ see Table S2<br>c units: ppm; p units: dimensionless |            |           |            |            |            |            |            |   |
| Angle                       |                                                                                                                                                                                                                    |            |           |            |            |            |            |            |   |
| $\phi$                      |                                                                                                                                                                                                                    |            |           | 0.4864764  | 0.4169099  | 0.2348974  | 0.2576444  | 0.1099509  | 0 |
| $\varphi$                   |                                                                                                                                                                                                                    |            |           | 0.2353466  | 0.2842276  | -0.0211099 | 0.1762757  | 0.1410861  | 0 |
| $\chi_1$                    |                                                                                                                                                                                                                    |            |           | 0.0417891  | 0.092503   | -0.2358528 | 0.1582806  | 0.4117375  | 0 |
| Category 8: Hydrogen bonds  | $f(\theta) = c E(\theta)$ , where $\theta \in \{d, \gamma_1, \gamma_2\}$ . For function E(x) see Eq. S1 and Table S1<br>c units: ppm                                                                               |            |           |            |            |            |            |            |   |
| Origin                      | residue                                                                                                                                                                                                            | parameter  |           |            |            |            |            |            |   |
| O                           | i-1                                                                                                                                                                                                                | d          |           | -2.91E-07  | -7.02E-06  | -7.27E-07  | -8.416E-05 | 9.89E-06   | 0 |
| O                           | i-1                                                                                                                                                                                                                | $\gamma_1$ |           | -0.000418  | 0.0006044  | -0.0012924 | -0.0165728 | 0.0046344  | 0 |
| O                           | i-1                                                                                                                                                                                                                | $\gamma_2$ |           | 5.246E-05  | -4.566E-05 | 0.0001313  | 0.0017067  | -0.0004593 | 0 |
| H                           | i                                                                                                                                                                                                                  | d          |           | -0.001257  | 0.0030459  | -0.0148477 | -0.0126117 | -0.0049753 | 0 |
| H                           | i                                                                                                                                                                                                                  | $\gamma_1$ |           | 0.0001398  | 0.0013573  | 0.0051242  | 0.0018565  | -0.0006142 | 0 |
| H                           | i                                                                                                                                                                                                                  | $\gamma_2$ |           | -4.26E-06  | -0.0001636 | -0.0005739 | -0.0002636 | 6.704E-05  | 0 |
| O                           | i                                                                                                                                                                                                                  | d          |           | 1.47E-06   | -2.472E-05 | -6.01E-06  | -7.949E-05 | -1.65E-05  | 0 |
| O                           | i                                                                                                                                                                                                                  | $\gamma_1$ |           | 0.0001921  | -0.0002637 | 2.224E-05  | 0.0055339  | -0.0107069 | 0 |
| O                           | i                                                                                                                                                                                                                  | $\gamma_2$ |           | -1.612E-05 | 3.028E-05  | 6.29E-06   | -0.0005244 | 0.0010978  | 0 |
| H                           | i+1                                                                                                                                                                                                                | d          |           | -0.0018399 | -0.0050053 | 0.0009498  | -0.0132878 | -0.0099268 | 0 |
| H                           | i+1                                                                                                                                                                                                                | $\gamma_1$ |           | 0.0009027  | 0.00308    | 9.249E-05  | 0.0128629  | 0.0060278  | 0 |
| H                           | i+1                                                                                                                                                                                                                | $\gamma_2$ |           | -8.296E-05 | -0.0003454 | -8.88E-07  | -0.0013345 | -0.0005737 | 0 |
| Category 9: Extra distances | $f(d) = c d^\beta$ , $\beta = 1$<br>c units: ppm/length                                                                                                                                                            |            |           |            |            |            |            |            |   |
| Atom 1                      | residue 1                                                                                                                                                                                                          | atom 2     | residue 2 |            |            |            |            |            |   |
| H                           | i                                                                                                                                                                                                                  | HA         | i         | -0.1629661 | -0.1483798 | 0.0135944  | 8.766847   | 2.1013204  | 0 |
| H                           | i                                                                                                                                                                                                                  | C          | i         | 0.4122232  | -4.2093755 | 0.5119419  | -6.7520934 | 0.3813989  | 0 |
| H                           | i                                                                                                                                                                                                                  | CB         | i         | 0          | 0          | 0          | 0          | 0          | 0 |
| C                           | i-1                                                                                                                                                                                                                | HA         | i         | -0.0651481 | 0.2987554  | 0.0891024  | 5.6900611  | 0.7835696  | 0 |
| C                           | i-1                                                                                                                                                                                                                | C          | i         | 0.5298099  | -4.9560248 | -0.9512783 | -8.4671022 | -0.8618283 | 0 |
| C                           | i-1                                                                                                                                                                                                                | CB         | i         | 0          | 0          | 0          | 0          | 0          | 0 |
| O                           | i                                                                                                                                                                                                                  | HA         | i         | 0.0989333  | -7.3344972 | 0.0778165  | -4.6575886 | -0.8408604 | 0 |
| O                           | i                                                                                                                                                                                                                  | N          | i         | -0.337499  | 3.5153174  | 1.0217624  | 3.4703765  | 0.6362337  | 0 |
| O                           | i                                                                                                                                                                                                                  | CB         | i         | 0          | 0          | 0          | 0          | 0          | 0 |
| N                           | i+1                                                                                                                                                                                                                | HA         | i         | -0.0386912 | -5.2279072 | 0.0624355  | -5.4231033 | -0.1365515 | 0 |
| N                           | i+1                                                                                                                                                                                                                | N          | i         | -0.0449491 | 2.1436293  | 0.4497398  | 1.1213514  | -0.0124586 | 0 |
| N                           | i+1                                                                                                                                                                                                                | CB         | i         | 0          | 0          | 0          | 0          | 0          | 0 |
| O                           | i-1                                                                                                                                                                                                                | HA         | i-1       | -0.1476902 | 1.2056681  | -0.340777  | -2.517914  | -0.363172  | 0 |
| O                           | i-1                                                                                                                                                                                                                | N          | i-1       | -0.1780503 | -0.1273927 | -0.4324141 | -1.1224459 | 0.2225914  | 0 |
| O                           | i-1                                                                                                                                                                                                                | CB         | i-1       | -0.0321439 | -0.0121417 | 0.0164976  | -2.2819998 | 0.1328632  | 0 |
| N                           | i                                                                                                                                                                                                                  | HA         | i-1       | -0.1467708 | 2.8171414  | 1.1421495  | -3.7811287 | 0.279518   | 0 |
| N                           | i                                                                                                                                                                                                                  | N          | i-1       | -0.0704203 | 0.4414006  | 0.8694495  | -0.7475809 | 0.4309026  | 0 |
| N                           | i                                                                                                                                                                                                                  | CB         | i-1       | 0.0173538  | 0.0600871  | -0.0325651 | 2.1044602  | -0.0954739 | 0 |
| CG                          | i                                                                                                                                                                                                                  | HA         | i         | 0.1217622  | -0.9510271 | 0.028993   | 0.3537814  | 0.109656   | 0 |
| CG                          | i                                                                                                                                                                                                                  | N          | i         | -0.096412  | -0.011697  | 0.2195154  | 2.1215038  | -0.1739345 | 0 |
| CG                          | i                                                                                                                                                                                                                  | C          | i         | -0.0905658 | 0.0338832  | -0.0730184 | 1.9813139  | 0.1401974  | 0 |
| CG                          | i                                                                                                                                                                                                                  | C          | i-1       | 0.0240178  | 0.0879133  | -0.1232099 | 1.0299104  | 0.052646   | 0 |
| CG                          | i                                                                                                                                                                                                                  | N          | i+1       | 0.0367706  | -0.0177007 | 0.0122126  | -0.5722059 | -0.0112693 | 0 |
| CG                          | i-1                                                                                                                                                                                                                | CA         | i         | 0.0040347  | -0.0018201 | 0.0107078  | -0.1536396 | -0.0100844 | 0 |
| CG                          | i+1                                                                                                                                                                                                                | CA         | i         | 0.0013451  | 0.0164845  | -0.0026209 | 0.0327525  | -0.0375762 | 0 |
| CA                          | i-1                                                                                                                                                                                                                | CA         | i+1       | -0.1203359 | 0.6912473  | -0.0638527 | -1.0492797 | 0.6711163  | 0 |

### Additional parameters for PRO

|                                  |         | H $\alpha$                                                           | C $\alpha$  | H <sub>N</sub> | N | C'           | C $\beta$  |
|----------------------------------|---------|----------------------------------------------------------------------|-------------|----------------|---|--------------|------------|
| Category 2: Backbone distances   |         | $f(d) = c d^{\beta}, \beta = 1$<br>c units: ppm/length               |             |                |   |              |            |
| Atom                             | residue |                                                                      |             |                |   |              |            |
| N                                | i-1     | 0.0297782                                                            | -0.3084801  |                | 0 | 0 0.0570203  | -0.2483017 |
| CA                               | i-1     |                                                                      | 0 0.8047905 |                | 0 | 0 0.4554952  | -1.6760849 |
| HA                               | i-1     | -0.0194261                                                           | -2.0300362  |                | 0 | 0 -0.3650702 | 0.2375751  |
| C                                | i-1     |                                                                      | 0 1.3222739 |                | 0 | 0 0          | -0.4814236 |
| O                                | i-1     | -0.2139526                                                           | -0.7680869  |                | 0 | 0 0.0210265  | 1.1264962  |
| N                                | i       |                                                                      | 0 0         |                | 0 | 0 0          | 1.6972503  |
| H                                | i       |                                                                      | 0 0         |                | 0 | 0 0          | 0          |
| CA                               | i       |                                                                      | 0 8.85E-11  |                | 0 | 0 0          | 0          |
| HA                               | i       | -1.88E-12                                                            | 7.724755    |                | 0 | 0 0          | 1.1828645  |
| C                                | i       |                                                                      | 0 1.7933113 |                | 0 | 0 -2.16E-11  | -4.7655492 |
| O                                | i       | 0.0466054                                                            | 7.9039908   |                | 0 | 0 0          | 0.9695745  |
| N                                | i+1     |                                                                      | 0 3.9079032 |                | 0 | 0 0          | 0.4914757  |
| H                                | i+1     | 0.2079951                                                            | 1.1819019   |                | 0 | 0 0          | 1.2655731  |
| CA                               | i+1     | 0.0271823                                                            | 0.7888304   |                | 0 | 0 -1.1011533 | -2.2653164 |
| HA                               | i+1     | 0.0331915                                                            | 0.0588155   |                | 0 | 0 -0.1836946 | 0.1337957  |
| C                                | i+1     | 0.1143958                                                            | 0.5778967   |                | 0 | 0 -0.860993  | 0.0970634  |
| Category 3: Side chain distances |         | $f(d) = c d^{\beta}, \beta = 1$<br>c units: ppm/length               |             |                |   |              |            |
| Amino acid                       | Atom    |                                                                      |             |                |   |              |            |
| PRO                              | CB      | 0.7663159                                                            | -6.674831   |                | 0 | 0 -6.5330139 | -1.16E-09  |
| PRO                              | CG      | -1.0693319                                                           | -4.4517713  |                | 0 | 0 -9.0566327 | 37.196099  |
| PRO                              | CD      | 0.5137461                                                            | -1.5048913  |                | 0 | 0 -3.7791219 | 3.9716195  |
| PRO                              | 1HB     | -0.7856916                                                           | 0.1989625   |                | 0 | 0 2.3072704  | 21.034246  |
| PRO                              | 2HB     | -0.7856916                                                           | 0.1989625   |                | 0 | 0 2.3072704  | 21.034246  |
| PRO                              | 1HG     | 0.644203                                                             | 2.0322733   |                | 0 | 0 3.8140635  | -21.435762 |
| PRO                              | 2HG     | 0.644203                                                             | 2.0322733   |                | 0 | 0 3.8140635  | -21.435762 |
| PRO                              | 1HD     | -0.1377958                                                           | 1.5457336   |                | 0 | 0 2.0392284  | -2.8604453 |
| PRO                              | 2HD     | -0.1377958                                                           | 1.5457336   |                | 0 | 0 2.0392284  | -2.8604453 |
| Category 4: Nonbonded I          |         | $f(d) = c d^{\beta}, \beta = -3$<br>c units: ppm·length <sup>3</sup> |             |                |   |              |            |
| Atom                             |         |                                                                      |             |                |   |              |            |
| Sub category 4a: sp3 hybridized  |         |                                                                      |             |                |   |              |            |
| C                                |         | -2.8890318                                                           | -11.570118  |                | 0 | 0 0.7454209  | -15.431234 |
| H                                |         | 0.678145                                                             | 3.8625409   |                | 0 | 0 1.5414621  | 4.9580328  |
| N                                |         | -1.6775879                                                           | -14.305472  |                | 0 | 0 30.44214   | -13.276479 |
| O                                |         | 0.1396715                                                            | -3.2341673  |                | 0 | 0 31.004812  | -3.7642266 |
| S                                |         | 6.1752519                                                            | -97.777556  |                | 0 | 0 -0.1268803 | 23.362399  |
| Sub category 4b: sp2 hybridized  |         |                                                                      |             |                |   |              |            |
| C                                |         | -0.0160994                                                           | -10.477399  |                | 0 | 0 -29.372628 | -1.8666475 |
| N                                |         | 1.0437019                                                            | -5.6041119  |                | 0 | 0 29.917336  | -4.3766057 |
| O                                |         | 8.0417551                                                            | -8.575915   |                | 0 | 0 24.741825  | -8.6247771 |
| Category 5: Nonbonded II         |         | $f(d) = c d^{\beta}, \beta = 1$<br>c units: ppm/length               |             |                |   |              |            |
| Atom                             |         |                                                                      |             |                |   |              |            |
| Sub category 5a: sp3 hybridized  |         |                                                                      |             |                |   |              |            |
| C                                |         | 0.0023439                                                            | 0.0353139   |                | 0 | 0 -0.0095636 | 0.0451183  |
| H                                |         | -0.0037569                                                           | -0.0063923  |                | 0 | 0 -0.0329768 | -0.0118314 |
| N                                |         | 0.0097003                                                            | 0.053891    |                | 0 | 0 -0.0036915 | 0.037665   |
| O                                |         | 0.0009191                                                            | 0.0031997   |                | 0 | 0 -0.0619811 | -0.0114114 |
| S                                |         | -0.0327975                                                           | 0.348281    |                | 0 | 0 -0.0211074 | -0.0725498 |
| Sub category 5b: sp2 hybridized  |         |                                                                      |             |                |   |              |            |
| C                                |         | -0.0070156                                                           | 0.0257928   |                | 0 | 0 0.0698801  | 0.0109669  |



|                             |           |            |                                                                                                                                                                                                                     |            |            |   |            |            |
|-----------------------------|-----------|------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------|------------|---|------------|------------|
| N                           |           |            | -0.0190643                                                                                                                                                                                                          | 0.0141753  | 0          | 0 | -0.0497686 | -0.0161789 |
| O                           |           |            | -0.0374516                                                                                                                                                                                                          | 0.0469155  | 0          | 0 | -0.1080708 | 0.0300053  |
| Category 6: Aromatic rings  |           |            | $f(\theta, r) = c (1 - 3 \cos^2(\theta))/r^3$<br>c units: ppm/length                                                                                                                                                |            |            |   |            |            |
| Ring type                   |           |            |                                                                                                                                                                                                                     |            |            |   |            |            |
| PHE                         |           |            | 0.0186948                                                                                                                                                                                                           | 0.0109772  | 0          | 0 | 0.0369795  | 0.0228389  |
| TYR                         |           |            | 0.0185362                                                                                                                                                                                                           | 0.0068703  | 0          | 0 | 0.0333031  | 0.0210853  |
| TRP2                        |           |            | 0.0119457                                                                                                                                                                                                           | 0.0208549  | 0          | 0 | 0.0008892  | 0.0260824  |
| TRP1                        |           |            | 0.0194632                                                                                                                                                                                                           | 0.0120662  | 0          | 0 | 0.0365632  | 0.0191159  |
| HIS                         |           |            | 0.0121215                                                                                                                                                                                                           | 0.0038377  | 0          | 0 | 0.0193006  | 0.0144385  |
| Category 7: Dihedral angles |           |            | $f(\theta) = c (p_1 \cos(3(\theta + p_4)) + p_2 \cos(\theta + p_5) + p_3)$ , where $\theta \in \{\phi, \varphi, \chi_1\}$ . For parameters $p_1$ through $p_5$ see Table S2<br>c units: ppm; p units: dimensionless |            |            |   |            |            |
| Angle                       |           |            |                                                                                                                                                                                                                     |            |            |   |            |            |
| $\phi$                      |           |            | 0.4106709                                                                                                                                                                                                           | 0.481939   | 0          | 0 | -0.0141746 | 0.5496927  |
| $\varphi$                   |           |            | 0.2242678                                                                                                                                                                                                           | 0.4381989  | 0          | 0 | 0.1017863  | 0.7894501  |
| $\chi_1$                    |           |            | 0.0579212                                                                                                                                                                                                           | 0.0899445  | 0          | 0 | 0.433849   | 0.1204433  |
| Category 8: Hydrogen bonds  |           |            | $f(\theta) = c E(\theta)$ , where $\theta \in \{d, \gamma_1, \gamma_2\}$ . For function E(x) see Eq. S1 and Table S1<br>c units: ppm                                                                                |            |            |   |            |            |
| Origin                      | residue   | parameter  |                                                                                                                                                                                                                     |            |            |   |            |            |
| O                           | i-1       | d          | 1.07E-08                                                                                                                                                                                                            | -6.69E-06  | 0          | 0 | 8.95E-06   | 3.469E-05  |
| O                           | i-1       | $\gamma_1$ | -0.0005608                                                                                                                                                                                                          | 0.0019834  | 0          | 0 | 0.0044442  | -0.0018979 |
| O                           | i-1       | $\gamma_2$ | 6.722E-05                                                                                                                                                                                                           | -0.0001937 | 0          | 0 | -0.0004373 | 0.0001956  |
| H                           | i         | d          | -0.0015129                                                                                                                                                                                                          | 0.0025176  | 0          | 0 | -0.0047888 | -0.0068513 |
| H                           | i         | $\gamma_1$ | -2.591E-05                                                                                                                                                                                                          | 0.0012989  | 0          | 0 | -0.0003295 | 0.0003949  |
| H                           | i         | $\gamma_2$ | 1.342E-05                                                                                                                                                                                                           | -0.0001582 | 0          | 0 | 3.708E-05  | 8.74E-06   |
| O                           | i         | d          | 1.89E-06                                                                                                                                                                                                            | -2.615E-05 | 0          | 0 | -1.792E-05 | -1.858E-05 |
| O                           | i         | $\gamma_1$ | 0.000219                                                                                                                                                                                                            | -0.0001293 | 0          | 0 | -0.0111639 | 0.0010705  |
| O                           | i         | $\gamma_2$ | -1.871E-05                                                                                                                                                                                                          | 1.616E-05  | 0          | 0 | 0.0011469  | -0.0001135 |
| H                           | i+1       | d          | -0.0018291                                                                                                                                                                                                          | -0.0047666 | 0          | 0 | -0.0083926 | 0.0016062  |
| H                           | i+1       | $\gamma_1$ | 0.0007124                                                                                                                                                                                                           | 0.0034823  | 0          | 0 | 0.0057975  | -0.0005487 |
| H                           | i+1       | $\gamma_2$ | -6.613E-05                                                                                                                                                                                                          | -0.0003854 | 0          | 0 | -0.0005543 | 7.667E-05  |
| Category 9: Extra distances |           |            | $f(d) = c d^\beta$ , $\beta = 1$<br>c units: ppm/length                                                                                                                                                             |            |            |   |            |            |
| Atom 1                      | residue 1 | atom 2     | residue 2                                                                                                                                                                                                           |            |            |   |            |            |
| H                           | i         | HA         | i                                                                                                                                                                                                                   | 0          | 0          | 0 | 0          | 0          |
| H                           | i         | C          | i                                                                                                                                                                                                                   | 0          | 0          | 0 | 0          | 0          |
| H                           | i         | CB         | i                                                                                                                                                                                                                   | 0          | 0          | 0 | 0          | 0          |
| C                           | i-1       | HA         | i                                                                                                                                                                                                                   | 0.0239546  | 0.0550619  | 0 | 0          | -0.1309367 |
| C                           | i-1       | C          | i                                                                                                                                                                                                                   | 0.3639351  | -1.8245109 | 0 | 0          | -2.1589941 |
| C                           | i-1       | CB         | i                                                                                                                                                                                                                   | 0.0601703  | -1.1517461 | 0 | 0          | 1.4440016  |
| O                           | i         | HA         | i                                                                                                                                                                                                                   | 0.0466054  | -7.9758753 | 0 | 0          | -0.4737369 |
| O                           | i         | N          | i                                                                                                                                                                                                                   | 0.0608192  | 0.0143416  | 0 | 0          | 0.4166167  |
| O                           | i         | CB         | i                                                                                                                                                                                                                   | -0.0032265 | 0.177568   | 0 | 0          | 0.3098538  |
| N                           | i+1       | HA         | i                                                                                                                                                                                                                   | -0.3380021 | -7.1442735 | 0 | 0          | 0.4825454  |
| N                           | i+1       | N          | i                                                                                                                                                                                                                   | 0.2101381  | -1.4483086 | 0 | 0          | 0.2440395  |
| N                           | i+1       | CB         | i                                                                                                                                                                                                                   | -0.1088596 | -0.1018623 | 0 | 0          | 0.0799778  |
| O                           | i-1       | HA         | i-1                                                                                                                                                                                                                 | -0.1535562 | 0.9541831  | 0 | 0          | -0.3530593 |
| O                           | i-1       | N          | i-1                                                                                                                                                                                                                 | -0.1617153 | -0.0384509 | 0 | 0          | 0.2598648  |
| O                           | i-1       | CB         | i-1                                                                                                                                                                                                                 | -0.0505202 | 0.0836814  | 0 | 0          | 0.2533118  |
| N                           | i         | HA         | i-1                                                                                                                                                                                                                 | -0.1062667 | 2.7549949  | 0 | 0          | 0.1927719  |
| N                           | i         | N          | i-1                                                                                                                                                                                                                 | -0.0340523 | 0.2772183  | 0 | 0          | 0.2516512  |
| N                           | i         | CB         | i-1                                                                                                                                                                                                                 | 0.0358333  | -0.0347704 | 0 | 0          | -0.2073699 |
| CG                          | i         | HA         | i                                                                                                                                                                                                                   | 0.1186278  | -0.5677036 | 0 | 0          | 0.0794325  |
| CG                          | i         | N          | i                                                                                                                                                                                                                   | -0.0881744 | 0.4042956  | 0 | 0          | -0.117154  |
| CG                          | i         | C          | i                                                                                                                                                                                                                   | -0.0746942 | 0.3357447  | 0 | 0          | -0.0332108 |
| CG                          | i         | C          | i-1                                                                                                                                                                                                                 | 0.0187258  | -0.1100216 | 0 | 0          | 0.0023606  |
| CG                          | i         | N          | i+1                                                                                                                                                                                                                 | 0.0290884  | -0.105078  | 0 | 0          | 0.0711681  |

|    |     |    |     |            |            |   |   |            |           |
|----|-----|----|-----|------------|------------|---|---|------------|-----------|
| CG | i-1 | CA | i   | 0.0042968  | -0.0012085 | 0 | 0 | -0.0091117 | 0.0070518 |
| CG | i+1 | CA | i   | 0.001109   | 0.0159162  | 0 | 0 | -0.0382256 | 0.0025576 |
| CA | i-1 | CA | i+1 | -0.1514723 | 0.7027408  | 0 | 0 | 0.4796896  | 0.3274878 |

Table S6. Values of the parameters of Eq. 1 in the main text. The equations for the terms  $f(\mathbf{x})$  describing the various contributions are also given. Chemical shifts  $\delta$  are calculated as random coil values  $c_0$  plus the sum over the  $f(\mathbf{x})$  terms for all categories. Additional parameters for the hydrogen bonding and the dihedral angle terms can be found in Tables S1 and S2, respectively. For categories 2, 3, 4, and 5, distances are calculated from the query atom to each of the atoms listed. The units of the parameters  $c$  are also given.

## References

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