

Table S1. 1s core-excitation energies (in eV) of C₂H₄, CO₂, N₂, NH₃, H₂O, F₂, and HF molecules and Ne atom calculated by TDDFT with LC-PSRSIC for various a values. Cc-pVTZ plus Rydberg basis functions were used. Errors with respect to the experimental data are shown in parentheses.

Molecule	Assignment	LC-PSRSIC with various values of a								Exptl.
$X = C$		a value								
		0.89	0.90	0.91	0.92	0.93	0.94	0.95	0.96	
C ₂ H ₄	C1s $\rightarrow \pi^*$	—	288.4	287.4	286.1	284.5	—	279.3	275.1	284.7 ^a
			(+3.7)	(+2.7)	(+1.4)	(-0.2)		(-5.4)	(-9.6)	
	C1s $\rightarrow 3s\sigma$	—	291.5	290.6	289.5	287.9	—	279.6	276.1	287.1 ^b
			(+4.4)	(+3.5)	(+2.4)	(+0.8)		(-7.5)	(-11.0)	
CO ₂	C1s $\rightarrow \pi^*$	296.1	295.2	294.2	292.9	291.2	289.1	286.1	282.1	291.0 ^c
			(+5.1)	(+4.2)	(+3.2)	(+1.9)	(+0.2)	(-1.9)	(-4.9)	(-8.9)
	C1s $\rightarrow 3p\pi$	298.4	297.5	296.5	295.3	293.7	291.6	288.8	284.8	295.3 ^c
			(+3.1)	(+2.2)	(+1.2)	(-0.0)	(-1.6)	(-3.7)	(-6.5)	(-10.5)
ME ⁱ		+2.0	+3.6	+2.6	+1.4	-0.2	-1.4	-6.1	-10.0	
$X = N$		a value								
		0.88	0.89	0.90	0.91	0.92	0.93	0.94	0.95	
N ₂	N1s $\rightarrow \pi^*$	407.1	406.0	404.9	403.4	401.8	399.7	397.0	393.5	401.0 ^d
			(+6.1)	(+5.0)	(+3.9)	(+2.4)	(+0.8)	(-1.3)	(-4.0)	(-7.5)
	N1s $\rightarrow 3p\pi$	411.5	410.4	409.2	407.7	405.9	403.7	401.0	397.4	407.1 ^e
			(+4.4)	(+3.3)	(+2.1)	(+0.6)	(-1.2)	(-3.4)	(-6.1)	(-9.7)
NH ₃	N1s $\rightarrow 3s$	403.4	402.4	401.2	399.8	398.1	395.9	393.1	389.5	400.7 ^f
			(+2.7)	(+1.7)	(+0.5)	(-0.9)	(-2.6)	(-4.8)	(-7.6)	(-11.2)
	N1s $\rightarrow 3p_e$	405.0	403.9	402.7	401.2	399.5	397.4	394.6	391.0	402.3 ^f
			(+2.7)	(+1.6)	(+0.4)	(-1.1)	(-2.8)	(-4.9)	(-7.7)	(-11.3)
ME ⁱ		+4.0	+2.9	+1.7	+0.3	-1.5	-3.6	-6.3	-9.9	
$X = O$		a value								
		0.87	0.88	0.89	0.90	0.91	0.92	0.93	0.94	
CO ₂	O1s $\rightarrow \pi^*$	541.1	539.8	538.4	536.6	534.6	532.1	529.1	525.5	534.6 ^c
			(+6.5)	(+5.2)	(+3.8)	(+2.0)	(-0.0)	(-2.5)	(-5.5)	(-9.1)
	O1s $\rightarrow 3p\pi$	542.8	541.5	540.0	538.3	536.3	533.9	531.0	527.4	538.4 ^c
			(+4.4)	(+3.1)	(+1.6)	(-0.1)	(-2.1)	(-4.5)	(-7.4)	(-11.0)
H ₂ O	O1s $\rightarrow 3s$	537.1	535.9	534.5	532.9	530.9	528.6	525.8	522.4	534.0 ^f
			(+3.1)	(+1.9)	(+0.5)	(-1.1)	(-3.1)	(-5.4)	(-8.2)	(-11.6)
	O1s $\rightarrow 3p_{b2}$	540.6	539.2	537.7	535.9	533.8	531.4	528.4	524.8	535.9 ^f
			(+4.7)	(+3.3)	(+1.8)	(+0.0)	(-2.1)	(-4.5)	(-7.5)	(-11.1)
ME ⁱ		+4.7	+3.4	+1.9	+0.2	-1.8	-4.2	-7.2	-10.7	
$X = F$		a value								
		0.85	0.86	0.87	0.88	0.89	0.90	0.91	0.92	
F ₂	F1s $\rightarrow \sigma^*$	690.8	689.5	688.1	686.5	684.7	682.5	680.0	677.1	682.2 ^g
			(+8.6)	(+7.3)	(+5.9)	(+4.3)	(+2.5)	(+0.3)	(-2.2)	(-5.1)
	F1s $\rightarrow 3p$	698.0	696.6	695.1	693.4	691.6	689.4	687.0	684.1	693.6 ^g
			(+4.4)	(+3.0)	(+1.5)	(-0.2)	(-2.0)	(-4.2)	(-6.6)	(-9.5)
HF	F1s $\rightarrow \sigma^*$	690.6	689.4	688.0	686.4	684.6	682.5	680.0	677.2	687.4 ^g
			(+3.2)	(+2.0)	(+0.6)	(-1.0)	(-2.8)	(-4.9)	(-7.4)	(-10.2)
	F1s $\rightarrow 3p$	694.2	692.8	691.3	689.5	687.6	685.4	682.9	679.9	690.8 ^g
			(+3.4)	(+2.0)	(+0.5)	(-1.3)	(-3.2)	(-5.4)	(-7.9)	(-10.9)
ME ⁱ		+4.9	+3.6	+2.1	+0.5	-1.4	-3.5	-6.0	-8.9	
$X = Ne$		a value								
		0.80	0.81	0.82	0.83	0.84	0.85	0.86	0.87	
Ne	Ne1s $\rightarrow 3p_{1u}$	872.3	871.0	869.6	868.2	866.6	865.0	863.2	861.3	867.1 ^h
			(+5.2)	(+3.9)	(+2.5)	(+1.1)	(-0.5)	(-2.1)	(-3.9)	(-5.8)

^a Ref. 51.^b Ref. 52.^c Ref. 58.^d Ref. 52.^e Chen, C. T.; Ma, Y.; Sette, F. Phys. Rev. A 1989, 40, 6737.^f Ref. 54.^g Ref. 55.^h Ref. 56.ⁱ Mean errors from the experimental data.