

Dense sphere packing in the NaZn₁₃ structure type – supplementary information

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Table 2 - extended Parameters and properties of the globally optimal A₁₃B packing are compared to those of atomic structures (when the atomic sites are decorated with touching binary hard spheres).

| Structure | r_A/r_B | ϕ | a/r_B | y | z |
|---|-----------|----------|---------|-------------|-------------|
| Globally optimal A ₁₃ B packing | 0.578458 | 0.748431 | 5.39970 | 0.180551 | 0.115354 |
| SbBe ₁₃ [Haase <i>et al.</i>] | 0.5692 | 0.7393 | 5.360 | 0.1781(5) | 0.1157(5) |
| BaBe ₁₃ [Klemm <i>et al.</i>] | 0.5319 | 0.7178 | 5.168 | 0.1740 | 0.1100 |
| CaBe ₁₃ [Baker <i>et al.</i>] | 0.5518 | 0.7303 | 5.267 | 0.1769(2) | 0.1123(2) |
| DyBe ₁₃ [Vigneron <i>et al.</i>] | 0.5641 | 0.7360 | 5.334 | 0.1775(5) | 0.1150(4) |
| MgBe ₁₃ [Baker <i>et al.</i>] | 0.5713 | 0.7439 | 5.363 | 0.1789(10) | 0.1143(8) |
| SrBe ₁₃ [Matyushenko <i>et al.</i>] | 0.5360 | 0.7212 | 5.186 | 0.1750 | 0.1100 |
| ThBe ₁₃ [Goldman <i>et al.</i>] | 0.5440 | 0.7225 | 5.235 | 0.1745(1) | 0.1129(1) |
| UBe ₁₃ [Goldman <i>et al.</i>] | 0.5590 | 0.7315 | 5.311 | 0.1763(1) | 0.1150(1) |
| UBe ₁₃ [McElfresh <i>et al.</i>] | 0.5602 | 0.7324 | 5.317 | 0.1765(9) | 0.1151(9) |
| CeBe ₁₃ [Wilson <i>et al.</i>] | 0.5538 | 0.7292 | 5.283 | 0.1761(3) | 0.1138(3) |
| LaCo ₁₃ [Zarechnyuk <i>et al.</i>] | 0.5580 | 0.7038 | 5.373 | 0.1780 | 0.1220 |
| BaCu ₁₃ [Braun <i>et al.</i>] | 0.5633 | 0.7152 | 5.380 | 0.1806 | 0.1192 |
| NaZn ₁₃ [Zintl <i>et al.</i>] | 0.5580 | 0.7038 | 5.374 | 0.1780 | 0.1220 |
| NaZn ₁₃ [Shoemaker <i>et al.</i>] | 0.5631 | 0.7147 | 5.380 | 0.18063(25) | 0.11924(28) |
| RbZn ₁₃ [Bruzzzone <i>et al.</i>] | 0.5654 | 0.7195 | 5.383 | 0.1800 | 0.1190 |

Table 4 - extended Parameters and properties of the optimal non-interstitial A₁₂BC packing in the NaZn₁₃ structure type are compared to those of atomic structures (when the atomic sites are decorated with touching ternary hard spheres)..

| Structure | r_A/r_B | r_C/r_A | ϕ | a/r_B | y | z |
|---|-----------|-----------|---------|---------|-------------|-------------|
| Globally optimal A ₁₂ BC packing | 0.59262 | 0.91796 | 0.77124 | 5.4169 | 0.17610 | 0.11408 |
| SbBe ₁₃ [Haase <i>et al.</i>] | 0.5821 | 0.9717 | 0.7533 | 5.404 | 0.1781(5) | 0.1157(5) |
| BaBe ₁₃ [Klemm <i>et al.</i>] | 0.5714 | 0.9098 | 0.7602 | 5.301 | 0.1740 | 0.1100 |
| CaBe ₁₃ [Baker <i>et al.</i>] | 0.5781 | 0.9414 | 0.7588 | 5.356 | 0.1769(2) | 0.1123(2) |
| DyBe ₁₃ [Vigneron <i>et al.</i>] | 0.5861 | 0.9519 | 0.7600 | 5.409 | 0.1775(5) | 0.1150(4) |
| MgBe ₁₃ [Baker <i>et al.</i>] | 0.5801 | 0.9722 | 0.7541 | 5.389 | 0.1789(10) | 0.1143(8) |
| SrBe ₁₃ [Matyushenko <i>et al.</i>] | 0.5743 | 0.9130 | 0.7626 | 5.315 | 0.1750 | 0.1100 |
| ThBe ₁₃ [Goldman <i>et al.</i>] | 0.5810 | 0.9176 | 0.7626 | 5.360 | 0.1745(1) | 0.1129(1) |
| UBe ₁₃ [Goldman <i>et al.</i>] | 0.5886 | 0.9354 | 0.7640 | 5.412 | 0.1763(1) | 0.1150(1) |
| UBe ₁₃ [McElfresh <i>et al.</i>] | 0.5878 | 0.9398 | 0.7626 | 5.411 | 0.1765(9) | 0.1151(9) |
| CeBe ₁₃ [Wilson <i>et al.</i>] | 0.5910 | 0.9191 | 0.7701 | 5.409 | 0.1761(3) | 0.1138(3) |
| LaCo ₁₃ [Zarechnyuk <i>et al.</i>] | 0.5580 | 1.0780 | 0.7133 | 5.373 | 0.1780 | 0.1220 |
| BaCu ₁₃ [Braun <i>et al.</i>] | 0.5633 | 1.0667 | 0.7234 | 5.380 | 0.1806 | 0.1192 |
| NaZn ₁₃ [Zintl <i>et al.</i>] | 0.5580 | 1.0780 | 0.7133 | 5.373 | 0.1780 | 0.1220 |
| NaZn ₁₃ [Shoemaker <i>et al.</i>] | 0.5631 | 1.0679 | 0.7231 | 5.380 | 0.18063(25) | 0.11924(28) |
| RbZn ₁₃ [Bruzzzone <i>et al.</i>] | 0.5654 | 1.0545 | 0.7262 | 5.383 | 0.1800 | 0.1190 |

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