Size-dependent transition to high-symmetry chiral structures in AgCu, AgCo, AgNi and AuNi nanoalloys - Online supporting information

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The form of the atom-atom potential used in the simulations is derived with the second-moment approximation to the tight-binding model [1, 2]. The binding energy of the system E is writte as:

$$E = \sum_{i}^{N} \left[E^{r}(i) + E^{a}(i) \right]$$
(1)

 $E^{r}(i)$ and $E^{a}(i)$ represent repulsive and attractive contributions, respectively, and are defined as

$$E^{r}(i) = \sum_{i \neq j}^{N} A(a, b) e^{-p(a, b)(r_{ij}/r_{0}(a, b) - 1)}$$
$$E^{a}(i) = \left[\sum_{i \neq j}^{N} \xi^{2}(a, b) e^{-2q(a, b)(r_{ij}/r_{0}(a, b) - 1)}\right]^{1/2}$$
(2)

where a(b) represent the atomic species of atom i(j), r_{ij} is the distance between these atoms, and r_0 , ξ , q, p and A are adjustable parameters. For a binary system a set of 15 parameters (5 for each element plus 5 describing the mixing) need to be defined, of which only 12 are independent (it is always possible to adjust the other parameters to changes in r_0). Here we present two parameter sets, named P1 and P2. The results in the Letter are obtained by P1, unless otherwise specified. Parameter sets for both potentials are reported in Table I. P2 was used in Refs. [3–5]. P1 has been refitted in order to achieve a better agreement with Density-Functional results for surface energies and the energetics of small clusters (up to 55 atoms, see Tables II and III), while reproducing the experimental data for lattice spacing, cohesive energy and bulk modulus for the pure elements. The results of both potentials are compared to the DF results for larger clusters (size between 100 and 300 atoms) in Table IV.

As follows from the analysis of the results, the agreement between DF calculations and P1 results is very good in the whole nanoalloy size range. P1 and DF always agree for the lowest energy structure. The agreement improves with increasing size. In fact, for sizes above 100 atoms, the energetic ordering of the isomers is always correctly reproduced, with a good quantitative agreement for the energy differences. For small sizes, some discrepancies remains, that we were not able to overcome by means of this simple interaction model. The agreement between P2 and DF is also good, even though P2 is not able to single out the lowest-energy structures of $Ag_{32}Cu_6$ and $Ag_{132}Cu_{147}$. In the latter case, energies of anti-Mackay and chiral icosahedra are however quasi-degenerate. The quantitative agreement of P2 with DF for the energy differences between isomers is on average somewhat worse than for the P1. We remark however that overall trends are the same for all calculations.

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TABLE I:						
	P1			P2		
Parameters	Ag-Ag	Cu-Cu	Ag-Cu	Ag-Ag	Cu-Cu	Ag-Cu
A(eV)	0.0801	0.0834	0.0900	0.1031	0.0894	0.0977
$\xi(eV)$	1.0883	1.2167	1.1115	1.2799	1.2799	1.2275
p(eV)	12.0	11.0	11.111	10.85	10.55	10.70
q(eV)	2.85	2.30	2.013	3.18	2.43	2.805
$r_0(\text{\AA})$	2.89	2.56	2.725	2.89	2.56	2.725

TABLE II: Surface energies γ (in mJ/m²) for three low-index facets of pure Ag and Cu fcc bulk systems. For the values of the parameters, see Table I. DF calculations [6] are made by the Quantum Espresso package [7] and use the PBE exchange-correlation functional [8].

Element	Quantity	Density Functional	P1	P2
Ag	γ_{111}	738	710	586
	γ_{100}	788	790	659
	γ_{110}	889	857	724
Cu	γ_{111}	1269	1211	1074
	γ_{100}	1360	1309	1156
	γ_{110}	1507	1412	1290

TABLE III: . Energetics of Mackay and anti-Mackay icosahedra for pure Ag and Cu clusters of size 45.The structures are shown in Fig. 1. Energies are given in eV.

System	n Structure	Density Functional	P1	P2
Ag_{45}	Mackay1	0.000	0.000	0.000
Ag_{45}	anti-Mackay	3.060	3.865	4.795
Cu_{45}	Mackay1	0.000	0.000	0.000
Cu_{45}	anti-Mackay	3.523	2.683	2.313

TABLE IV: Energetics of small-size nanoalloys. For each size and composition, the data report the energy difference from the most stable isomer according to DF calculations, which is taken as the zero of the energy. The structures are shown in Fig. 1, with the exception of the 13-atom icosahedra. Energy differences are given in eV.

size and composition	structure	Density Functional	P1	P2
13 Ag_1Cu_{12}	Ihsup	0.000	0.000	0.000
	Ihcen	1.771	2.522	1.608
13 $Ag_{12}Cu_1$	Ihcen	0.000	0.000	0.000
	Ihsup	0.415	0.233	0.706
34 Ag ₂₇ Cu ₇	pc5	0.000	0.000	0.000
	pc5def	0.627	0.531	0.448
	asymm	0.999	0.438	0.305
38 Ag ₃₂ Cu ₆	pc5mod	0.000	0.000	0.000
	рс6	0.335	0.320	-0.261
	C_s	0.790	0.226	0.189
	truncated octahedron (TO)	1.585	0.614	0.623
45 $Ag_{32}Cu_{13}$	anti-Mackay	0.000	0.000	0.000
	Mackay1	1.300	0.797	1.081
	Mackay2	1.385	0.422	0.853
55 Ag ₃₂ Cu ₁₃	Mackay	0.000	0.000	0.000
	D_{5h}	0.873	0.794	0.747
	Ino decahedron	3.010	3.399	2.628
	cuboctahedron	4.063	4.221	3.287

TABLE V: Energetics of large nanoalloys. For each size and composition, the data report the energy difference from the most stable isomer according to DF calculations, which is taken as the zero of the energy. The structures are shown in Fig. 2. Energy differences are given in eV.

structure	Density Functional	P1	P2
anti-Mackay	0.000	0.000	0.000
tetraIh	0.644	0.744	1.183
Mackay	2.013	2.604	2.952
chiral icosahedron	not stable	not stable	not stable
tetraIh	0.000	0.000	0.000
anti-Mackay	1.087	0.752	0.087
pentaIh	0.000	0.000	0.000
Mackay	1.220	1.120	2.156
Marks decahedron	9.460	7.300	7.882
pentaIh	0.000	0.000	0.000
Mackay	0.352	0.133	1.357
Ino decahedron	7.831	7.589	3.901
cuboctahedron	9.850	9.412	8.296
chiral C ₅	0.000	0.000	0.000
Marks decahedron	7.991	7.412	7.602
anti-Mackay	0.000	0.000	0.000
chiral icosahedron	0.430	0.072	-0.132
Mackay	7.083	7.943	7.467
chiral icosahedron		0.000	0.000
anti-Mackay		1.666	1.718
chiral icosahedron		0.000	0.000
anti-Mackay		not stable	2.171
chiral icosahedron		0.000	0.000
anti-Mackay		not stable	6.448
	anti-Mackay tetraIh Mackay chiral icosahedron tetraIh anti-Mackay pentaIh Mackay Marks decahedron pentaIh Mackay Mackay Marks decahedron chiral C5 Marks decahedron chiral C5 Marks decahedron anti-Mackay chiral icosahedron Mackay chiral icosahedron anti-Mackay chiral icosahedron	anti-Mackay 0.000 tetraIh 0.644 Mackay 2.013 chiral icosahedron not stable tetraIh 0.000 anti-Mackay 1.087 pentaIh 0.000 Mackay 1.220 Mackay 1.220 Marks decahedron 9.460 pentaIh 0.000 Mackay 0.352 Ino decahedron 7.831 cuboctahedron 9.850 chiral C5 0.000 Marks decahedron 7.991 anti-Mackay 0.000 chiral icosahedron 0.430 Mackay 7.083 chiral icosahedron — anti-Mackay — chiral icosahedron — chiral icosahedr	anti-Mackay 0.000 0.000 tetraIh 0.644 0.744 Mackay 2.013 2.604 chiral icosahedron not stable not stable 1 tetraIh 0.000 0.000 anti-Mackay 1.087 0.752 pentaIh 0.000 0.000 Mackay 1.220 1.120 Marks decahedron 9.460 7.300 pentaIh 0.000 0.000 Mackay 0.352 0.133 Ino decahedron 7.831 7.589 cuboctahedron 9.850 9.412 chiral C5 0.000 0.000 Marks decahedron 7.991 7.412 anti-Mackay 0.000 0.000 Marks decahedron 7.991 7.412 anti-Mackay 0.000 0.000 chiral icosahedron - 0.000 anti-Mackay 0.000 0.000 anti-Mackay - 0.000 anti-Mackay - 0.000 anti-Mackay - 0.000

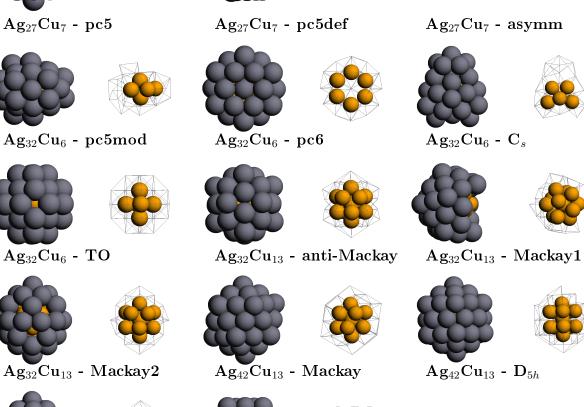
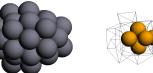


FIG. 1: Structures of small size nanoalloys. Dh stands for decahedron.







 $Ag_{32}Cu_6$ - TO



 $Ag_{32}Cu_{13}$ - Mackay2



 $Ag_{42}Cu_{13}$ - Ino Dh





 $\mathbf{Ag}_{42}\mathbf{Cu}_{13}$ - cuboctahedron











$Ag_{72}Cu_{55}$ - anti-Mackay $Ag_{72}Cu_{55}$ - tetraIh $\mathbf{Ag}_{72}\mathbf{Cu}_{55}$ - Mackay $\mathbf{Ag}_{75}\mathbf{Cu}_{52}$ - tetraIh $Ag_{75}Cu_{52}$ - anti-Mackay $Ag_{90}Cu_{56}$ - pentaIh $Ag_{90}Cu_{56}$ - Mackay $Ag_{90}Cu_{56}$ - Marks Dh $Ag_{92}Cu_{55}$ - pentaIh $Ag_{92}Cu_{55}$ - Mackay $Ag_{92}Cu_{55}$ - Ino Dh $Ag_{92}Cu_{55}$ - cuboctahedron

 $\mathbf{Ag}_{107}\mathbf{Cu}_{85}$ - \mathbf{C}_{5}

- $Ag_{132}Cu_{147}$ anti-Mackay $Ag_{132}Cu_{147}$ chiral

FIG. 2: Structures of large nanoalloys. Dh stands for decahedron.