Review and Analysis of Molecular Simulations of Methane, Hydrogen, and Acetylene Storage in Metal-Organic Frameworks

Supporting Information

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This supporting information discusses the following:

- 1. Interaction models for H₂ with Li-doped and Li-alkoxide-functionalized IRMOF-8
- 2. Details of GCMC simulations
- 3. Reviews of simulated vs. experimental adsorption results for CH_4 and H_2 in MOFs.

S1. Interaction Models for H₂ with Li-Doped and Li-Alkoxide-Functionalized Variants of **IRMOF-8**

In section 5.3.2 of the main text, results are compared for simulations that use different model choices for hydrogen adsorption in Li-doped and Li-alkoxide-functionalized MOFs. Details of those simulations are provided here.

S1.1 H₂ Interactions with C, H, O, Zn, and H₂

H₂ interactions with framework C, H, O (excluding O in the alkoxide groups), and Zn atoms were calculated using Lennard-Jones potentials. Framework atom parameters were taken from the DREIDING force field.¹ Lennard-Jones Parameters for H₂ were taken from empirical data based on the second virial coefficient.² Each H₂ molecule was treated as a single sphere. Cross-

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term H_2/MOF parameters were obtained using the Lorentz-Berthelot mixing rules and are provided in Table S1. H_2/H_2 interactions were also computed using a Lennard-Jones potential, treating each H_2 molecule as a single sphere. All Lennard-Jones interactions were calculated out to a cut-off distance of 12 Å. This interaction model has been previously shown to reproduce experimental isotherms in un-doped, unfunctionalized MOFs very well.³

Table S1. Lennard-Jones parameters used to describe H₂/H₂ and H₂/framework atom interactions

Х	$\sigma_{ m H2-X}$ (Å)	$\varepsilon_{\text{H2-X}}/k_B$ (K)
Zn	3.499	31.884
С	3.214	41.910
Н	2.90	16.76
0	2.994	42.054
H_2	2.958	36.700

S1.2 H₂ Interactions with Li and Li Alkoxide Groups

 H_2 interactions with Li (doped MOFs) and Li alkoxide (functionalized MOFs) were calculated using Morse (doped MOFs) and Morse plus Coulomb potentials (functionalized MOFs.) Morse parameters were obtained from *ab initio* results (the parameterization procedures and final sets of parameters are given below.) Both H nuclei in the H_2 molecule were treated as Morse sites in these calculations. Partial charges in the alkoxide groups in functionalized MOFs were taken from *ab initio* calculations. The full procedure for obtaining these charges is described in depth in the Supporting Information by Getman et al.⁴ For simulations on functionalized MOFs, partial charges along the H_2 axis were taken from the Darkrim-Levesque model,⁵ which places charges of +0.468 at the H nuclei and a charge of -0.936 at the center of mass in order to simulate the quadrupole. Coulomb interactions were only calculated for the H_2 /alkoxide O and H_2 /alkoxide Li interactions. All other charge-quadrupole, quadrupole-quadrupole, and other Coulomb effects were neglected in our simulations.

S1.3 H₂/Li and H₂/Li Alkoxide Morse Parameters

In this review, we calculated H_2 adsorption isotherms in Li-doped IRMOF-8 and Li-alkoxidefunctionalized IRMOF-8. We calculated isotherms in Li-doped IRMOF-8 using three different sets of interaction parameters for H_2/Li . Two of these were developed in this work using two different Li^+ site models and the other was taken from Deng *et al.*⁶ All force fields developed in this work were parameterized by fitting a pair potential to the electronic binding energies for H_2 adsorbed in a variety of configurations surrounding the Li^+ site,

$$\Delta E^{bind}(r) = E^{elec}_{\mathrm{Li}^+ - \mathrm{H}_2}(r) - E^{elec}_{\mathrm{Li}^+} - E^{elec}_{\mathrm{H}_2}$$
(Eq. S1)

where 'Li⁺' broadly describes the model containing the open Li⁺ site. ΔE^{bind} values for the first set were calculated with MP2/6-311+G** between H₂ and a bare Li⁺ cation and fit to a Morse potential

$$\mathcal{V}_{ij} = D_{ij} \left[e^{\alpha_{ij} \left(1 - r_{ij} / r_{ij}^{*} \right)} - 2 e^{\left(\alpha_{ij} / 2 \right) \left(1 - r_{ij} / r_{ij}^{*} \right)} \right]$$
(Eq. S2)

Note that this H_2/Li^+ system has a net charge of +1 in the quantum calculations. However all species were considered to be neutral in the pair potentials and GCMC calculations, i.e. the

charge/quadropole interactions were implicitly incorporated into the Morse potential instead of added as separate terms.

For the second parameter set, we used a similar procedure, this time using potential energies calculated between H_2 and a $Li^+(C_{10}H_8)^-$ model at the same level of theory. Note that Li in this system adopts a partial positive charge and $C_{10}H_8$ adopts the opposite charge, but the system as a whole is charge neutral. Here we only developed parameters to describe the H_2/Li^+ interaction, and H_2 interactions with all other atoms were simulated using the conventional force field models described above.

The third parameter set was taken from Deng *et al.*⁶ All parameters are provided in Table S2.

We used two different interaction models to simulate H₂ adsorption in Li-alkoxidefunctionalized IRMOF-8. The first set we took directly from our previous work,⁴ which fit ΔE^{bind} between H₂ and Li alkoxide benzene models calculated at the MP2/6-311+G** level of theory to a Morse + Coulomb potential

$$\mathcal{V}_{ij} = -D_{ij} \left[1 - \left(1 - e^{-\alpha_{ij} \left(r_{oj} - r_{ij}^{*} \right)} \right)^{2} \right] + \frac{q_{i}q_{j}}{4\pi\epsilon_{0}r_{ij}}$$
(Eq. S3)

The second set are Lennard-Jones parameters taken from Klontzas *et al.*⁷ The Lennard-Jones equation is

$$\mathcal{V}_{ij} = 4\varepsilon_{ij} \left[\left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^{6} \right]$$
(Eq. S4)

All parameters are provided in Table S2.

Table S2. Interaction parameters for H₂/Li (doped MOFs) and H₂/alkoxide O and H₂/alkoxide Li (functionalized MOFs) developed using different methods.

Li-Doped IRMOF-8								
Parameters from	X	Interaction Equation	r _{H-X} (Å)	$\begin{array}{c c} D_{\text{H-X}}/k_B \\ (\text{K}) \end{array}$	$\alpha_{\text{H-X}}$ (Å ⁻¹)	Partial charge		
This work, bare Li^+	Li ⁺	S2	2.017	1101.428	8.147	N/A		
This work, $Li^+(C_{10}H_8)^-$	Li ⁺	S2	2.123	562.775	6.664	N/A		
Deng et al. ⁶	Li ⁺	S2	2.066	1361.751	6.684	N/A		
		Li Alkoxide-	Functionalize	ed IRMOF-8				
Parameters	Χ	Interaction	r _{H-X} or	$D_{\rm H-X}/k_B$ or	α _{H-X} (Å ⁻¹)	Partial		
from		Equation	σ _{H2-X} (Å)	$\epsilon_{\mathrm{H2-X}}/k_B$ (K)		charge		
Getman <i>et</i> $al.^4$	Li^+	S3	2.271	226.993	2.086	+0.9		
	0_	S3	4.550	11.992	1.074	-0.9		
Klontzas <i>et</i> $al.^7$	Li ⁺	S4	1.80	1505.0	N/A	N/A		
	0-	S4	2.43	859.0	N/A	N/A		

S1.4 Force Field Parameterization Procedure

Our force field parameterization procedure is described in depth in the Supporting Information of

Ref.⁴ The main points are summarized here.

$S1.4.1 H_2/Li^+$

Parameters for H_2 interactions with a bare Li^+ cation were obtained by fitting a Morse equation (Eq. S2) to discrete energies calculated using the Gaussian 09^8 quantum chemical software. We included two routes for H_2 to Li^+ , one where H_2 binds side on to Li^+ and one where it binds head on. We allowed the H—H bond to relax in the calculations, but we held the H_2 — Li^+ distance fixed at each point. Calculations were performed at the MP2/6-311+G** level of theory using the counterpoise method⁹ to offset errors due to basis set superposition. The final set of parameters is given in Table S2. Force field energies are compared with *ab initio* energies in Figure S1. The RMS difference between force field and *ab initio* energies is 3.29 kJ mol⁻¹ for all configurations where the *ab initio* energies are less than 0.



Figure S1. Interaction energies calculated with the Morse potential (Eq. S2, lines) compared with energies calculated with MP2/6-311+G** (symbols) for H₂ interactions with a bare Li^+ cation.

 $S1.4.2 H_2/Li^+(C_{10}H_8)^-$

Parameters for H₂ interactions with the Li ion in $\text{Li}^+(\text{C}_{10}\text{H}_8)^-$ were obtained by fitting a Morse + Lennard-Jones potential to discrete energies calculated using the Gaussian 09⁸ quantum chemical software. The Morse and Lennard-Jones equations are given in Eqs. S2 and S4, respectively. In the quantum chemical calculations, the geometry of the $\text{Li}^+(\text{C}_{10}\text{H}_8)^-$ group was held fixed at the calculated optimum in the absence of H₂, the distance between the H₂ center of mass and Li⁺ was held fixed at each point, and the orientation of the H₂ molecule was held fixed with respect to $\text{Li}^+(\text{C}_{10}\text{H}_8)^-$. The H—H bond was allowed to relax. We attempted to sample the entire interaction region surrounding Li⁺, moving H₂ from 5 to 1.5 Å from Li⁺ and exploring a variety of "approach" routes (see Figure S2). Calculations were performed at the MP2/6-311+G** level of theory using the counterpoise method⁹ to offset errors due to basis set superposition. In these calculations, H₂, Li, and C₁₀H₈ were all considered to be separate fragments.

In the Morse + Lennard-Jones potential, dispersion and repulsion interactions between the H₂ center of mass and C and H were calculated with Lennard-Jones potentials, employing the parameters in Table S1 (these parameters were held fixed). Dispersion and repulsion interactions between each H nucleus and Li were calculated with a Morse potential. Morse parameters were obtained by fitting the pairwise sum of all interactions,

$$\mathcal{V}^{\text{force field}} = \sum_{i} \mathcal{V}_{i}^{\text{Morse}} + \sum_{j} \mathcal{V}_{j}^{\text{Lennard-Jones}}$$
 (Eq. S5)

where *i* is over the interactions between the H nuclei and Li, and *j* is over the interactions between the H₂ center of mass and the atoms in the $C_{10}H_8$ fragment, to the *ab initio* energies using a simulated annealing method.¹⁰ The final set of parameters, i.e. the set that minimizes the root mean square difference between parameterized and *ab initio* energies, is given in Table S2.

Force field energies are compared with *ab initio* energies in Figure S2. The RMS difference between force field and *ab initio* energies is 1.40 kJ mol⁻¹ for all configurations where the *ab initio* energies are less than 0.



Figure S2. Interaction energies calculated with the Morse potential (Eq. S2, lines) compared with energies calculated with MP2/6-311+G** (symbols) for H₂ interactions with $\text{Li}^+(\text{C}_{10}\text{H}_8)^-$.

S1.4.3 H₂/Li Alkoxide

The force field parameterization fitting procedure for this system is described in depth in the Supporting Information of Ref.⁴ The final set of parameters is given in Table S2. Force field energies are compared with *ab initio* energies in Figure S3. The RMS difference between force field and *ab initio* energies is 0.73 kJ mol⁻¹ for all configurations where the *ab initio* energies are less than 0.



Figure S3. Interaction energies calculated with the modified-Morse/Lennard-Jones plus Coulomb potential described in Ref.⁴ (lines) compared with energies calculated with MP2/6-311+G** (circles) for H₂ interaction with Li alkoxide benzene. In addition to the approaches shown here, we also sampled configurations with different H₂ configurations, such as "head on" adsorption to Li, for a total of 225 quantum chemical energies. Reproduced with permission from Getman *et al.*⁴ Copyright 2011 American Chemical Society.

S2 H₂ Adsorption Simulations

Classical simulations were performed with our in-house, multipurpose code RASPA.¹¹ Positions of framework atoms were taken from crystallography¹². Positions of Li (doped IRMOF-8) and

Li alkoxide groups (functionalized IRMOF-8) are not available from crystallography. These were taken from the *ab initio* calculations discussed above. The H₂ molecule was assumed to be rigid with a bond length of 0.741 Å. H₂/framework atom interactions were using the potentials and parameters described above. H₂ adsorption isotherms were calculated using grand canonical Monte Carlo (GCMC) simulations. In these simulations, 100,000 cycles were performed to equilibrate the positions of H₂ in the systems, and an additional 60,000 cycles were performed to compute ensemble averages. In each cycle, an average of *N* moves were performed, where *N* is the number of molecules in the system (which fluctuates in GCMC). GCMC moves used were translation, rotation, insertion, deletion, and reinsertion into a new position within the framework.

The isosteric heats of adsorption were computed from the GCMC simulations using the expression¹³

$$Q_{\rm st} = RT - \left(\frac{\partial \langle \mathcal{V} \rangle \langle N \rangle}{\partial \langle N \rangle}\right)_{T,V}$$
(Eq. S6)

S3 Comparison of Simulated and Experimental Isotherms for CH₄ and H₂ Adsorption in

MOFs

Table S3. Potential models used in GCMC simulations from the literature for CH ₄ adsorption in
MOFs and COFs and the agreement of the calculated isotherms with experiment

Literature	MOFs	T P _{max}	CH ₄ model	MOF model	Expt Data	Agreement with expt. ^a
Düren et al. ¹⁴	IRMOF-1 IRMOF-6	298 K 40 bar	spherical LJ ¹⁵	DREIDING	16	good
Gallo and Glossman- Mitnik ¹⁷	IRMOF-1	298 K 80 bar	spherical LJ ¹⁵	UFF	16	good
Garberoglio et al. ¹⁸	HKUST-1	295 K 1 bar	spherical LJ ¹⁹	DREIDING or UFF	20	slightly +
Yang and Zhong ²¹	IRMOF-1	298 K 40 bar	spherical LJ ²²	refitted portions of OPLS-AA	16	good
Yang and Zhong ²³	HKUST-1	295 K 1 bar	spherical LJ ²²	refitted portions of OPLS-AA	20	good
Wang ²⁴	Cu(SiF ₆)(bpy) ₂ Cu(GeF ₆)(bpy) ₂ CPL-2	298 K 35 bar	spherical LJ ²²	refitted portions of OPLS-AA	24-26	good
Lan et al. ²⁵	COF-102	298 K 100 bar	spherical LJ ¹⁵	CH ₄ -MOF FFs from ab initio MP2 calculations	26	slightly +
Mendoza-Cortes et al. ²⁷	COF-5 COF-8	298 K 100 bar	CH ₄ -CH ₄ FFs from ab initio MP2 calculations	CH ₄ -MOF FFs from ab initio MP2 calculations	27	good

^a+: simulations overestimated experiments

Literature	MOFs	T P _{max}	H ₂ model ^a + Quantum diffraction effect ^b	del ^a ntum MOF model tion ^b		Agreement with expt. ^c
Frost et al. ²⁸	IRMOF-1 IRMOF-8	77 K 1 bar	spherical LJ ²⁹	DREIDING	12	- (low P) + (high P)
	IRMOF-18	77 K 1 bar	spherical LJ ²⁹	DREIDING	12	+
Frost et al. ³⁰	IRMOF-1	298 K 120 bar	spherical LJ ²⁹	DREIDING +UFF(Cu)	31-33	good (low P) - (high P)
	HKUST-1	298 K 120 bar	spherical LJ ²⁹	DREIDING +UFF(Cu)	31	good (low P) – (high P)
Ryan et al. ³	IRMOF-1	77 K 298 K 120 bar	spherical LJ ²⁹	DREIDING	34	good
Gallo and Glossman- Mitnik ¹⁷	IRMOF-1 IRMOF-11 MOF-74	298 K 80~100 bar	spherical LJ	UFF	35	good
Yang and Zhong ³⁶	IRMOF-1 IRMOF-18	77 K 1 bar	two-site LJ	refitted portions of OPLS-AA	12	good
Jung et al. ³⁷	IRMOF-1 IRMOF-18	77 K 1 bar	two-site LJ ³⁶	refitted portions of UFF	12,38	good
Jung et al. ³⁹	IRMOF-9	77 K 1 bar	two-site-LJ ³⁶	modified UFF ³⁷	40	+
	IRMOF-11	77 K 1 bar	two-site-LJ ³⁶	modified UFF ³⁷	12	good
	IRMOF-13	77 K 1 bar	two-site-LJ ³⁶	modified UFF ³⁷	40	slightly –
Sagara et al.41	IRMOF-1	78 K 1 bar	modified three- site (DL)	modified UFF	12	+
	IRMOF-1	298 K 50 bar	three- site	UFF	42,43	_
Yang and Zhong ⁴⁴	MOF-505	77 K 1 bar	three- site $(DL)^5$	Refitted portions of OPLS-AA	45	good
Gaberoglio et al. ¹⁸	Manganese formate	78 K 1 bar	three- site UFF or $(DL)^5$ DREIDING		46	_
Gaberoglio et al. ¹⁸	IRMOF-1	77 K 1 bar	spherical LJ (Buch) ⁴⁷	UFF	12	good
			spherical LJ (Buch) ⁴⁷ + PIMC	UFF	12	good
			three- site (DL) ⁵	UFF	12	+
Gaberoglio et al. ¹⁸	IRMOF-8	77 K 1 bar	spherical LJ (Buch) ⁴⁷	UFF	12	– (low P)
			spherical LJ	UFF	12	- (low P)

 Table S4. Potential models used in GCMC simulations from the literature for H₂ adsorption in MOFs and the agreement of the calculated isotherms with experiment

			$(Buch)^{47}$ + PIMC			
Gaberoglio et al. ¹⁸	IRMOF-1	298 K 95 bar	spherical LJ (Buch) ⁴⁷	UFF	42	_
			three- site $(DL)^5$	UFF	42	_
	Cu-MMOM	298 K 45 bar	spherical LJ (Buch) ⁴⁷	UFF	43	_
Liu et al. ⁴⁸	HKUST-1	77 K 50 bar	spherical LJ (Buch) ⁴⁷	UFF	48	- (low P) slightly + (high P)
			spherical LJ (Buch) ⁴⁷ + FH	UFF	48	(low P) slightly – (high P)
	HKUST-1	87 K 50 bar	spherical LJ $(Buch)^{47} + FH$	UFF	48	_
	HKUST-1	175 K 298 K 50 bar	spherical LJ (Buch) ⁴⁷	UFF	48	slightly – (175 K) good (298 K)
Liu et al. ⁴⁹	Zn(bdc)(ted)	77 K 50 bar	spherical LJ $(Buch)^{47} + FH$	UFF	49	slightly + (low P)
			spherical LJ $(Buch)^{47}$ + FH	DREIDING	49	good
	Zn(bdc)(ted)	298 K 50 bar	spherical LJ (Buch) ⁴⁷	UFF	49	slightly +
			spherical LJ (Buch) ⁴⁷	DREIDING	49	good
Han et al. ⁵⁰	IRMOF-1	77 K 1 bar	FFs from ab initio second-order MP2 calculations		12	good

^aThree-site model: three point charges with single LJ core

^bFH: Feynman-Hibbs effective potential method⁵¹; PIMC: Path Integral Monte Carlo method⁵²; if nothing is indicated, the simulations did not account for quantum diffraction effects

^c+: simulations overestimated experiments; - : simulations underestimated experiments

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