

Supporting information for
Si₃AlP: a new promising material for solar cell absorber

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Su-Huai Wei[‡]

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I. Lattice vectors and atomic positions of the *Cc*-Si₃AlP phase

The unrelaxed lattice vectors of primitive cell for *Cc*- Si₃AlP are

$$\mathbf{a}_1 = (1.00 \quad -0.50 \quad 0.50)$$

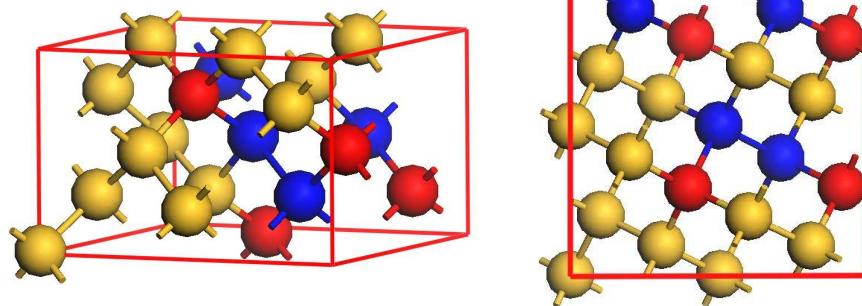
$$\mathbf{a}_2 = (1.00 \quad 0.50 \quad 0.50)$$

$$\mathbf{a}_3 = (-1.50 \quad 0.00 \quad 0.50)$$

The unrelaxed atomic positions within the unit cell (in direct lattice coordinates) are

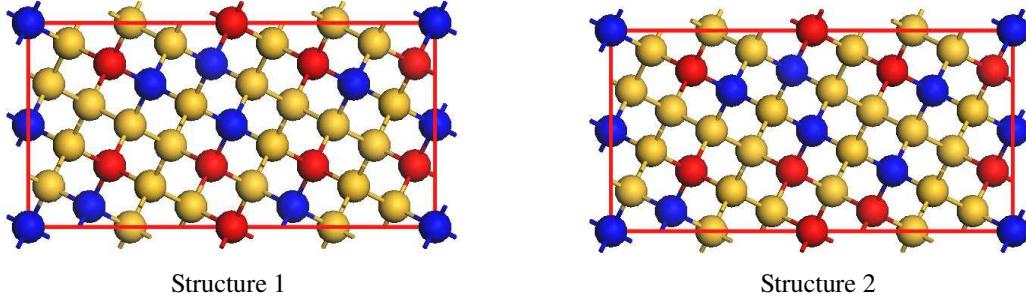
Si	0.00	0.00	0.00
Si	0.40	0.40	0.20
Si	0.55	0.05	0.90
Si	0.75	0.25	0.50
Si	0.15	0.65	0.70
Si	0.80	0.80	0.40
Al	0.95	0.45	0.10
Al	0.20	0.20	0.60
P	0.60	0.60	0.80
P	0.35	0.85	0.30

II. Structure with Al-Al bond.



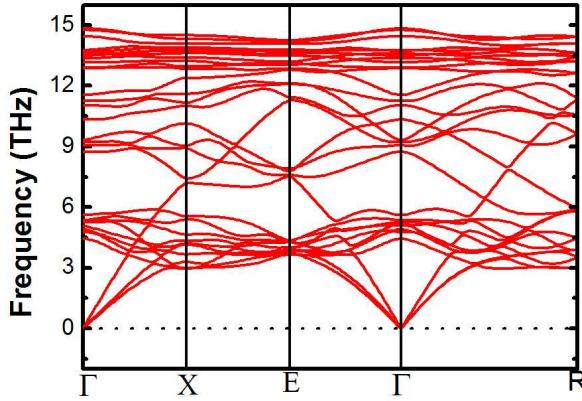
The red balls are P, blue balls are Al and yellow balls are Si. We find that formation of Al-Al bond is strongly energetically unfavorable.

III. Si₃AlP with 40-atoms structures for the test



This figure shows two 40-atoms structures randomly generated for our tests. The first one has an energy of 25 meV/atom higher than the *Cc* structure and the second one has an energy of 42 meV/atom higher.

IV. Phonon spectrum of $Cc\text{-Si}_3\text{AlP}$



We calculated the phonon spectrum of $Cc\text{-Si}_3\text{AlP}$ using PHONOPY package. As we can see, there are no imaginary phonon modes, suggesting the dynamic stability of this structure.

V. Bader analysis of charge on each atomic sites for $Cc\text{-Si}_3\text{AlP}$

Through the Bader analysis, we find that for $Cc\text{-Si}_3\text{AlP}$ the net charge on Si site is about -0.09, the net charge state on Al site is about 1.72, and the net charge on P site is about -1.45.

VI. LDA calculated lattice parameters of Si_3AlP , Si, and AlP in the 20-atoms cell:

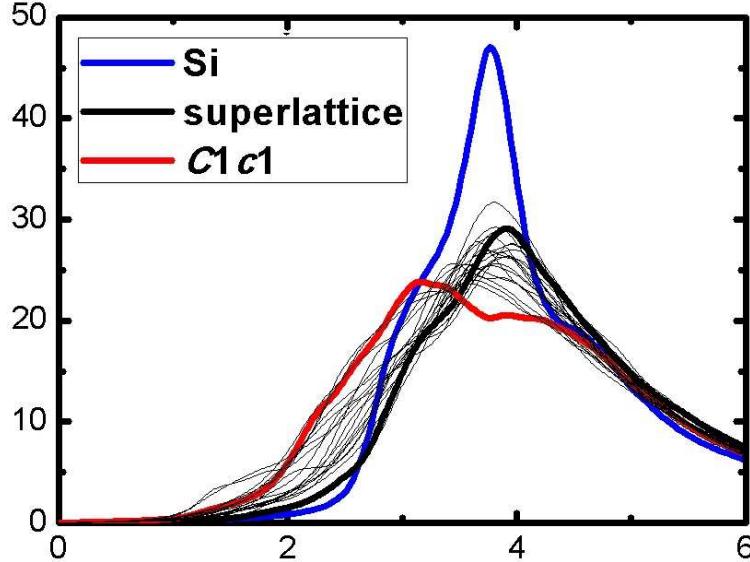
structure	a	b	c	α	β	γ	Lattice mismatch to Si
Si	8.5422	8.5422	5.4026	90	90	90	0
AlP	8.5864	8.5864	5.4351	90	90	90	0.52%
$Cc\text{-Si}_3\text{AlP}$	8.5505	8.5806	5.4642	90	90	89.6606	0.45%
$P1_1\text{-Si}_3\text{AlP}$	8.5706	8.5705	5.4524	90.0000	90.0000	90.0000	0.33%
$P1_2\text{-Si}_3\text{AlP}$	8.5699	8.5699	5.4519	90.0003	89.9999	90.0000	0.32%
$P1_3\text{-Si}_3\text{AlP}$	8.5521	8.5810	5.4622	89.9815	90.1029	90.0978	0.45%
$P1_4\text{-Si}_3\text{AlP}$	8.5650	8.5555	5.4724	90.0001	90.0000	90.2449	0.27%
$P1_5\text{-Si}_3\text{AlP}$	8.5621	8.5928	5.4494	90.0001	90.0001	90.3840	0.59%

Since the Si_3AlP cell is grown on the Si (001) surface, we only considered **a** vector and **b** vector to calculate the lattice mismatch between Si_3AlP and Si. The larger one of **a** and **b** (we use **a** in the following formula) is used and the lattice mismatch is calculated according to:

$$\text{Lattice mismatch} = (\mathbf{a}_{\text{Si}_3\text{AlP}} \cdot \mathbf{a}_{\text{Si}}) / \mathbf{a}_{\text{Si}}$$

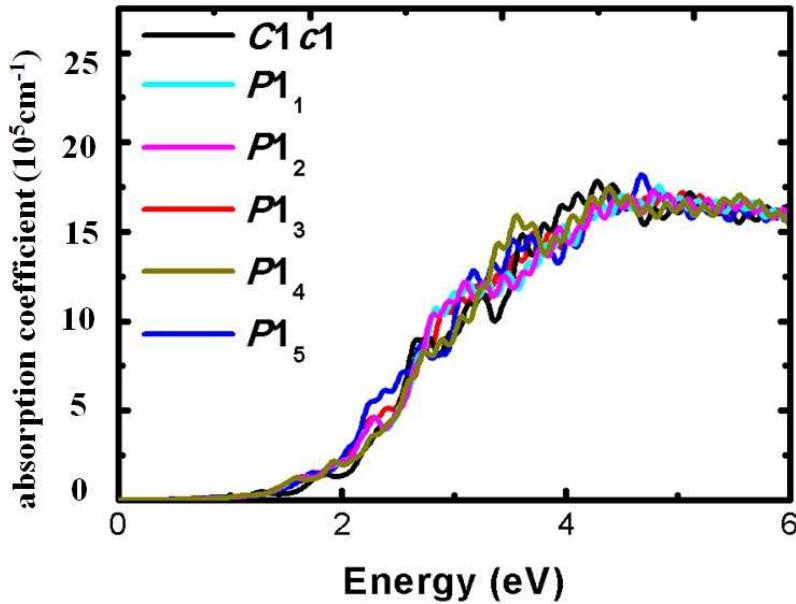
As we can see, the lattice mismatch between Si_3AlP and Si is very small and almost negligible. Besides, the lattice is only a little distorted and can be neglected.

VII. Calculated imaginary dielectric function of the 10-atom structures that are more energetically stable than the *Cc*-structure.



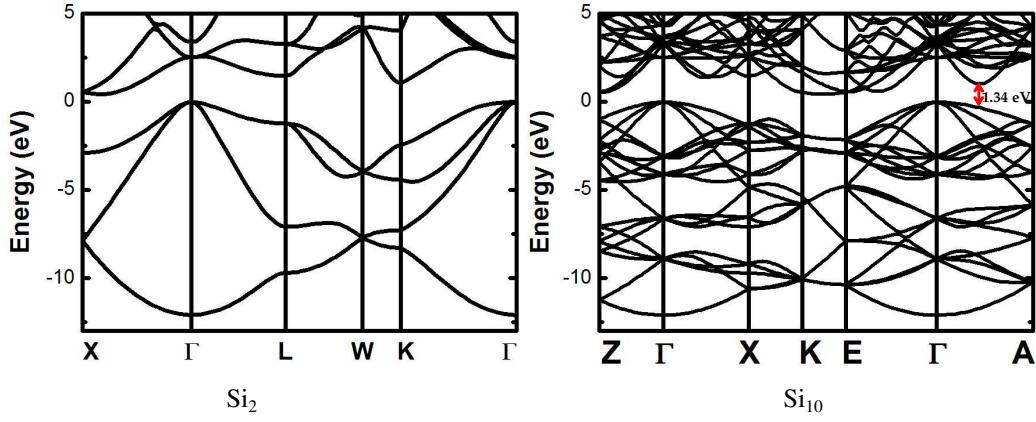
The LDA calculated optical spectrum of these structures show that they generally have their values in between the superlattice structure and *Cc*-structure. Some of them also show metallic behavior, which is not plotted here. We find that *Cc*-structure gives the best optical properties for solar cell applications.

VIII. Absorption coefficients of other structure with $[\text{AlPSi}_3]$ arrangements.



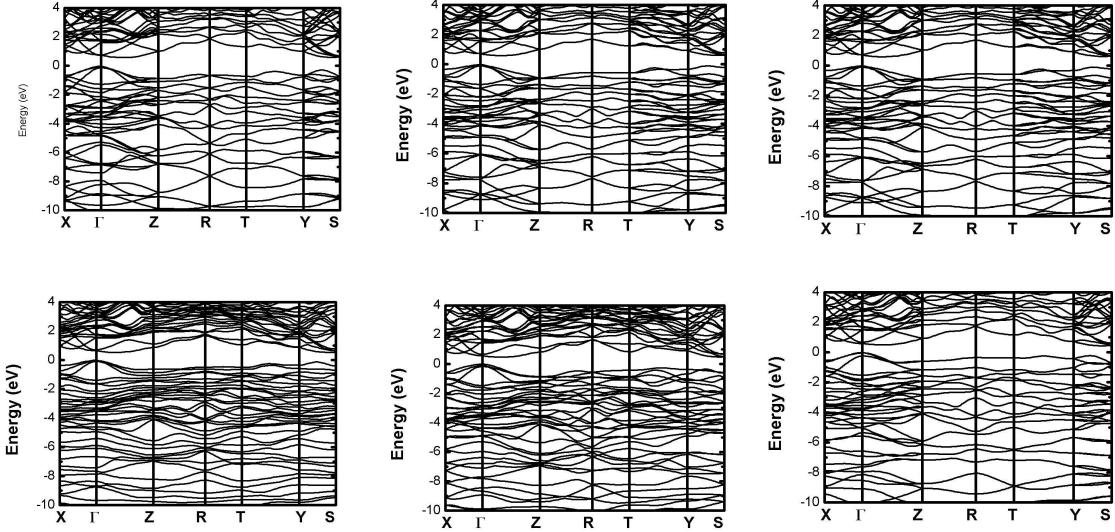
As we can see, the absorption spectrums are almost the same for all the six structures. This indicates that the optical properties of these materials are not sensitive to the atomic arrangements in the unit cell once the local structural motif is preserved, which provides convenience for the synthesis.

IX. band structures of Si in its 2-atoms primitive cell and 10-atoms *Cc* cell



In the Si 2-atoms primitive cell, the LDA calculated minimum direct band gap is at Γ point and has a value of 2.53 eV; in the Si 10-atoms *Cc* cell, the minimum pseudo direct band gap appears to be at a point along Γ -A line and has a value of 1.34 eV, as shown in the figure. But the transition at this point is not allowed in pure Si, because the CBM state and VBM state are folded from two different k-points of the original 2-atom Si cell. After AIP is mixed, the transition becomes allowed due to the reduction of the symmetry.

XI. Band structures of the six 20-atoms structures (same order as in Figure 2)



As we can see, the band structures of the structures with different arrangements of the basic unit [Si₃AlP] are almost the same, indicating that as long as the basic motif is the same, the band gaps are not sensitive to the atomic arrangements, which offers convenience for the experiment. This can be easily understood since the band folding relationships and the local chemical environment are the same.

XII. Structural and energy information of relaxed Cc, superlattice, and P1₁ to P1₅ structures

1. Cc primitive cell and superlattice structure

	Cc (primitive)	superlattice																																																																																																						
Relaxed energy (Hartree/atom)	-0.2085146	-0.2139194																																																																																																						
Relaxed atomic positions	<table> <thead> <tr> <th>Si</th><th>Al</th><th>P</th></tr> </thead> <tbody> <tr> <td>5.402570000000000</td><td></td><td></td></tr> <tr> <td>1.0066964650592214</td><td>-0.5056785178695579</td><td>0.5010704755550753</td></tr> <tr> <td>1.0066964650592214</td><td>0.5056785178695579</td><td>0.5010704755550753</td></tr> <tr> <td>-1.5083734565946452</td><td>0.0000000000000000</td><td>0.4977307071733382</td></tr> <tr> <td>6</td><td>2</td><td>2</td></tr> <tr> <td>Direct</td><td></td><td></td></tr> <tr> <td>0.4101825316708377</td><td>0.4135639303793042</td><td>0.1981428140487651</td></tr> <tr> <td>0.7802397504655261</td><td>0.8463083241881790</td><td>0.4113648059737045</td></tr> <tr> <td>0.0228493080534307</td><td>0.9959696302532564</td><td>0.0097126586674179</td></tr> <tr> <td>0.1435639303793081</td><td>0.6710825316708338</td><td>0.6981428140487651</td></tr> <tr> <td>0.5763083241881830</td><td>0.0502397504655221</td><td>0.9113648059737045</td></tr> <tr> <td>0.7259696302532532</td><td>0.2928493080534338</td><td>0.5097126586674179</td></tr> <tr> <td>0.9359647647685421</td><td>0.4757842370491900</td><td>0.1019143128771276</td></tr> <tr> <td>0.2057842370491869</td><td>0.2059647647685452</td><td>0.6019143128771276</td></tr> <tr> <td>0.5770849615558973</td><td>0.6311525616158420</td><td>0.7988654084329738</td></tr> <tr> <td>0.3611525616158389</td><td>0.8470849615559004</td><td>0.2988654084329738</td></tr> </tbody></table>	Si	Al	P	5.402570000000000			1.0066964650592214	-0.5056785178695579	0.5010704755550753	1.0066964650592214	0.5056785178695579	0.5010704755550753	-1.5083734565946452	0.0000000000000000	0.4977307071733382	6	2	2	Direct			0.4101825316708377	0.4135639303793042	0.1981428140487651	0.7802397504655261	0.8463083241881790	0.4113648059737045	0.0228493080534307	0.9959696302532564	0.0097126586674179	0.1435639303793081	0.6710825316708338	0.6981428140487651	0.5763083241881830	0.0502397504655221	0.9113648059737045	0.7259696302532532	0.2928493080534338	0.5097126586674179	0.9359647647685421	0.4757842370491900	0.1019143128771276	0.2057842370491869	0.2059647647685452	0.6019143128771276	0.5770849615558973	0.6311525616158420	0.7988654084329738	0.3611525616158389	0.8470849615559004	0.2988654084329738	<table> <thead> <tr> <th>Si</th><th>Al</th><th>P</th></tr> </thead> <tbody> <tr> <td>1.000000000000000</td><td></td><td></td></tr> <tr> <td>-2.7071592416448516</td><td>2.7071592416448516</td><td>0.000000000000000</td></tr> <tr> <td>-2.7071592416448516</td><td>0.000000000000000</td><td>-2.7071592416448516</td></tr> <tr> <td>-10.8673537493067336</td><td>-8.1601945076618829</td><td>8.1601945076618829</td></tr> <tr> <td>6</td><td>2</td><td>2</td></tr> <tr> <td>Direct</td><td></td><td></td></tr> <tr> <td>0.9998218661326490</td><td>0.9998218661326490</td><td>0.0005344016020530</td></tr> <tr> <td>0.3495632199660363</td><td>0.3495632199640326</td><td>0.9513103401049108</td></tr> <tr> <td>0.3992785070982379</td><td>0.3992785070982379</td><td>0.8021644787052793</td></tr> <tr> <td>0.7490693728910145</td><td>0.749069372890108</td><td>0.7527918813299621</td></tr> <tr> <td>0.7987655530861133</td><td>0.7987655530861133</td><td>0.6037033407416459</td></tr> <tr> <td>0.1486292090524302</td><td>0.1486292090524302</td><td>0.5541123728396968</td></tr> <tr> <td>0.2005487832709392</td><td>0.2005487832709392</td><td>0.3983536501871754</td></tr> <tr> <td>0.6009087854322814</td><td>0.6009087854322814</td><td>0.1972736437031770</td></tr> <tr> <td>0.5516465447234467</td><td>0.5516465447234467</td><td>0.3450603658266616</td></tr> <tr> <td>0.9517681583478534</td><td>0.9517681583478534</td><td>0.1446955249594311</td></tr> </tbody> </table>	Si	Al	P	1.000000000000000			-2.7071592416448516	2.7071592416448516	0.000000000000000	-2.7071592416448516	0.000000000000000	-2.7071592416448516	-10.8673537493067336	-8.1601945076618829	8.1601945076618829	6	2	2	Direct			0.9998218661326490	0.9998218661326490	0.0005344016020530	0.3495632199660363	0.3495632199640326	0.9513103401049108	0.3992785070982379	0.3992785070982379	0.8021644787052793	0.7490693728910145	0.749069372890108	0.7527918813299621	0.7987655530861133	0.7987655530861133	0.6037033407416459	0.1486292090524302	0.1486292090524302	0.5541123728396968	0.2005487832709392	0.2005487832709392	0.3983536501871754	0.6009087854322814	0.6009087854322814	0.1972736437031770	0.5516465447234467	0.5516465447234467	0.3450603658266616	0.9517681583478534	0.9517681583478534	0.1446955249594311
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2. Cc conventional cell and P1₁ structures

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</tbody></table>	Si	Al	P	1.000000000000000			8.5807165173050759	0.0255343741861376	0.0000009634865445	0.0254911639914040	8.5500079180329731	0.0000008188459229	0.000000055325108	-0.0000007246842219	5.4643111510166333	12	4	4	Direct			0.5005707868013829	0.0078693727597141	0.2270022389641397	0.8077937760848073	0.1019205515663870	0.7537697665498655	0.0005536077957302	0.0078759368342105	0.0229910734994192	0.3078080044008544	0.1019206393888084	0.4962155109438271	0.098322216781413	0.204066995841423	0.2734642069327151	0.000566669960434	0.5078896037063458	0.7270251760437532	0.3078027606397029	0.6019100787883858	0.2537831286416363	0.5983116537676523	0.2040710992120438	0.976522442472735	0.5005838873675330	0.5078832070198587	0.5229814931475119	0.8077883067030456	0.6019101530047735	0.9962315994759692	0.5983189166308165	0.7040832980382987	0.7734715939588597	0.0983293707316122	0.7040790935745704	0.4765416752528751	0.2025398505936806	0.4004781825816082	0.9901077443191824	0.7025524710485200	0.4004593484696670	0.2598994544337430	0.2025383393917650	0.9004973499157174	0.7598962481135985	0.7025509021885341	0.90047875432511496	0.4900965092676515	0.4038588213389573	0.2987555744222945	0.7330087814397643	0.9038750920812575	0.2987472121887222	0.5169928413426845	0.9038654291742603	0.7987325896439472	0.2330212475383888	0.4038491435857026	0.7987409589753369	0.0169772856616817	<table> <thead> <tr> <th>Si</th><th>Al</th><th>P</th></tr> </thead> <tbody> <tr> <td>1.000000000000000</td><td></td><td></td></tr> <tr> <td>8.5705502882058404</td><td>0.000000000000000</td><td>0.000000000000000</td></tr> <tr> <td>0.000000000000000</td><td>8.5705137887544875</td><td>0.000000000000000</td></tr> <tr> <td>0.000000000000000</td><td>0.000000000000000</td><td>5.4524291404590155</td></tr> <tr> <td>12</td><td>4</td><td>4</td></tr> <tr> <td>Direct</td><td></td><td></td></tr> <tr> <td>0.504700320886025</td><td>0.004306102448683</td><td>0.2177494791508678</td></tr> <tr> <td>0.8005387323545818</td><td>0.1009289995811002</td><td>0.7177470564310866</td></tr> <tr> <td>0.1008556511421688</td><td>0.210205841977606</td><td>0.264314439997653</td></tr> <tr> <td>0.0042106356703684</td><td>0.5028066886749301</td><td>0.7521228082050300</td></tr> <tr> <td>0.3010288551244500</td><td>0.6024318867731751</td><td>0.2521238090060436</td></tr> <tr> <td>0.6043069297741823</td><td>0.2005342137422730</td><td>0.9677450683612250</td></tr> <tr> <td>0.4950319397189418</td><td>0.5008590326903715</td><td>0.51433223548427</td></tr> <tr> <td>0.810209501071013</td><td>0.6043779239604987</td><td>0.0143326605814025</td></tr> <tr> <td>0.1028065367826869</td><td>0.7010295861397893</td><td>0.502121894872738</td></tr> <tr> <td>0.2024303788680299</td><td>0.4042082416552262</td><td>0.0021257314974790</td></tr> <tr> <td>0.2043785326207299</td><td>0.8950317824505802</td><td>0.7643307459631430</td></tr> <tr> <td>0.7009319858394178</td><td>0.9046996264860283</td><td>0.4677462101334129</td></tr> <tr> <td>0.3096184524512111</td><td>0.1006953845337435</td><td>0.5070067186998344</td></tr> <tr> <td>0.7006954917202890</td><td>0.3956153007837528</td><td>0.2570072494776525</td></tr> <tr> <td>0.9956172556926575</td><td>0.0045412963224436</td><td>0.0070078559798503</td></tr> <tr> <td>0.6045447240494610</td><td>0.7096214213803620</td><td>0.7570115368448924</td></tr> <tr> <td>0.3983483647658161</td><td>0.3071430161734341</td><td>0.7587898441741459</td></tr> <tr> <td>0.9071428993493242</td><td>0.3068885180730234</td><td>0.5087907684318722</td></tr> <tr> <td>0.9068888147074787</td><td>0.7980951475436768</td><td>0.2587887932694741</td></tr> <tr> <td>0.3980939974085160</td><td>0.7983499888129444</td><td>0.0087878067597202</td></tr> </tbody> </table>	Si	Al	P	1.000000000000000			8.5705502882058404	0.000000000000000	0.000000000000000	0.000000000000000	8.5705137887544875	0.000000000000000	0.000000000000000	0.000000000000000	5.4524291404590155	12	4	4	Direct			0.504700320886025	0.004306102448683	0.2177494791508678	0.8005387323545818	0.1009289995811002	0.7177470564310866	0.1008556511421688	0.210205841977606	0.264314439997653	0.0042106356703684	0.5028066886749301	0.7521228082050300	0.3010288551244500	0.6024318867731751	0.2521238090060436	0.6043069297741823	0.2005342137422730	0.9677450683612250	0.4950319397189418	0.5008590326903715	0.51433223548427	0.810209501071013	0.6043779239604987	0.0143326605814025	0.1028065367826869	0.7010295861397893	0.502121894872738	0.2024303788680299	0.4042082416552262	0.0021257314974790	0.2043785326207299	0.8950317824505802	0.7643307459631430	0.7009319858394178	0.9046996264860283	0.4677462101334129	0.3096184524512111	0.1006953845337435	0.5070067186998344	0.7006954917202890	0.3956153007837528	0.2570072494776525	0.9956172556926575	0.0045412963224436	0.0070078559798503	0.6045447240494610	0.7096214213803620	0.7570115368448924	0.3983483647658161	0.3071430161734341	0.7587898441741459	0.9071428993493242	0.3068885180730234	0.5087907684318722	0.9068888147074787	0.7980951475436768	0.2587887932694741	0.3980939974085160	0.7983499888129444	0.0087878067597202
Si	Al	P																																																																																																																																																																		
1.000000000000000																																																																																																																																																																				
8.5807165173050759	0.0255343741861376	0.0000009634865445																																																																																																																																																																		
0.0254911639914040	8.5500079180329731	0.0000008188459229																																																																																																																																																																		
0.000000055325108	-0.0000007246842219	5.4643111510166333																																																																																																																																																																		
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0.5005707868013829	0.0078693727597141	0.2270022389641397																																																																																																																																																																		
0.8077937760848073	0.1019205515663870	0.7537697665498655																																																																																																																																																																		
0.0005536077957302	0.0078759368342105	0.0229910734994192																																																																																																																																																																		
0.3078080044008544	0.1019206393888084	0.4962155109438271																																																																																																																																																																		
0.098322216781413	0.204066995841423	0.2734642069327151																																																																																																																																																																		
0.000566669960434	0.5078896037063458	0.7270251760437532																																																																																																																																																																		
0.3078027606397029	0.6019100787883858	0.2537831286416363																																																																																																																																																																		
0.5983116537676523	0.2040710992120438	0.976522442472735																																																																																																																																																																		
0.5005838873675330	0.5078832070198587	0.5229814931475119																																																																																																																																																																		
0.8077883067030456	0.6019101530047735	0.9962315994759692																																																																																																																																																																		
0.5983189166308165	0.7040832980382987	0.7734715939588597																																																																																																																																																																		
0.0983293707316122	0.7040790935745704	0.4765416752528751																																																																																																																																																																		
0.2025398505936806	0.4004781825816082	0.9901077443191824																																																																																																																																																																		
0.7025524710485200	0.4004593484696670	0.2598994544337430																																																																																																																																																																		
0.2025383393917650	0.9004973499157174	0.7598962481135985																																																																																																																																																																		
0.7025509021885341	0.90047875432511496	0.4900965092676515																																																																																																																																																																		
0.4038588213389573	0.2987555744222945	0.7330087814397643																																																																																																																																																																		
0.9038750920812575	0.2987472121887222	0.5169928413426845																																																																																																																																																																		
0.9038654291742603	0.7987325896439472	0.2330212475383888																																																																																																																																																																		
0.4038491435857026	0.7987409589753369	0.0169772856616817																																																																																																																																																																		
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8.5705502882058404	0.000000000000000	0.000000000000000																																																																																																																																																																		
0.000000000000000	8.5705137887544875	0.000000000000000																																																																																																																																																																		
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0.504700320886025	0.004306102448683	0.2177494791508678																																																																																																																																																																		
0.8005387323545818	0.1009289995811002	0.7177470564310866																																																																																																																																																																		
0.1008556511421688	0.210205841977606	0.264314439997653																																																																																																																																																																		
0.0042106356703684	0.5028066886749301	0.7521228082050300																																																																																																																																																																		
0.3010288551244500	0.6024318867731751	0.2521238090060436																																																																																																																																																																		
0.6043069297741823	0.2005342137422730	0.9677450683612250																																																																																																																																																																		
0.4950319397189418	0.5008590326903715	0.51433223548427																																																																																																																																																																		
0.810209501071013	0.6043779239604987	0.0143326605814025																																																																																																																																																																		
0.1028065367826869	0.7010295861397893	0.502121894872738																																																																																																																																																																		
0.2024303788680299	0.4042082416552262	0.0021257314974790																																																																																																																																																																		
0.2043785326207299	0.8950317824505802	0.7643307459631430																																																																																																																																																																		
0.7009319858394178	0.9046996264860283	0.4677462101334129																																																																																																																																																																		
0.3096184524512111	0.1006953845337435	0.5070067186998344																																																																																																																																																																		
0.7006954917202890	0.3956153007837528	0.2570072494776525																																																																																																																																																																		
0.9956172556926575	0.0045412963224436	0.0070078559798503																																																																																																																																																																		
0.6045447240494610	0.7096214213803620	0.7570115368448924																																																																																																																																																																		
0.3983483647658161	0.3071430161734341	0.7587898441741459																																																																																																																																																																		
0.9071428993493242	0.3068885180730234	0.5087907684318722																																																																																																																																																																		
0.9068888147074787	0.7980951475436768	0.2587887932694741																																																																																																																																																																		
0.3980939974085160	0.7983499888129444	0.0087878067597202																																																																																																																																																																		

3. P1₂ and P1₃ structures

	P1 ₂			P1 ₃		
Relaxed energy (Hartree/atom)	-0.2079946			-0.2079178		
	Si	Al	P	Si	Al	P
	1.000000000000000			1.000000000000000		
Relaxed atomic positions	8.5699235688503812	-0.0000027129412904	-0.0000218882567377	8.5521075435636202	-0.0073050614262203	0.0013765880652257
	-0.0000004264601075	8.569899392449473	0.0000101643987910	-0.0073200796149963	8.5809881294659061	-0.0077117961866391
	-0.0000141340954601	0.0000065143236870	5.4518813519390648	0.0008783877560087	-0.0049045290241338	5.4622336213478873
	12	4	4	12	4	4
	Direct			Direct		
	0.4949617731733227	0.0008366213903486	0.2357215428743515	0.5041929951383537	0.0038296632150931	0.2240012079435232
	0.8102647673086594	0.1044123653550955	0.7357315681288625	0.8008307457738226	0.1045694927408789	0.7159187696111218
	0.0042090345714598	0.0027932519888481	0.9979057167772822	0.1013118962615422	0.2081531151691962	0.2593730929456655
	0.3010371628031905	0.1024549368669625	0.4979156839639742	0.3037637058849469	0.6023884118229716	0.2486361075621986
	0.1027974916430949	0.2010351948232909	0.2479108391709062	0.608334782849845	0.2036928012311279	0.9759301303677717
	0.5047089442869463	0.5042834867436241	0.5321595988242862	0.5006952299783478	0.4990054836915334	0.512220290340307
	0.8005183994591505	0.6009403387710961	0.0321571473419340	0.8045800987106588	0.6034298933126578	0.0329854664672524
	0.6042814438072455	0.7005195189172966	0.2871554805188455	0.104492855799371	0.7038916972297571	0.4958878305034489
	0.1008504522534324	0.7102670401476630	0.4857272511733939	0.2058233094203175	0.4030627265479296	0.9993522146345768
	0.2044039863825446	0.3949682287784952	0.9857253832806663	0.6974599180576249	0.397009932428187	0.2560379093200638
	0.7009427140934363	0.4047062444283966	0.2821607783291711	0.2059047858808754	0.8943558703213910	0.761036497792337
	0.2024568800302404	0.9042074765642454	0.7479064675606111	0.6996552567805239	0.9037394206479803	0.4783316312186017
	0.6045190665743334	0.2095590230949043	0.9930281678303885	0.3075394304682959	0.1023551316452327	0.5133162187245546
	0.995686950344060	0.0545342668210679	0.7430279461723472	0.9978698497997911	0.5014720429048793	0.7477443312570742
	0.7007014850024831	0.8956842488188101	0.4930281369177223	0.9973974651616686	0.0034227171439198	0.9991888214464879
	0.3095645909727054	0.6006936711274449	0.2430221056011916	0.6071368303873470	0.7062335433941129	0.7634350227208486
	0.3980908879971850	0.2983557411457980	0.7411778711768306	0.404825471540377	0.3065155588727535	0.7631990442906087
	0.9068869794770720	0.2980973906915025	0.4911729384931319	0.8969368610570640	0.303487208963221	0.4878913880136508
	0.9071506906238298	0.8068818476439859	0.241784232694885	0.9041900453347935	0.8024495156508635	0.2611960287064790
	0.3983462986052757	0.8071391058811486	0.9911869525944326	0.3994385906656390	0.7993051612185980	0.0040480011628290

4. P1₄ and P1₅ structures

	P1 ₄			P1 ₅		
Relaxed energy (Hartree/atom)	-0.2078771			-0.2078117		
	Si	Al	P	Si	Al	P
	1.000000000000000			1.000000000000000		
Relaxed atomic positions	8.5649365675647875	-0.0183073675755205	-0.0000070668810263	8.5620383559265107	-0.0287155117232978	-0.0000061640142410
	-0.0182769354634959	8.5554979382128984	0.0000019485983528	-0.0287703419188870	8.5927309108795100	-0.0000063899577137
	-0.0000044681883739	0.0000019284959099	5.4723752122369405	-0.0000043780965054	-0.0000037946536270	5.4494432379146547
	12	4	4	12	4	4
	Direct			Direct		
	0.5001277870641161	0.0033944185607240	0.2351998884610822	0.5037067764947878	0.9997848273045591	0.2229900426230955
	0.0001239116733842	0.0033966334530930	0.0147983902490409	0.8015302702918419	0.1054557876868003	0.7229939740970579
	0.1031829674758242	0.2053420196352675	0.2616033572177869	0.0993405316449198	0.2081035030567833	0.2576978776029151
	0.999790456264929	0.4993382474924033	0.7446355133858162	0.6091797192601049	0.2044251065431339	0.98868065916014217
	0.3037282268219386	0.5988149609823950	0.243500659638881	0.5037143422193964	0.4998053298993810	0.5269862313711045
	0.6031793191489285	0.2053431184435368	0.9883963662573478	0.8015227005263696	0.6054300518014557	0.0269937574179551
	0.4997940644124341	0.4993377542970308	0.5053666740501157	0.6091844013914738	0.7044382353644781	0.7631856573107285
	0.8037242749227431	0.5988143907167469	0.0066500812828778	0.0993691022917886	0.7081478135426593	0.4923182742391958
	0.2012636727514661	0.400318008553506	0.9895928752666521	0.2058804389212767	0.3970883762698705	0.9923012333152883
	0.701264993646379	0.4003156031670017	0.2604094698930268	0.6960480674448277	0.4007941867629654	0.2631796652523448
	0.2028236350119954	0.9012316158001070	0.7887746375350346	0.2059028004128649	0.8971412984452911	0.7577091502149855
	0.7028258870244954	0.9012258441186773	0.4612226319358328	0.6960504648109094	0.9008134870727176	0.4868184279947485
	0.3057440261407081	0.0995044657458806	0.5238522095357144	0.3056317569934563	0.1033106929514318	0.5053504360203718
	0.8057371154968180	0.0995047815251056	0.7261439950596298	0.9996374740770051	0.5019627911832956	0.7446455444553948
	0.1028542644153987	0.7092544367359324	0.5031792212466897	0.9996032981857255	0.0019241532705436	0.0053627463591610
	0.6028491308171411	0.7092566527061592	0.7468247492900133	0.3056026996279329	0.6032713133065215	0.2446401268979912
	0.4044474838318806	0.3081528833221370	0.7586772110766589	0.4083217687729359	0.3017783559801615	0.764576245020042
	0.9044512533457763	0.3081507592978738	0.491323528457030	0.8969302782701902	0.3034925768011902	0.4854175810493189
	0.9022354038738101	0.8008350413296910	0.2419400356185548	0.8969158563820159	0.8034560314117627	0.2645998520326529
	0.4022312307799893	0.8008383638148970	0.0080592928285128	0.4083072519801547	0.8017459913449869	0.9854265656422427