

Supplemental Figures

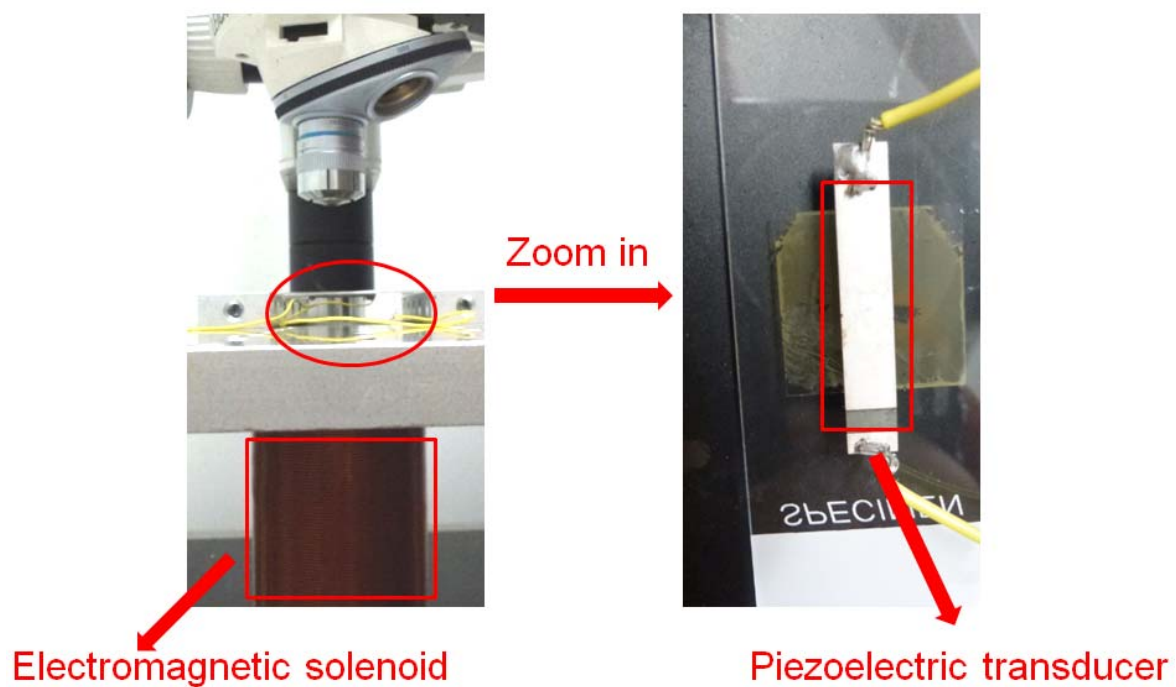


Figure S1. A photograph of our experimental setup: the sample was observed under an upright microscope, with the solenoid underneath the sample. For the experiments with acoustic concentration, a piezoelectric transducer is attached to the back of the slide to generate acoustic field.

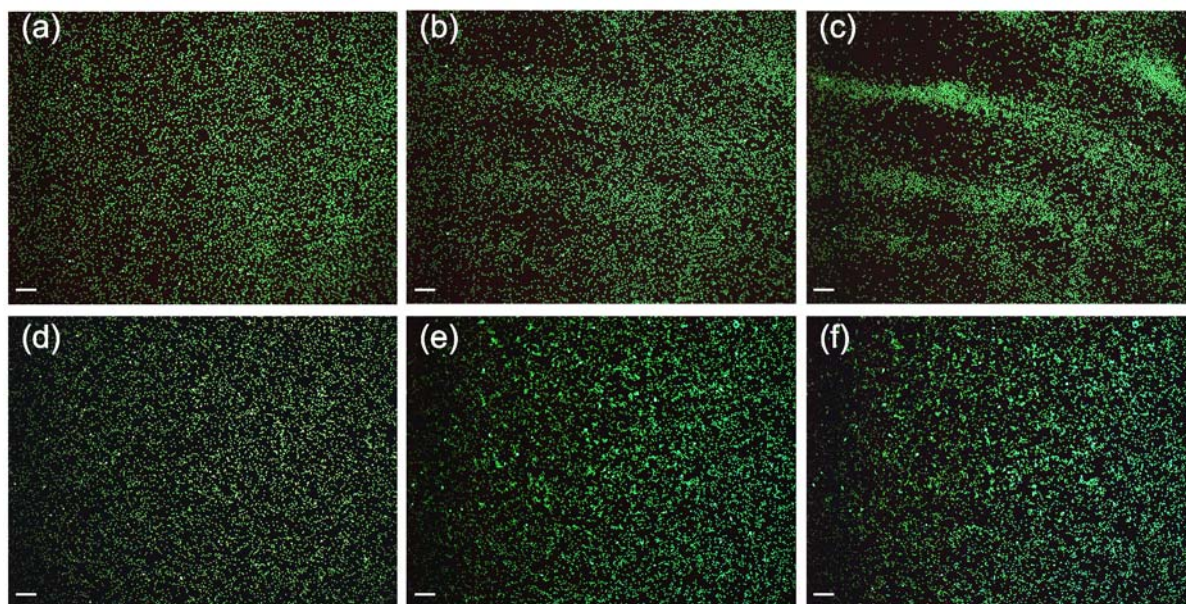


Figure S2. Illustration of acoustic concentration effects. A 1V, 2.93 MHz sine wave was used to drive PZT to generate acoustic field and concentrate the particles in local regions for: (a) 1 hour; (b) 2 hours; (c) 3 hours. Control experiments without acoustic field were conducted for: (a) 1 hour; (b) 2 hours; (c) 3 hours. The particles begin to locally concentrate in certain regions after applying the acoustic field for 2 hours. All the scale bars are 50 μ m.

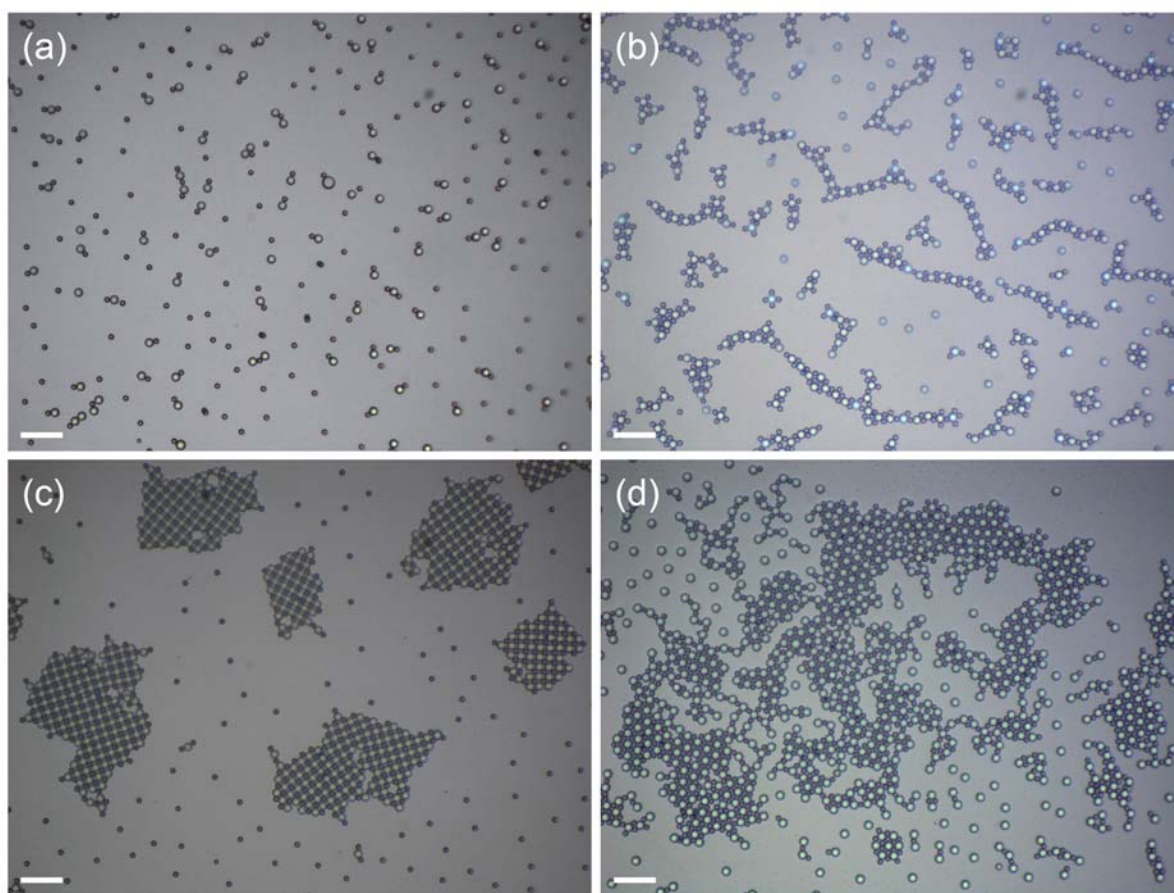
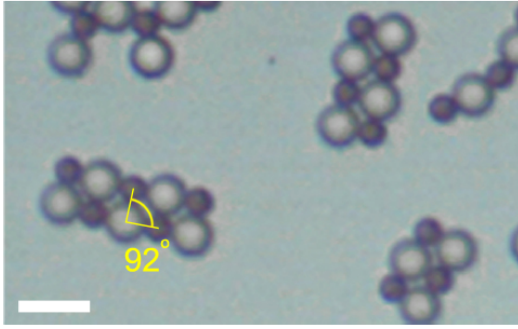


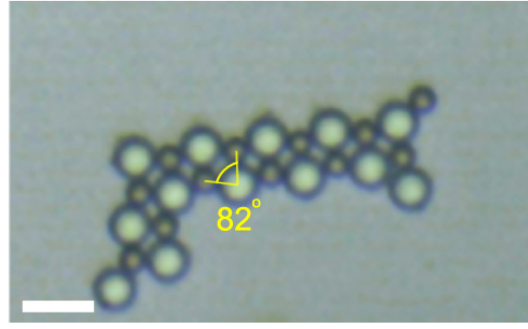
Figure S3. Wide field images of examples for different structures are illustrated: (a) MN ring at $\phi=0.1\%$; (b) M_2N chains at $\phi=0.8\%$; (c) square lattice at $\phi=0.5\%$; (d) honeycomb lattice at $\phi=0.8\%$. Although there are sometimes multiple different types of structures present within each image, we chose to plot the dominant phase in the phase diagram. The scale bars are $25\mu\text{m}$.

(a)



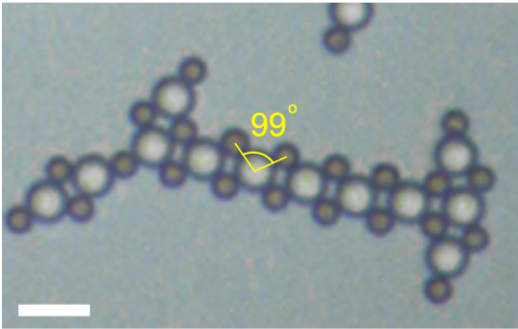
$$\phi = 0.4\%$$

(b)



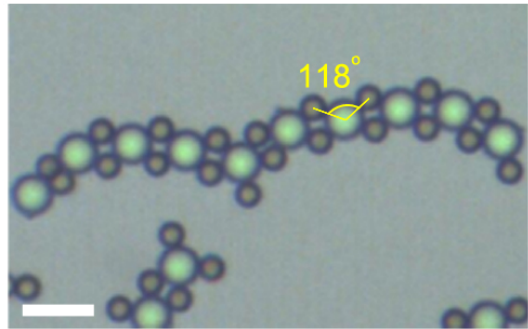
$$\phi = 0.7\%$$

(c)



$$\phi = 0.5\%$$

(d)



$$\phi = 0.8\%$$

Figure S4. In the 2-particle system, the particle sized difference introduces variations for the 1D chain structures in their way of packing. At slightly different ferrofluid concentrations, two different M_2N_2 chain structures (a)(b), and two different M_2N structures (c)(d) can be observed. And the difference between (a) and (b), (c) and (d) can be observed through measurement angle measurement. The scale bars are $10\mu\text{m}$.

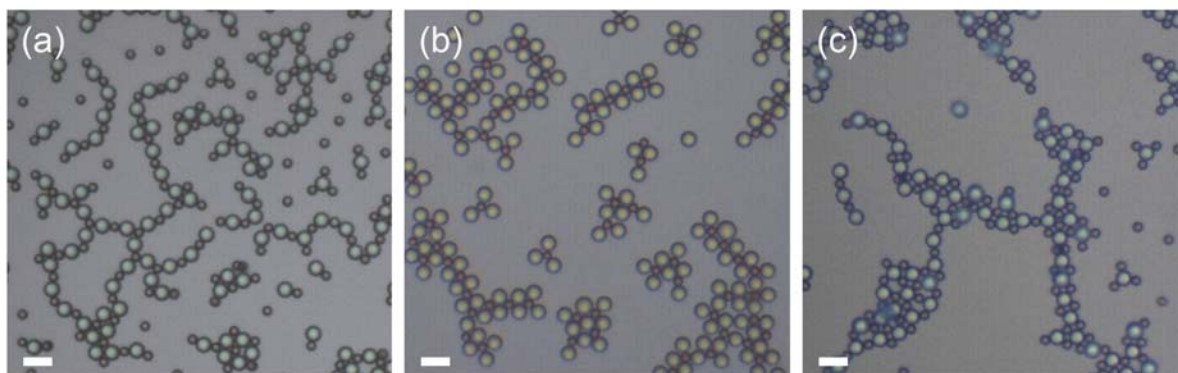


Figure S5. For certain ferrofluid concentrations at the border between two different equilibrium phases, a percolating network of chains was sometimes observed, such as those shown in (a) a network of MN chains at $\varphi=0.2\%$; (b) a network of MN_2 chains at $\varphi=0.3\%$; (c) a network of MN_2 chains at $\varphi=0.5\%$. The scale bars are $10\mu\text{m}$.