## SUPPORTING INFORMATION

## SI. Bulk formation energy calculations

## SI1. Case of anionic doping

This section gives more details about the thermodynamic equations of the formation energies of the various anionic S-doping configurations and reported in the main text.

For reaction (2), the formation energies per Ti of the various anionic S-doped systems are defined by:

$$E_{form}(2) = \frac{1}{n} \left[ E_{tot}(doped) - E_{tot}(pure) + 2(p - m)\mu_H + m.\mu_{H_2O} - p.\mu_{H_2S} \right]$$
 (SI1.1)

Using  $\mu_i = E_i + \Delta \mu_i$ , equation (SI1.1) leads to the following expression:

$$E_{form}(2) = \frac{1}{n} [E_{tot}(doped) - E_{tot}(pure) + (p - m)(E_{H_2} + 2\Delta\mu_H) + m(E_{H_2O} + \Delta\mu_{H_2O}) - p(E_{H_2S} + \Delta\mu_{H_2S})]$$
(SI1.2)

$$E_{form}(2) = \frac{1}{n} [E_{tot}(doped) - E_{tot}(pure) + (p - m)(E_{H_2} + 2\Delta\mu_H) + m(E_{H_2} + \frac{1}{2}E_{O_2} - \Delta E_1 + \Delta\mu_{H_2O}) - p(E_{H_2} + \frac{1}{2}E_{S_2} - \Delta E_2 + \Delta\mu_{H_2S})]$$
(SI1.3)

As a consequence, we obtain the following equations given in the main text

$$E_{form}(2) = E_{form}^{0K}(1) + \frac{1}{n} \left[ m(\Delta \mu_{H_2O} - 2\Delta \mu_H - \Delta E_1) - p(\Delta \mu_{H_2S} - 2\Delta \mu_H - \Delta E_2) \right]$$
 (7)

with

$$\Delta E_1 = E_{H_2} + \frac{1}{2} E_{O_2} - E_{H_2O} \tag{8}$$

$$\Delta E_2 = \frac{1}{2} E_{S_2} + E_{H_2} - E_{H_2S} \tag{9}$$

 $\Delta E_1 = +2.89$  eV and  $\Delta E_2 = +1.25$  eV represent the electronic energy variations for the chemical reactions:  $H_2O \to H_2 + \frac{1}{2}O_2$  and  $H_2S \to \frac{1}{2}S_2 + H_2$  respectively.

Formally, this equation can be rewritten as follows:

$$E_{form}(2) = E_{form}^{0K}(1) + \frac{1}{n} [m(\Delta \mu_O' - \Delta E_1) - p(\Delta \mu_S' - \Delta E_2)]$$
(10)

where

$$\Delta \mu_{H,S} = \Delta \mu_S' + 2\Delta \mu_H \tag{11}$$

$$\Delta \mu_{H,O} = \Delta \mu_O' + 2\Delta \mu_H \tag{12}$$

For reaction (3), the formation energies are expressed as follows:

$$E_{form}(3) = \frac{1}{n} \left[ E_{tot}(doped) - E_{tot}(pure) + p.\mu_{CO(NH_2)_2} - p.\mu_{CS(NH_2)_2} - (p - m)\mu_O \right]$$
 (SI1.4)

Using  $\mu_i = E_i + \Delta \mu_i$ , equation (SI1.4) leads to the following expression:

$$E_{form}(3) = \frac{1}{n} [E_{tot}(doped) - E_{tot}(pure) + p(E_{CO(NH_2)_2} + \Delta\mu_{CO(NH_2)_2}) - p(E_{CS(NH_2)_2} + \Delta\mu_{CS(NH_2)_2}) - (p - m)(\frac{1}{2}E_{O_2} + \Delta\mu_O)]$$

(SI1.5)

$$\begin{split} E_{form}(3) &= \frac{1}{n} [E_{tot}(doped) - E_{tot}(pure) + p(\Delta E_3 - \frac{1}{2}E_{S_2} + \frac{1}{2}E_{O_2}) + p(\Delta \mu_{CO(NH_2)_2} - \Delta \mu_{CS(NH_2)_2}) \\ &- (p - m)(\frac{1}{2}E_{O_2} + \Delta \mu_O)] \end{split}$$

(SI1.6)

As a consequence, we obtain the following equations given in the main text

$$E_{form}(3) = E_{form}^{0K}(1) + \frac{1}{n} [(m-p)\Delta\mu_O + p(\Delta E_3 + \Delta\mu_{CO(NH_2)_2} - \Delta\mu_{CS(NH_2)_2})]$$
 (13)

with

$$\Delta E_3 = E_{CO(NH_2)_2} - E_{CS(NH_2)_2} + \frac{1}{2}E_{S_2} - \frac{1}{2}E_{O_2}$$
(14)

 $\Delta E_3$  =-1.89 eV represents the electronic energy variation for the chemical reaction:

$$CS(NH_2)_2 + \frac{1}{2}O_2 \to CO(NH_2)_2 + \frac{1}{2}S_2$$
.

## SI2. Case of anionic doping

We give in this section more details about the thermodynamic equations of the formation energies of the various cationic S-doping configurations and reported in the main text.

For reaction (15), the formation energies per Ti are calculated through the following expression:

$$E_{form}(15) = -\frac{1}{n}E_{tot}(pure) + \frac{1}{(n-k)}[E_{tot}(doped) - kE_{O_2} - \frac{p}{2}E_{S_2} - 2k.\Delta\mu_O - p.\Delta\mu_S]$$
 (SI2.1)

As a consequence, we obtain the following equations given in the main text:

$$E_{form}(15) = E_{form}^{0K}(15) - \frac{1}{(n-k)} [2k \cdot \Delta \mu_O + p \cdot \Delta \mu_S]$$
(18)

where

$$E_{form}^{0K}(15) = -\frac{1}{n}E_{tot}(pure) + \frac{1}{(n-k)}[E_{tot}(doped) - kE_{O_2} - \frac{p}{2}E_{S_2}]$$

For reaction (16), the formation energies per Ti are defined by:

$$E_{form}(16) = -\frac{1}{n}E_{tot}(pure) + \frac{1}{(n-k)}[E_{tot}(doped) + pE_{H_2} - kE_{O_2} - pE_{H_2S} + 2p.\Delta\mu_H - 2k.\Delta\mu_O - p.\Delta\mu_{H_2S}]$$
(SI2.2)

As a consequence, we obtain the following equation also given in the main text:

$$E_{form}(16) = E_{form}^{0K}(15) - \frac{1}{(n-k)} [2k \cdot \Delta \mu_O + p(\Delta \mu_S' - \Delta E_2)]$$
(19)

For reaction (17), the formation energies per Ti are expressed as follows:

$$E_{form}(17) = -\frac{1}{n}E_{tot}(pure) + \frac{1}{(n-k)}[E_{tot}(doped) + pE_{CO(NH_2)_2} - pE_{CS(NH_2)_2} - \frac{(2k+p)}{2}E_{O_2} + p\Delta\mu_{CO(NH_2)_2} - p\Delta\mu_{CS(NH_2)_2} - (2k+p)\Delta\mu_{O}]$$
(S12.3)

As a consequence, we obtain the following equation also given in the main text:

$$E_{form}(17) = E_{form}^{0K}(15) - \frac{1}{(n-k)} [(2k+p)\Delta\mu_O - p(\Delta E_3 + \Delta\mu_{CO(NH_2)_2} - \Delta\mu_{CS(NH_2)_2}]$$
 (20)