

**Table S1.** List of relevant equations and related description for **NRHB** model.

Description	Mathematical expression
<p>S1. Phase equilibrium condition on penetrant chemical potential. The expression for chemical potential is given in a general form which is valid for both pure penetrant (<math>\phi_1=1</math>) in the gas phase and for penetrant in the binary polymer mixture.</p>	$\frac{\mu_1^{GAS}}{RT} = \frac{\mu_1^{POL}}{RT}$ <p>where <math display="block">\frac{\mu_1}{RT} = \ln \frac{\phi_1}{\omega_1 r_1} - r_1 \sum_{j=1}^2 \frac{\phi_j l_j}{r_j} + \ln \tilde{\rho} + r_1 (\tilde{v} - 1) \ln(1 - \tilde{\rho}) - \frac{z}{2} r_1 \left[ \tilde{v} - 1 + \frac{q_1}{r_1} \right] \ln \left[ 1 - \tilde{\rho} + \frac{q}{r} \tilde{\rho} \right]</math> <math display="block">+ \frac{z q_1}{2} \left[ \ln \Gamma_{11} + \frac{r_1}{q_1} (\tilde{v} - 1) \ln \Gamma_{00} \right] + r_1 \frac{\tilde{P} \tilde{v}}{\tilde{T}} - \frac{q_1}{\tilde{T}_1} + \frac{\mu_{1,H}}{RT}</math> <p>where</p> <math display="block">\tilde{P} = \frac{P}{P^*}; \quad \tilde{T} = \frac{T}{T^*}; \quad RT^* = P^* v^* = \varepsilon^* \quad \text{with: } \varepsilon^* = \sum_{i=1}^2 \sum_{j=1}^2 \theta_i \theta_j \varepsilon_{ij}^* \quad v^* = 9.75 \text{ cm}^3 / \text{mol}</math> <math display="block">\varepsilon_{12}^* = (1 - k_{12}) \sqrt{\varepsilon_{11}^* \varepsilon_{22}^*}; \quad \text{with } \varepsilon_{ii}^* = \varepsilon_{hi}^* + (T - 298.15) \varepsilon_{s,i}^*</math> <math display="block">\tilde{v} = \frac{V - \sum_i^m \sum_j^n N_{ij} V_{ij}^0}{r N v^*} \quad \text{where } V \text{ is the total volume of the mixture}</math> <math display="block">\tilde{\rho} = 1/\tilde{v}</math> </p>
<p>S2. HB contribution to the expression of chemical potential of penetrant. The expression for the <math>\mu_{1,H}</math> is given in a general form which is valid for both pure penetrant (component 1) in the gas phase and for penetrant in the binary polymer mixture.</p>	$\frac{\mu_{1,H}}{RT} = r_1 v_H - \sum_i^m d_i^1 \ln \left( \frac{v_d^i}{v_{i0}} \right) - \sum_j^n a_j^1 \ln \left( \frac{v_a^j}{v_{0j}} \right)$
<p>S3. Expression of the EOS. The expression for the EOS is given in a general form which is valid for both pure penetrant (<math>\phi_1=1</math>) in the</p>	$\tilde{P} + \tilde{T} \left[ \ln(1 - \tilde{\rho}) - \tilde{\rho} \left( \sum_{i=1}^2 \phi_i \frac{l_i}{r_i} - v_H \right) - \frac{z}{2} \ln \left( 1 - \tilde{\rho} + \frac{q}{r} \tilde{\rho} \right) + \frac{z}{2} \ln \Gamma_{00} \right] = 0$

gas phase and for penetrant in the binary polymer mixture.	
S4. Average number of hydrogen bonds per molecular segment	$v_H = \sum_i^m \sum_j^n v_{ij} = \sum_i^m \sum_j^n \frac{N_{ij}}{rN}$
S5. Expression obtained by minimizing the Gibbs energy as a function of $N_{ij}$ variable.	$\frac{v_{ij}}{v_{i0}v_{0j}} = \tilde{\rho} \exp\left(-\frac{G_{ij}^0}{RT}\right)$ <p>where</p> $G_{ij}^0 = E_{ij}^0 - T \cdot S_{ij}^0 + p \cdot V_{ij}^0$
S6. Expression obtained by minimizing the Gibbs energy as a function of the number of contacts between segment of species $i$ and $j$ (0, 1 and 2 representing, respectively, empty lattice sites, penetrant and polymer)	$\frac{\Gamma_{ii}\Gamma_{jj}}{\Gamma_{ij}^2} = \exp\left(-\frac{\Delta\epsilon_{ij}}{RT}\right)$ <p>where</p> $\Gamma_{ij} = \frac{N_{ij}^{NR}}{N_{ij}^{NR,0}} \quad \text{with } N_{ij}^{NR,0} \text{ representing the effective number of contacts in the compressible lattice between the mers of kind } i \text{ and the mers of kind } j \text{ in the case of random statistics.}$ $\Delta\epsilon_{ij} = \epsilon_{ii} + \epsilon_{jj} - 2(1 - k_{ij})\sqrt{\epsilon_{ii}\epsilon_{jj}} \quad \text{with } \epsilon_{ii} = \epsilon_{ii}^* \frac{2}{z}$
S7. Material balance expression for the non random factors $\Gamma$ s	$\sum_{i=0}^t \theta_i \theta_r \Gamma_{ij} = 1 \quad j = 0, 1, \dots, t$ <p>where</p> $\theta_r = \sum_{i=1}^t \theta_i$ <p>Here <math>t</math> is the number of components, '0' representing empty sites.</p>

S8. Definition of the 'close-packed' specific volume	$v_{sp,i}^* = \frac{1}{\rho_i^*} = v_{sp,0i}^* + (T - 298.15)v_{sp,1i}^*$ <p>where <math>v_{sp,1i}^*</math> is a characteristic parameters for different homologous series and <math>\rho_i^*</math> is the 'close-packed' density of component 'i'.</p>
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**Table S2.** List of relevant equations and related description for **NETGP-NRHB** model.

Description	Mathematical expression
<p>S9. Chemical potential of penetrant according to NRHB theory. Expression A4 still holds also in this case. Moreover, due to the hypothesis of ‘instantaneous’ evolution kinetics for <math>\underline{N}_{ij}</math> and <math>\underline{N}_{rs}^{NR}</math>, also eqs. A5, A6 and A7 hold true.</p>	$\frac{\mu_1^{GAS}}{RT} = \frac{\mu_1^{POL, PE}}{RT}$ <p>where</p> $\begin{aligned} \frac{\mu_1^{GAS}}{RT} = & \ln \frac{\phi_1}{\delta_1 r_1} - r_1 \sum_{j=1}^2 \frac{\phi_j l_j}{r_j} + \ln \tilde{\rho} + r_1 (\tilde{v} - 1) \ln(1 - \tilde{\rho}) - \frac{z}{2} r_1 \left[ \tilde{v} - 1 + \frac{q_1}{r_1} \right] \ln \left[ 1 - \tilde{\rho} + \frac{q}{r} \tilde{\rho} \right] \\ & + \frac{z q_1}{2} \left[ \ln \Gamma_{11} + \frac{r_1}{q_1} (\tilde{v} - 1) \ln \Gamma_{00} \right] + r_1 \frac{\tilde{P} \tilde{v}}{\tilde{T}} - \frac{q_1}{\tilde{T}_1} + \frac{\mu_{1,H}^{GAS}}{RT} \end{aligned}$ $\begin{aligned} \frac{\mu_1^{POL, PE}}{RT} = & \ln \frac{\phi_1}{\delta_1 r_1} - r_1 \sum_{j=1}^2 \frac{\phi_j l_j}{r_j} + \ln \tilde{\rho} + r_1 (\tilde{v} - 1) \ln(1 - \tilde{\rho}) - \frac{z}{2} r_1 \left[ \tilde{v} - 1 + \frac{q_1}{r_1} \right] \ln \left[ 1 - \tilde{\rho} + \frac{q}{r} \tilde{\rho} \right] + \frac{z q_1}{2} \left[ \ln \Gamma_{11} + \frac{r_1}{q_1} (\tilde{v} - \right. \\ & \left. - \frac{q_1}{\tilde{T}_1} + \tilde{T} \left[ \ln(1 - \tilde{\rho}) - \tilde{\rho} \left( \sum_i \phi_i \frac{l_i}{r_i} \right) - \frac{z}{2} \ln \left( 1 - \tilde{\rho} + \frac{q}{r} \tilde{\rho} \right) + \frac{z}{2} \ln \Gamma_{00} \right] \cdot \frac{r x_2 \cdot \frac{\partial \tilde{v}}{\partial x_1} \Big _{P, T, \rho_2, \underline{N}_{ij}, \underline{N}_{rs}^{NR}}}{\tilde{T}} + \frac{\mu_{1,H}^{POL, PE}}{RT} \end{aligned}$

	<p>where</p> $1/\tilde{v} = \tilde{\rho} = \rho_2/(\omega_2 \rho^*)$ <p>according to the hypothesis that <math>V_{ij}^0 = 0 \quad \forall i, j</math> ; <math>\rho^*</math> represents the close-packed density of polymer-penetrant mixture</p>
S10. HB contribution to the expression of chemical potential of penetrant in the gas phase.	$\frac{\mu_{1,H}^{GAS}}{RT} = r_1 v_H - \sum_i^m d_i^1 \ln \left( \frac{v_d^i}{v_{i0}} \right) - \sum_j^m a_j^1 \ln \left( \frac{v_a^j}{v_{0j}} \right)$
S11. HB contribution to the expression of chemical potential of penetrant in the polymer phase	$\frac{\mu_{1,H}^{POL, PE}}{RT} = r_1 v_H - \sum_i^m d_i^1 \ln \left( \frac{v_d^i}{v_{i0}} \right) - \sum_j^n a_j^1 \ln \left( \frac{v_a^j}{v_{0j}} \right) + v_H \left. \frac{\partial \ln \tilde{v}}{\partial x_1} \right _{P, T, \rho_2, \underline{N}_{ij}, \underline{N}_{rs}^{NR}} x_2 r$

**Table S3.** List of relevant symbols and parameters for **NRHB** and **NETGP-NRHB** models, not explicitly defined in the text..

Description	Symbol ( <i>latin letters</i> )	Dimension
Number of proton acceptor groups of kind $j$ present on a molecule of type 1	$a_j^1$	-
Number of proton donor of type $i$ on the molecule of type 1	$d_i^1$	-
Molar internal energy of formation of hydrogen bonding between proton donor group of type $i$ and proton acceptor group of type $j$	$E_{ij}^0$	[J mol <sup>-1</sup> ]
Molar Gibbs energy of formation of hydrogen bonding between proton donor group of type $i$ and proton acceptor group of type $j$	$G_{ij}^0$	[J mol <sup>-1</sup> ]
Mean field lattice fluid binary interactional parameter	$k_{12}$	-
Dimensionless parameter of component $i$ defined in ref. [46]	$l_j$	-
Number of types of proton donors	$m$	-
Number of types of proton acceptors	$n$	-
Number of occupied cells of the lattice in the mixture or in the pure component	$N$	-
Number of hydrogen bondings involving a proton donor of type $i$ and a proton acceptor of type $j$	$N_{ij}$	-
Characteristic pressure of pure components or average characteristic pressure for the mixture	$P^*$	[MPa]
Average number of lattice contacts per molecule in the mixture	$q$	-
Number of lattice contacts per molecule for component 1	$q_1$	-
Average number of cells occupied per molecule in the mixture	$r$	-
Lattice cells occupied by one molecule of component 1 in the mixture or in the pure phase of component 1	$r_1$	-
Lattice cells occupied by one molecule of component 2 in the mixture or in the pure phase of component 2	$r_2$	-
Universal gas constant	$R$	[J K <sup>-1</sup> mol <sup>-1</sup> ]
Molar entropy of formation of hydrogen bonding between the proton donor group of type $i$ and the proton acceptor group of type $j$	$S_{ij}^0$	[J mol <sup>-1</sup> K <sup>-1</sup> ]
Characteristic temperature of pure components or average characteristic temperature for the mixture	$T^*$	[K]

Scaled temperature of the mixture	$\tilde{T}$	-
Scaled temperature of the component 1 in pure phase of component 1 or in the mixture	$\tilde{T}_1$	-
'Close-packed' volume of an elementary cell of the lattice in pure components or in the mixture.	$v^*$	$[\text{cm}^3 \text{mol}^{-1}]$
Temperature independent contribution to 'close-packed' specific volume of the pure component of type 1	$v_{sp,01}^*$	$[\text{cm}^3 \text{g}^{-1}]$
Temperature independent contribution to 'close-packed' specific volume of the pure component of type 2	$v_{sp,02}^*$	$[\text{cm}^3 \text{g}^{-1}]$
Scaled lattice fluid volume of the pure components or of the mixture	$\tilde{v}$	-
Molar volume change upon the formation of hydrogen bonding between proton donor group of type $i$ and proton acceptor group of type $j$	$V_{ij}^0$	$[\text{cm}^3 \text{mol}^{-1}]$
Lattice coordination number	$z$	-
<b>Description</b>	<b>Symbol (Greek letters)</b>	<b>Dimension</b>
Non random factor for the distribution of an empty site around another empty site in the lattice	$\Gamma_{00}$	-
Non random factor for the distribution of a site occupied by component 1 around another site occupied by component 1 in the lattice	$\Gamma_{11}$	-
Number of configurations available to a molecule of component 1 in the 'close-packed' state.	$\delta_1$	-
Lattice fluid interaction energy per mole of contact $i$ - $i$	$\varepsilon_{ii}$	$[\text{J mol}^{-1}]$
Average lattice fluid intersegmental interaction energy per mole of average segment in the polymer-water mixture	$\varepsilon^*$	$[\text{J/mol}]$
Enthalpic contribution to lattice fluid interaction energy per mole of segment of component 1	$\varepsilon_{h1}^*$	$[\text{J/mol}]$
Entropic contribution to lattice fluid interaction energy per mole of segment of component 1	$\varepsilon_{s1}^*$	$[\text{J mol}^{-1} \text{K}^{-1}]$
Enthalpic contribution to lattice fluid interaction energy per mole of segment of component 2	$\varepsilon_{h2}^*$	$[\text{J/mol}]$
Entropic contribution to lattice fluid interaction energy per mole of segment of component 2	$\varepsilon_{s2}^*$	$[\text{J mol}^{-1} \text{K}^{-1}]$
Average lattice fluid interaction energy per mole of segment of one molecule	$\varepsilon_{ii}^*$	$[\text{J mol}^{-1}]$

of component $i$		
Average lattice fluid interaction energy per mole of average segment in the binary $i$ - $j$ mixture	$\varepsilon_{ij}^*$	[J mol <sup>-1</sup> ]
Surface fraction of component $i$	$\theta_i$	-
Sum of surface fraction of the component 1 and 2	$\theta_r$	-
Average number of total hydrogen bonds per molecular segment	$\nu_H$	-
Average number of un-bonded proton donor of type $i$ per molecular segment	$\nu_{i0}$	-
Average number of proton donor of type $i$ per molecular segment	$\nu_d^i$	-
Average number of proton acceptor of type $j$ per molecular segment	$\nu_a^j$	-
Average number of un-bonded proton acceptor of type $j$ per molecular segment	$\nu_{0j}$	-
Average number per molecular segment of hydrogen bonding established between a proton donor of type $i$ and a proton acceptor of type $j$	$\nu_{ij}$	-
‘Close packed’ density of the polymer-penetrant mixture	$\rho^*$	[g cm <sup>-3</sup> ]
‘Close packed’ volumetric fraction of component 1	$\phi_1$	-
‘Close packed’ volumetric fraction of component 2	$\phi_2$	-
Mass fraction of component 2	$\omega_2$	-