Supporting information for:

Optimization across water-energy nexus for integrating heat, power and water for industrial processes coupled with hybrid thermal-membrane desalination

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Steam and water properties

The steam and water properties were estimated via correlations developed by Al-Azri et al. ¹ with some modifications for this study. These equations are shown in Table S1.

Table S1 Correlations for steam and water thermodynamic properties

Equation	Description
$T_{sat} = 117.66 P_{sat}^{0.2219}$	Saturation temperature ^a $(14.7 \le P_{sat} \le 2400 \text{ psia})$ Error = ±0.79%
$T_{sat} = 102.80 P_{sat}^{0.2741}$	Saturation temperature ^a $(1.5 \le P_{sat} \le 14.7 \text{ psia})$ $\text{Error} = \pm 1.76\%$
$s_{sat}^f = 1.6308 \times 10^{-3} T_{sat} - 3.0838 \times 10^{-2}$	Saturated water entropy ^a $(1.5 \le P_{sat} \le 14.7 \text{ psia})$ Error = $\pm 0.87\%$
$s_{sat}^{v} = -3.9857 \times 10^{-9} T_{sat}^{3} + 5.4089 \times 10^{-6} T_{sat}^{2} - 3.3698 \times 10^{-3} T_{sat} + 2.2658$	Saturated steam entropy ^a $(1.5 \le P_{sat} \le 2400 \text{ psia})$ $Error = \pm 0.37\%$
$s^{v} = s_{sat}^{v} + 0.46883 - 0.46883 \exp\left(-k_{T}\Delta T_{sat}\right)$ $k_{T} = 1.3845 \times 10^{-2} \left(\frac{T_{sat}}{1000}\right)^{2} - 9.8258 \times 10^{-3} \left(\frac{T_{sat}}{1000}\right)$	Entropy of steam ^a $14.7 \text{ psia} < P < 1500 \text{ psia}$ $T_{\text{sat}} \le T \le 1300 ^{\text{o}}\text{F}$ $\text{Error} = \pm 1.36\%$
$+3.1462 \times 10^{-3}$ $\Delta T_{sat} = T - T_{sat}$	
$H_{sat}^f = 4.2433 \times 10^{-5} T_{sat}^2 + 9.8773 T_{sat} - 31.146$	Saturated water enthalpy ^a $1.5 \text{ psia} < P_{sat} < 14.7 \text{ psia}$ $Error = \pm 0.02\%$

^a This study; ^b Adopted from work by Al-Azri et al. ¹

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Table S1 Correlations for steam and water thermodynamic properties(*Continued*)

Equations	Descriptions
$H_{sat}^f = 4.5395 \times 10^{-4} T_{sat}^2 + 0.74207 T_{sat} + 4.8112$	Saturated water enthalpy ^a 14.7 psia $<$ P _{sat} $<$ 1500 psia Error = $\pm 1.26\%$
$H_{sat}^{v} = -2.0449 \times 10^{-4} T_{sat}^{2} + 0.47202 T_{sat} + 1.0595$	Saturated steam enthalpy ^a $1.5 \text{ psia} < P_{\text{sat}} < 14.7 \text{ psia}$ Error = $\pm 0.01\%$
$H^{\nu} = 0.2029T_{sat}(s^{\nu})^{3.647} + 817.35$	Enthalpy steam ^b Error = ±0.66%

Turbine modeling

Table S2 Regression coefficients used in isentropic efficiency equation

	Back Pressure turbines		Condensing turbines	
Coefficient	W^{max}	W^{max}	W^{max}	W^{max}
	<4.1 MMB tu/hr	>4.1 MMBtu/hr	< 5.12 MMBtu/hr	> 5.12 MMBtu/hr
a_o [Btu/hr]	-0.1508	-1.038755556	-0.115877778	-0.062488889
a_1 [Btu/hr- $^{\rm o}$ F]	0.00065	0.003461111	0.000555556	0.000777778
b_o [Btu/hr]	0.961977778	1.111644444	1.195233333	1.166466667
$b_{ m l}$ [Btu/hr- $^{ m o}$ F]	0.000844444	0.000261111	0.000333333	0.000166667

The coefficients are taken from Varbanov et al. ² and Mavromatis and Kokosiss ³ with original values expressed in SI units.

MED process modeling

The general mass and salt component balance equations for all effects, the down condenser and the distillate flashing boxes are given by Equations 50 - 55 and are summarized in

Table S3. In addition, the corresponding energy balances are given by Equations 56 - 64 for all the effects as well as the condenser, distillate flashing boxes and steam ejector. These energy balances are described in more detail by Gabriel et al. ⁴. They represent an alternative approach to modeling the MED-TVC process from the previously utilized specific heat capacity model.

Table S3 Mass and energy balance equations for MED-TVC process

Equations	Descriptions
$F^{ extit{MED}} = \sum_{i \in N_{eff}} F_i^{ extit{MED}}$	Total MED feed flow
$F_i^{MED} = V_i + B_i$	Mass balance on effect 1
$F_i^{MED} + B_{i-1} = V_i + B_i$	Mass balance on effect 2 to N_{eff}
$egin{aligned} egin{aligned} egin{aligned\\ egin{aligned} egi$	Cooling seawater balance on condenser
$M_{feed}^{salt} = M_1^{salt}$	Salt balance on effect 1
$M_{feed}^{salt} + M_{i-1}^{salt} = M_{i}^{salt}$	Salt balance on effect 2 to $N_{\it eff}$
$Q_{i}^{EVAP} + M_{feed}H_{feed} + \frac{Q^{PRE}}{N_{eff}} = M_{feed,i}^{stm}H_{i}^{v} + M_{feed,i}^{brine}H_{i}^{brine}$	Energy balance on effect evaporator
$Q_i^{EVAP} = Q_i^{vap} + Q_i^{sens}$	Energy distribution of effect evaporator
$Q_i^{vap} = M_{feed,i}^{stm} H_i^{v}$	eneer evaporator
$M_{feed,i-1}^{brine}H_{feed,i-1}^{brine}+M_{BF,i-1}^{brine}H_{BF,i-1}^{brine}=M_{BF,i}^{brine}H_{BF,i}^{brine}+M_{BF,i}^{stm}H_{BF}^{v'}$	Energy balance on brine flashing (BF)
$m{M}_{brine}^{MED} = m{M}_{BF,N_{eff}}^{brine}$	MED brine flow
$D_{i-1}H_{i-1}^{f"} + M_i^c H_{i-1}^c = M_{pot,i}^{stm} H_i^{v"} + M_{pot,i}^{water} H_i^{f"}$	Distillate (D) flashing pot balance
$M_{pot,i}^{water} = M_{DS,i}^{water} + M_{BFW,i} + D_i$	Mass balance on flash pot outflow (W)
$m{M}_{perm}^{MED} = m{D}_{N-1} + ig(m{V}_{N_{eff}} + m{M}_{pot,N_{eff}-1}^{stm} ig) - m{D} m{r}$	MED permeate flow
$S_{mot} \cdot H_{mot}^{v} + Dr \cdot H_{N_{eff}}^{v} + \sum_{i=1}^{N} M_{DS,i}^{water} H_{i}^{f''} = M_{DS}^{stm} H_{DS}^{v}$	De-superheater balance
$+M_{DS}^{c}H_{DS}^{f}$	

Heat transfer area calculations

The heat transfer coefficient, logarithmic mean temperature difference and corresponding area for each effect is calculated using equations given in Table S4.

Table S4 Equations for calculating the heat transfer area, logarithmic mean temperature difference and overall heat transfer coefficients for MED-TVC process

Equations	Descriptions
$A_i^{vap} = rac{Q_i^{vap}}{U_i^{e\!f\!f}ig(T_{i\!-\!1}^c-T_i^{e\!f\!f}ig)}$	Vaporization heat transfer area for each evaporator
$A_{i}^{sens} = \frac{Q_{i}^{sens}}{U_{i}^{eff} (LMTD)_{i}^{sens}}$	Sensible heat transfer area for each evaporator
$A_i^{Total} = A_i^{vap} + A_i^{sens}$	Total heat transfer area for each evaporator
$A_{cond} = \frac{Q_{total}^{COND}}{U_{cond}(LMTD)_{cond}}$	Condenser heat transfer area
$ (LMTD)_{i}^{sens} = \left[\left(T_{i-1}^{c} - T_{f} \right) \cdot \left(T_{i-1}^{c} - T_{i}^{eff} \right) \cdot \left(T_{i-1}^{c} - \frac{T_{f} + T_{i}^{eff}}{2} \right) \right]^{\frac{1}{3}} $	Logarithmic mean temperature difference for each effect based on approximation by Chen et al. ⁵
$(LMTD)_{cond} = \left[\left(T_{N_{eff}}^c - T_f \right) \cdot \left(T_{N_{eff}}^c - T_{sea}^{IN} \right) \cdot \left(T_{N_{eff}}^c - \frac{T_f + T_{sea}^{IN}}{2} \right) \right]^{\frac{1}{3}}$	Logarithmic mean temperature difference for condenser based on approximation by Chen at al. ⁵
$U_i^{eff} = 2.318 \times 10^{-6} (T_i^{eff})^3 - 2.0752 \times 10^{-4} (T_i^{eff})^2$	Overall heat transfer coefficient for
$+1.4056 \times 10^{-3} (T_i^{eff}) + 1.9394$	evaporator
$U_{cond} = -8.026 \times 10^{-8} \left(T_{N_{eff}}^{c} \right)^{3} + 1.825 \times 10^{-4} \left(T_{N}^{c} \right)^{2} $ $+1.537 \times 10^{-4} \left(T_{N_{eff}}^{c} \right) + 1.6175$	Overall heat transfer coefficient for condenser

Overall heat transfer coefficients for evaporator and condenser are presented in their original units as described in work by El-Dessouky et al. ⁶

Effect temperature profile

The temperature profile of the saturated vapor, condensate, brine and distillate are calculated using the equations given in Table S5.

Table S5 Equations for calculating the temperature profile of saturated vaporheat transfer area, logarithmic mean temperature difference and overall heat transfer coefficients for MED-TVC process

Equations	Description	
$\Delta T^{\it eff} = rac{T_1^{\it eff} - T_N^{\it eff}}{N_{\it eff} - 1}$	Temperature difference of all	
$\Delta I = \frac{1}{N_{eff}-1}$	effects	
$T^{DS} = T_1^{\it eff} + \Delta T^{\it eff}$	Temperature of steam from	
	de-superheater	
$T_{i+1}^{\it eff} = T_i^{\it eff} - \Delta T^{\it eff}$	Temperature of effects 2 to	
	$N_{e\!f\!f}$	
$T_f \leq T_N^{c} - \Delta T_{ m min}^{cond}$	Feed seawater temperature	
	constraint	
$T_i^{v} = T_i^{eff} - BPE_i$	Temperature of vapor formed	
	in each effect	
$T_i^{brine} = T_i^{eff} + NEA_i^{brine}$	Temperature of flashed brine	
$T_i^{flash} = T_i^{\ v} + NEA_i^{flash}$	Temperature of flashed	
	distillate	
$BPE = C(X_{sal}^{eff})^2 + D(X_{sal}^{eff})$	Boiling point elevation ⁷ .	
$C = -4.584 \times 10^{-4} (T^{eff})^{2} + 0.2823 (T^{eff}) + 17.95$		
$D = 1.536 \times 10^{-4} (T^{eff})^{2} + 5.267 \times 10^{-2} (T^{eff}) + 6.56$		
$33 \cdot \left(T_{\cdot}^{eff} - T_{\cdot}^{eff}\right)^{0.55}$	Non-equilibrium allowance	
$NEA_{i}^{brine} = \frac{33 \cdot \left(T_{i-1}^{eff} - T_{i}^{eff}\right)^{0.33}}{T_{i}^{v}}$	for flashing brine	
$NEA_{i}^{flash} = \frac{0.33 \cdot \left(T_{i-1}^{c} - T_{i}^{v}\right)}{T^{v}}$	Non-equilibrium allowance	
T_i^{ν}	for flashing distillate	

Reverse Osmosis (RO) unit modeling

Design and operating parameters used in RO network optimization are given in Table S6. The RO unit was modeled using correlations developed by DOW and utilized in their Reverse Osmosis Systems Analysis (ROSA) Filmtec software ⁸. These equations are given in Table S7 along with the mass balances for the RO units.

Table S6 Design and operating parameters for Reverse osmosis network (RON)

Parameter	Unit	Value
Final permeate pressure	psia	14.5
Final reject pressure	psia	14.5
Energy recovery device efficiency	%	80
Pump efficiency	%	80
Seawater feed temperature	°F	77
Maximum pressure drop across RO unit	psia	18.9
Maximum feed pressure to RO unit	psia	1015
Maximum number of modules in one unit		1000
Membrane area per module (6 elements/module)	ft^2	2641

Table S7 General modeling equations for reverse osmosis (RO) unit

Equations	Descriptions
$NM = \frac{M_{feed}^{RO}}{SM \cdot \overline{A}(\overline{\pi}) \cdot TCF \cdot FF \cdot \rho_{f} \cdot \left[P_{f} - \frac{\overline{\Delta P}_{fc}}{2} - P_{p} - \pi_{pf}\right]}$	Number of modules
$\pi_{pf} = \pi_f \Biggl(rac{\overline{C}_{fc}}{C_f} pf + \overline{R} - 1 \Biggr)$	
if $\pi_f \le 2$ $\overline{A}(\overline{\pi}) = 0.125$	Membrane permeability at 25°C
if $25 \le \pi_f \le 200$ $\overline{A}(\pi) = 0.125 - 0.011 \cdot \left(\frac{\pi_f - 25}{35}\right)$	25 C
if $200 \le \pi_f \le 400$ $\overline{A}(\pi) = 0.070 - 0.0001 \cdot (\pi_f - 200)$	
if $T \ge 25$, $TCF = \exp\left[2640 \cdot \left(\frac{1}{298} - \frac{1}{273 + T}\right)\right]$	Temperature correction factor
if $T \le 25$, $TCF = \exp\left[3020 \cdot \left(\frac{1}{298} - \frac{1}{273 + T}\right)\right]$	
$\overline{\Delta P}_{fc} = 0.04 \cdot \left(\frac{M_{feed}^{RO} + M_{brine}^{RO}}{2 \cdot NM \cdot \overline{\rho}} \right)^{2}$	Average concentrate side systempressure drop
$\frac{\overline{C}_{fc}}{C_f} = -\frac{\ln(1-Y)}{Y}$	Approximate log-mean concentrates side to feed concentration ratio for system
$\pi_{feed} = 1.12 \cdot (273 + T) \cdot \sum_{i=1}^{Nc} m_i \qquad i \in Nc$	Feed osmotic pressure
$pf = \exp(0.7Y)$	Concentration polarization factor

$$F^{RO} = M_{perm}^{RO} + M_{brine}^{RO}$$

$$X_{feed}^{RO} F^{RO} = X_{perm}^{RO} M_{perm}^{RO} + X_{brine}^{RO} M_{brine}^{RO}$$

$$X_{feed}^{RO} = \sum_{i \in Nc} X_{feed,i}^{RO}$$

$$X_{perm}^{RO} = \sum_{i \in Nc} X_{perm,i}^{RO}$$

$$X_{brine}^{RO} = \sum_{i \in Nc} X_{brine,i}^{RO}$$

$$Y = \frac{M_{perm}^{RO}}{F^{RO}}$$

$$RO \text{ unit recovery}$$

$$Recovery$$

$$Recovery$$

$$Recovery$$

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$$Recovery$$

The coefficients used to determine air cooling and cooling water tower power consumption rates are given in Table S8. In addition, cooling tower makeup water requirements based on evaporative losses is also calculated using coefficients given in Table S8. These parameters were adopted from previous studies ⁹.

Table S8 Cooling utility power and water requirement factors

Cooling parameter	Value
Air cooler draft fan power [kW/MMBtu/hr]	1.000
Cooling tower daft fan power [kW/MMBtu/hr]	0.092
Cooling tower water makeup [lb/MMBtu/hr]	1.000

NOMENCLATURE

 A_i Heat transfer area in *i*th effect A_{ij} Area for heat transfer between *i*th HPS and *j*th US $\overline{A}(\overline{\pi})$ Membrane permeability B_i Brine flow from *i*th effect BPE Boiling point elevation Cp Specific heat capacity \overline{C}_{fc} Log mean concentrate-side to feed concentration ratio in RO unit

 D_i Distillate mass flowrate from *i*th flash pot

Dr Mass flowrate of entrained steam from final effect

F Flowrate

FF Fouling factor of RO unit

H Enthalpy of stream

LMTD Logarithmic mean temperature difference

 \dot{m} Mass flowrate of stream M Mass flowrate of stream

Number of effects

NEA Non-equilibrium allowance

NM Number of modules

pf Concentration polarization factor

 P_f Feed pressure to RO unit

 P_p Permeate pressure from RO unit

 $\overline{\Delta P}_{fc}$ Average concentrate-side system pressure drop for RO unit

Q Heat exchanger duty

 \overline{R} Average salt rejection of RO unit

S Steam mass flowrate

SM Module surface area of RO unit

 $SUMDT_{i,j}$ Sum of heat exchanger temperature differences

Temperature

TCF Temperature correction factor or RO unit

 ΔT Temperature difference

U Heat transfer coefficient of heat exchanger

 V_i Vapor flow from *i*th effect

X Salt concentration in feed to RO unit

Y Recovery of RO unit

Greek letters

 η Unit efficiency

λ Latent heat of vaporization

Osmotic pressure of seawater feed to RO unit $\pi_{\scriptscriptstyle f}$

Density of fluid ρ

Defined sets

Number of components Nc

Subscripts and superscripts

Actual exit conditions a

BFBrine flashing

BFWBoiler feed water stream

Condensate stream

Condenser cond

DS De-superheater EXExit conditions **Exhaust conditions**

exh

Saturated water conditions

Saturated water conditions in brine flashing Saturated water conditions in distillate flashing

MEDMulti-effect distillation unit

Motive mot

Reverse osmosis unit RO

Salt

Salt in brine flashing s'

Vapor conditions ν

v'Vapor conditions in brine flashing v''Vapor conditions in distillate flashing

Vacuum conditions vac

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