# Dinitrogen Reduction, Sulfur Reduction, and Isoprene Polymerization via Photochemical Activation of Trivalent Bis(cyclopentadienyl) Rare Earth Metal Allyl Complexes 

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## Table of Contents

Crystallographic Details ..... p.S3
Figure S1 (4-Y) ..... p.S3
Table S1 (4-Y) ..... p.S4
Table S2 (4-Y/3-Y) ..... p.S5
Figure S2 (5-Y(tol)) ..... p.S7
Table S3 (5-Y(tol)) ..... p.S8
Figure S3 (5-Lu(tol)) ..... p.S9
Table S4 (5-Lu(tol)) ..... p.S10
Table S5 (5-Y(tol)/5-Lu(tol)) ..... p.S11
Figure S4 (5-Lu(hex)) ..... p.S12
Table S6 (5-Lu(hex)) ..... p.S13
Table S7 (5-Lu(hex)) ..... p.S14
Computational Details ..... p.S15
Figure S5 (molecular orbital plots) ..... p.S16
Table S8 (Electronic excitation summary) ..... p.S17
Elemental Analysis ..... p.S18
References. ..... p.S19

## X-ray Data Collection, Structure Solution and Refinement for 4-Y.

A yellow crystal of approximate dimensions $0.280 \times 0.296 \times 0.329 \mathrm{~mm}$ was mounted on a glass fiber and transferred to a Bruker SMART APEX II diffractometer. The APEX2 ${ }^{1}$ program package was used to determine the unit-cell parameters and for data collection ( $15 \mathrm{sec} / \mathrm{frame}$ scan time for a sphere of diffraction data). The raw frame data was processed using SAINT ${ }^{2}$ and SADABS $^{3}$ to yield the reflection data file. Subsequent calculations were carried out using the SHELXTL ${ }^{4}$ program. There were no systematic absences nor any diffraction symmetry other than the Friedel condition. The centrosymmetric triclinic space group $P \overline{1}$ was assigned and later determined to be correct.

The structure was solved by direct methods and refined on $\mathrm{F}^{2}$ by full-matrix least-squares techniques. The analytical scattering factors ${ }^{5}$ for neutral atoms were used throughout the analysis. Hydrogen atoms were included using a riding model. There were two molecules of the formulaunit present $(Z=4)$.

At convergence, wR2 $=0.0808$ and Goof $=1.071$ for 473 variables refined against 10760 data $(0.73 \AA), \mathrm{R} 1=0.0312$ for those 9129 data with $\mathrm{I}>2.0 \sigma(\mathrm{I})$.


Figure S1. Thermal ellipsoid plot of $\left.\left[\left(\eta^{5}-\mathrm{C}_{5} \mathrm{Me}_{5}\right)_{2} \mathrm{Ln}\left(\eta^{3}-\mathrm{CH}_{2} \mathrm{C}_{\left(\mathrm{CH}_{3}\right)}\right) \mathrm{CH}_{2}\right)\right]$, 4-Y, drawn at the $50 \%$ probability level. There are two independent molecules of $4-\mathrm{Y}$ in the unit cell. The second independent molecule of $\mathbf{4 - Y}$ and hydrogen atoms are omitted for clarity.

Table S1. Crystal data and structure refinement for 4-Y.

| Empirical formula | $\mathrm{C}_{24} \mathrm{H}_{37} \mathrm{Y}$ |
| :---: | :---: |
| Formula weight | 414.44 |
| Temperature | 88(2) K |
| Wavelength | 0.71073 Å |
| Crystal system | Triclinic |
| Space group | $P \overline{1}$ |
| Unit cell dimensions | $a=11.0137(17) \AA$ A $\quad \alpha=67.4577(18)^{\circ}$. |
|  | $\mathrm{b}=14.194(2) \AA \quad \beta=75.8753(19)^{\circ}$. |
|  | $\mathrm{c}=15.681(2) \AA \quad \gamma=84.5088(19)^{\circ}$. |
| Volume | 2195.6(6) $\AA^{3}$ |
| Z | 4 |
| Density (calculated) | $1.254 \mathrm{Mg} / \mathrm{m}^{3}$ |
| Absorption coefficient | $2.660 \mathrm{~mm}^{-1}$ |
| F(000) | 880 |
| Crystal color | yellow |
| Crystal size | $0.329 \times 0.296 \times 0.280 \mathrm{~mm}^{3}$ |
| Theta range for data collection | 1.680 to $29.060^{\circ}$ |
| Index ranges | $-14 \leq h \leq 14,-19 \leq k \leq 18,-21 \leq l \leq 21$ |
| Reflections collected | 27139 |
| Independent reflections | $10760[\mathrm{R}($ int $)=0.0203]$ |
| Completeness to theta $=25.500^{\circ}$ | 99.7 \% |
| Absorption correction | Numerical |
| Max. and min. transmission | 0.6306 and 0.5168 |
| Refinement method | Full-matrix least-squares on $\mathrm{F}^{2}$ |
| Data / restraints / parameters | 10760 / 0 / 473 |
| 2 |  |
| Goodness-of-fit on F | 1.071 |
| Final R indices [ $\mathrm{I}>2 \operatorname{sigma}(\mathrm{I})=9129$ data $]$ | $\mathrm{R} 1=0.0312, \mathrm{wR} 2=0.0772$ |
| R indices (all data, 0.73£) | $\mathrm{R} 1=0.0398, \mathrm{wR} 2=0.0808$ |
| Largest diff. peak and hole | 0.699 and -0.718 e. $\AA^{-3}$ |

Table S2. Selected bond lengths [ $\AA$ ] and angles [ ${ }^{\circ}$ ] for $\left(\mathrm{C}_{5} \mathrm{Me}_{5}\right)_{2} \mathrm{Y}\left(\mathrm{CH}_{2} \mathrm{C}(\mathrm{Me}) \mathrm{CH}_{2}\right), \mathbf{4 - Y}$, and analogous values of $\left(\mathrm{C}_{5} \mathrm{Me}_{5}\right)_{2} \mathrm{Y}\left(\mathrm{CH}_{2} \mathrm{CHCH}_{2}\right), \mathbf{3 - Y},{ }^{15}$ for comparison.

|  | $\mathbf{4 - Y}$ | $\mathbf{3 - Y}$ |  | $\mathbf{4 - Y}$ | $\mathbf{3 - Y}$ |
| :--- | :---: | :--- | :--- | :---: | :---: |
| $\mathrm{Y}(1)-\mathrm{Cnt} 1$ | 2.403 | 2.381 | $\mathrm{Y}(1)-\mathrm{C}(21)$ | $2.562(2)$ | $2.582(2)$ |
| $\mathrm{Y}(1)-\mathrm{Cnt} 2$ | 2.365 | 2.362 | $\mathrm{Y}(1)-\mathrm{C}(22)$ | $2.7021(2)$ | $2.601(2)$ |
| $\mathrm{Y}(1)-\mathrm{C}(1)$ | $2.6855(2)$ | $2.665(2)$ | $\mathrm{Y}(1)-\mathrm{C}(23)$ | $2.570(2)$ | $2.582(2)$ |
| $\mathrm{Y}(1)-\mathrm{C}(2)$ | $2.7075(2)$ | $2.709(2)$ | $\mathrm{C}(21)-\mathrm{C}(22)$ | $1.401(3)$ | $1.392(3)$ |
| $\mathrm{Y}(1)-\mathrm{C}(3)$ | $2.6814(2)$ | $2.670(2)$ | $\mathrm{C}(22)-\mathrm{C}(23)$ | $1.403(3)$ | $1.391(3)$ |
| $\mathrm{Y}(1)-\mathrm{C}(4)$ | $2.6850(2)$ | $2.651(2)$ | $\mathrm{C}(22)-\mathrm{C}(24)$ | $1.514(3)$ |  |
| $\mathrm{Y}(1)-\mathrm{C}(5)$ | $2.6814(2)$ | $2.648(2)$ |  |  |  |
| $\mathrm{Y}(1)-\mathrm{C}(11)$ | $2.6685(2)$ | $2.674(2)$ | $\mathrm{Cnt1-Y(1)-Cnt2}$ | 135.7 | 138.8 |
| $\mathrm{Y}(1)-\mathrm{C}(12)$ | $2.6804(2)$ | $2.673(2)$ | $\mathrm{C}(21)-\mathrm{C}(22)-\mathrm{C}(23)$ | $123.24(2)$ | $125.9(2)$ |
| $\mathrm{Y}(1)-\mathrm{C}(13)$ | $2.6381(2)$ | $2.6378(2)$ | $\mathrm{C}(22)-\mathrm{Y}(1)-\mathrm{C}(2)$ | $92.06(6)$ | $94.33(7)$ |
| $\mathrm{Y}(1)-\mathrm{C}(14)$ | $2.6553(2)$ | $2.640(2)$ | $\mathrm{C}(24)-\mathrm{C}(22)-\mathrm{Y}(1)$ | $132.78(1)$ |  |
| $\mathrm{Y}(1)-\mathrm{C}(15)$ | $2.6285(2)$ | $2.636(2)$ | $\mathrm{C}(23)-\mathrm{C}(22)-\mathrm{C}(24)$ | $118.48(2)$ |  |
| $\mathrm{C}(1)-\mathrm{C}(2)$ | $1.419(3)$ | $1.419(3)$ | $\mathrm{C}(23)-\mathrm{C}(22)-\mathrm{C}(24)$ | $118.00(2)$ |  |
| $\mathrm{C}(2)-\mathrm{C}(3)$ | $1.421(3)$ | $1.414(3)$ |  |  |  |
| $\mathrm{C}(3)-\mathrm{C}(4)$ | $1.416(3)$ | $1.419(3)$ |  |  |  |
| $\mathrm{C}(4)-\mathrm{C}(5)$ | $1.420(3)$ | $1.421(3)$ |  |  |  |
| $\mathrm{C}(1)-\mathrm{C}(5)$ | $1.419(3)$ | $1.418(3)$ |  |  |  |
| $\mathrm{C}(11)-\mathrm{C}(12)$ | $1.416(3)$ | $1.420(3)$ |  |  |  |
| $\mathrm{C}(12)-\mathrm{C}(13)$ | $1.421(3)$ | $1.417(3)$ |  |  |  |
| $\mathrm{C}(13)-\mathrm{C}(14)$ | $1.419(3)$ | $1.416(3)$ |  |  |  |
| $\mathrm{C}(14)-\mathrm{C}(15)$ | $1.418(3)$ | $1.419(3)$ |  |  |  |
| $\mathrm{C}(11)-\mathrm{C}(15)$ | $1.422(3)$ | $1.418(3)$ |  |  |  |
|  |  |  |  |  |  |

Table S 2 shows that the metal- $\mathrm{C}_{5} \mathrm{Me}_{5}$ ring centroid distances and angles of $\mathbf{4}-\mathrm{Y}$ are similar to those of 3-Y. ${ }^{15}$ The Y-C21 and Y-C23 distances to the outer carbons of the allyl ligands in the two structures are similar and fall into a narrow range, 2.562(2) - 2.582(2) $\AA$. The $\mathrm{Y}-\mathrm{C}(22)$ distances to the middle carbon of the allyl ligand differ with the 2.702(2) A distance of the methyl substituted carbon in 4-Y significantly longer than the 2.601(2) $\AA$ in 3-Y.

## X-ray Data Collection, Structure Solution and Refinement for 5-Y(tol).

A colorless crystal of approximate dimensions $0.264 \times 0.072 \times 0.070 \mathrm{~mm}$ was mounted on a glass fiber and transferred to a Bruker SMART APEX II diffractometer. The APEX2 ${ }^{6}$ program package was used to determine the unit-cell parameters and for data collection ( $120 \mathrm{sec} / \mathrm{frame}$ scan time for a sphere of diffraction data). The raw frame data was processed using SAINT ${ }^{7}$ and SADABS ${ }^{8}$ to yield the reflection data file. Subsequent calculations were carried out using the SHELXTL ${ }^{4}$ program. The systematic absences were consistent with the tetragonal space group $P^{\overline{4}}{ }_{21} c$ which was later determined to be correct.

The structure was solved by direct methods and refined on $\mathrm{F}^{2}$ by full-matrix least-squares techniques. The analytical scattering factors ${ }^{5}$ for neutral atoms were used throughout the analysis. The molecule was located on a two-fold rotation axis. Hydrogen atoms were included using a riding model. There were high residuals present in the final difference-Fourier map. It was not possible to determine the nature of the residuals, although it was probable that hexane solvent was present. The SQUEEZE routine in the PLATON ${ }^{9}$ program package was used to account for the electrons in the solvent accessible voids.

At convergence, wR2 $=0.0633$ and Goof $=1.051$ for 205 variables refined against 4554 data $(0.78 \AA), \mathrm{R} 1=0.0286$ for those 4107 data with $\mathrm{I}>2.0 \sigma(\mathrm{I})$. The absolute structure was assigned by refinement of the Flack parameter. ${ }^{10}$


Figure S2. Thermal ellipsoid plot of $\left[\left(\mathrm{C}_{5} \mathrm{Me}_{5}\right)_{2} \mathrm{Y}\right]_{2}(\mu-\mathrm{S}), \mathbf{5 - Y}(\mathbf{t o l})$, drawn at the $50 \%$ probability level. Hydrogen atom are omitted for clarity.

Table S3. Crystal data and structure refinement for $\mathbf{5 - Y}(\mathbf{t o l})$.

| Empirical formula | $\mathrm{C}_{40} \mathrm{H}_{60} \mathrm{SY}_{2}$ |
| :---: | :---: |
| Formula weight | 750.76 |
| Temperature | 143(2) K |
| Wavelength | 0.71073 A |
| Crystal system | Tetragonal |
| Space group | $P^{4}{ }_{21}{ }^{\text {c }}$ |
| Unit cell dimensions | $a=14.7891(7) \AA \quad \alpha=90^{\circ}$. |
|  | $b=14.7891(7) \AA \quad \beta=90^{\circ}$. |
|  | $\mathrm{c}=18.9371(9) \AA \quad \gamma=90^{\circ}$. |
| Volume | 4141.9(4) $\AA^{3}$ |
| Z | 4 |
| Density (calculated) | $1.204 \mathrm{Mg} / \mathrm{m}^{3}$ |
| Absorption coefficient | $2.861 \mathrm{~mm}^{-1}$ |
| F(000) | 1576 |
| Crystal color | colorless |
| Crystal size | $0.264 \times 0.072 \times 0.070 \mathrm{~mm}^{3}$ |
| Theta range for data collection | 1.747 to $27.091^{\circ}$ |
| Index ranges | $-18 \leq h \leq 18,-18 \leq k \leq 18,-23 \leq l \leq 24$ |
| Reflections collected | 31743 |
| Independent reflections | $4554[\mathrm{R}(\mathrm{int})=0.0489]$ |
| Completeness to theta $=25.242^{\circ}$ | 100.0 \% |
| Absorption correction | Numerical |
| Max. and min. transmission | 0.8974 and 0.5618 |
| Refinement method | Full-matrix least-squares on $\mathrm{F}^{2}$ |
| Data / restraints / parameters | 4554 / 0 / 205 |
| Goodness-of-fit on $\mathrm{F}^{2}$ | 1.051 |
| Final R indices [ $\mathrm{I}>2 \operatorname{sigma}(\mathrm{I})=4107$ data $]$ | $\mathrm{R} 1=0.0286, \mathrm{wR} 2=0.0611$ |
| R indices (all data, 0.78 Å) | $\mathrm{R} 1=0.0357, \mathrm{wR} 2=0.0633$ |
| Absolute structure parameter | -0.022(3) |
| Largest diff. peak and hole | 0.469 and -0.181 e. $\AA^{-3}$ |

## X-ray Data Collection, Structure Solution and Refinement for 5-Lu(tol).

A yellow crystal of approximate dimensions $0.124 \times 0.134 \times 0.398 \mathrm{~mm}$ was mounted on a glass fiber and transferred to a Bruker SMART APEX II diffractometer. The APEX2 ${ }^{1}$ program package was used to determine the unit-cell parameters and for data collection ( $20 \mathrm{sec} / \mathrm{frame}$ scan time for a sphere of diffraction data). The raw frame data was processed using SAINT ${ }^{2}$ and $\operatorname{SADABS}^{3}$ to yield the reflection data file. Subsequent calculations were carried out using the SHELXTL ${ }^{4}$ program. The systematic absences were consistent with the hexagonal space group $P^{\overline{4}}{ }_{21} c$ which was later determined to be correct.

The structure was solved by direct methods and refined on $\mathrm{F}^{2}$ by full-matrix least-squares techniques. The analytical scattering factors ${ }^{5}$ for neutral atoms were used throughout the analysis. The molecule was located on a two-fold rotation axis. Hydrogen atoms were included using a riding model. There were high residuals present in the final difference-Fourier map. It was not possible to determine the nature of the residuals, although it was probable that hexane or toluene solvent was present. The SQUEEZE routine in the PLATON ${ }^{9}$ program package was used to account for the electrons in the solvent accessible voids.

At convergence, $\mathrm{wR} 2=0.0334$ and Goof $=1.093$ for 205 variables refined against 5330 data $(0.73 \AA), \mathrm{R} 1=0.0141$ for those 5208 data with $\mathrm{I}>2.0 \sigma(\mathrm{I})$. The absolute structure was assigned by refinement of the Flack parameter. ${ }^{10}$


Figure S3. Thermal ellipsoid plot of $\left[\left(\mathrm{C}_{5} \mathrm{Me}_{5}\right)_{2} \mathrm{Lu}\right]_{2}(\mu-\mathrm{S}), \mathbf{5 - L u}(\mathbf{t o l})$, drawn at the $50 \%$ probability level. Hydrogen atom are omitted for clarity.

Table S4. Crystal data and structure refinement for $\mathbf{5 - L u}(\mathbf{t o l})$.

Empirical formula
Formula weight
Temperature
Wavelength
Crystal system
Space group
Unit cell dimensions

Volume
Z
Density (calculated)
Absorption coefficient
F(000)
Crystal color
Crystal size
Theta range for data collection
Index ranges
Reflections collected
Independent reflections
Completeness to theta $=25.500^{\circ}$
Absorption correction
Max. and min. transmission
Refinement method
Data / restraints / parameters
Goodness-of-fit on $\mathrm{F}^{2}$
Final R indices [ $\mathrm{I}>2 \operatorname{sigma}(\mathrm{I})=5208$ data $]$
R indices (all data, $0.73 \AA$ )
Absolute structure parameter
Largest diff. peak and hole
$\mathrm{C}_{40} \mathrm{H}_{60} \mathrm{Lu}_{2} \mathrm{~S}$
922.88

88(2) K
0.71073 Å

Tetragonal
$P^{4}{ }_{21} c$
$a=14.6701(7) \AA \quad \alpha=90^{\circ}$.
$b=14.6701(7) \AA \quad \beta=90^{\circ}$.
$\mathrm{c}=18.9233(9) \AA \quad \gamma=90^{\circ}$.
4072.5(4) $\AA^{3}$

4
$1.505 \mathrm{Mg} / \mathrm{m}^{3}$
$4.894 \mathrm{~mm}^{-1}$
1832
yellow
$0.398 \times 0.134 \times 0.124 \mathrm{~mm}^{3}$
1.756 to $29.200^{\circ}$
$-20 \leq h \leq 20,-20 \leq k \leq 20,-25 \leq l \leq 25$
49601
$5330[\mathrm{R}(\mathrm{int})=0.0244]$
100.0 \%

Numerical
0.6345 and 0.3881

Full-matrix least-squares on $\mathrm{F}^{2}$
5330 / 0 / 205
1.093
$\mathrm{R} 1=0.0141, \mathrm{wR} 2=0.0331$
$R 1=0.0148, w R 2=0.0334$
0.002(3)
0.889 and -0.262 e. $\AA^{-3}$

Table S5. Selected bond lengths $[\AA]$ and angles $\left[{ }^{\circ}\right]$ for $\mathbf{5 - Y}(\mathbf{t o l})$ and $\mathbf{5 - L u}(\mathbf{t o l})$.

|  | 5-Y(tol) | 5-Lu(tol) |  | 5-Y(tol) | 5-Lu(tol) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\operatorname{Ln}(1)-\mathrm{Cnt} 1$ | 2.341 | 2.288 | $\operatorname{Ln}(1)-\mathrm{S}(1)-\operatorname{Ln}(1){ }^{\prime}$ | 171.91(6) | 173.27(5) |
| $\operatorname{Ln}(1)-\mathrm{Cn}$ 2 | 2.351 | 2.297 | $\mathrm{S}(1)-\operatorname{Ln}(1)-\mathrm{Cnt} 1$ | 111.0 | 111.0 |
| $\operatorname{Ln}(1)-\mathrm{S}(1)$ | 2.5433(3) | 2.5026(2) | $\mathrm{S}(1)-\mathrm{Ln}(1)-\mathrm{Cnt} 2$ | 110.7 | 110.8 |
| $\operatorname{Ln}(1)-\mathrm{C}(1)$ | 2.622(3) | 2.581(3) | Cnt1-Ln(1)-Cnt2 | 138.3 | 138.2 |
| $\operatorname{Ln}(1)-\mathrm{C}(2)$ | 2.634(3) | 2.589(3) |  |  |  |
| $\operatorname{Ln}(1)-\mathrm{C}(3)$ | 2.646 (3) | 2.600 (3) |  |  |  |
| $\operatorname{Ln}(1)-\mathrm{C}(4)$ | 2.620(4) | $2.567(3)$ |  |  |  |
| $\operatorname{Ln}(1)-\mathrm{C}(5)$ | $2.638(3)$ | $2.594(3)$ |  |  |  |
| $\operatorname{Ln}(1)-\mathrm{C}(11)$ | 2.641(3) | 2.590(3) |  |  |  |
| $\operatorname{Ln}(1)-\mathrm{C}(12)$ | 2.648 (4) | 2.604(3) |  |  |  |
| $\operatorname{Ln}(1)-\mathrm{C}(13)$ | $2.638(3)$ | 2.588(3) |  |  |  |
| $\operatorname{Ln}(1)-\mathrm{C}(14)$ | 2.618(4) | 2.576(3) |  |  |  |
| $\operatorname{Ln}(1)-\mathrm{C}(15)$ | 2.660(3) | $2.612(3)$ |  |  |  |
| $\mathrm{C}(1)-\mathrm{C}(2)$ | $1.416(5)$ | 1.419(4) |  |  |  |
| $\mathrm{C}(2)-\mathrm{C}(3)$ | $1.418(5)$ | 1.423(4) |  |  |  |
| $\mathrm{C}(3)-\mathrm{C}(4)$ | $1.409(5)$ | 1.413(4) |  |  |  |
| $\mathrm{C}(4)-\mathrm{C}(5)$ | 1.419(5) | $1.424(5)$ |  |  |  |
| $\mathrm{C}(1)-\mathrm{C}(5)$ | 1.411(5) | $1.407(5)$ |  |  |  |
| $\mathrm{C}(11)-\mathrm{C}(12)$ | $1.416(5)$ | 1.422(5) |  |  |  |
| $\mathrm{C}(12)-\mathrm{C}(13)$ | $1.426(5)$ | $1.415(4)$ |  |  |  |
| $\mathrm{C}(13)-\mathrm{C}(14)$ | $1.410(5)$ | 1.419(4) |  |  |  |
| $\mathrm{C}(14)-\mathrm{C}(15)$ | $1.412(5)$ | 1.410(4) |  |  |  |
| $\mathrm{C}(11)-\mathrm{C}(15)$ | $1.413(5)$ | 1.423(4) |  |  |  |

## X-ray Data Collection, Structure Solution and Refinement for 5-Lu(hex).

A colorless crystal of approximate dimensions $0.198 \times 0.166 \times 0.096 \mathrm{~mm}$ was mounted on a glass fiber and transferred to a Bruker SMART APEX II diffractometer. The APEX2 ${ }^{11}$ program package and CELL_NOW ${ }^{12}$ were used to determine the unit-cell parameters. Data was collected using a $15 \mathrm{sec} /$ frame scan time for a sphere of diffraction data. The raw frame data was processed using SAINT ${ }^{2}$ and TWINABS ${ }^{13}$ to yield the reflection data file (HKLF5 format) ${ }^{13}$. Subsequent calculations were carried out using the SHELXTL ${ }^{14}$ program. There were no systematic absences nor any diffraction symmetry other than the Friedel condition. The centrosymmetric triclinic space group $P \overline{1}$ was assigned and later determined to be correct.

The structure was solved by direct methods and refined on $\mathrm{F}^{2}$ by full-matrix least-squares techniques. The analytical scattering factors ${ }^{5}$ for neutral atoms were used throughout the analysis. Hydrogen atoms were included using a riding model.

At convergence, $\mathrm{wR} 2=0.0650$ and Goof $=1.035$ for 410 variables refined against 9521 data $(0.74 \AA), \mathrm{R} 1=0.0269$ for those 8485 with $\mathrm{I}>2.0 \sigma(\mathrm{I})$. The structure was refined as a thee-component twin, $\mathrm{BASF}^{14}=0.14471$ and 0.02977 .


Figure S4. Thermal ellipsoid plot of $\left.\left[\left(\mathrm{C}_{5} \mathrm{Me}_{5}\right)_{2} \mathrm{Lu}\right]_{2}(\mu-\mathrm{S}), \mathbf{5 - L u ( h e x}\right)$, drawn at the $50 \%$ probability level. Hydrogen atom are omitted for clarity.

Table S6. Crystal data and structure refinement for 5-Lu(hex).

Empirical formula
Formula weight
Temperature
Wavelength
Crystal system
Space group
Unit cell dimensions

Volume
Z

Density (calculated)
Absorption coefficient F(000)
Crystal color

Crystal size
Theta range for data collection
Index ranges
Independent reflections
Completeness to theta $=25.500^{\circ}$
Absorption correction
Max. and min. transmission

Refinement method
Data / restraints / parameters
2
Goodness-of-fit on F
Final R indices [ $\mathrm{I}>2 \operatorname{sigma}(\mathrm{I})=8485$ data]
R indices (all data, $0.74 \AA$ )

Largest diff. peak and hole
$\mathrm{C}_{40} \mathrm{H}_{60} \mathrm{Lu}_{2} \mathrm{~S}$
922.88

88(2) K
$0.71073 \AA$
Triclinic
$P \overline{1}$
$a=10.5471(5) \AA \quad \alpha=77.2811(7)^{\circ}$.
$b=11.3849(6) \AA \quad \beta=76.8625(7)^{\circ}$.
$\mathrm{c}=16.6188(9) \AA \quad \gamma=85.1302(7)^{\circ}$.
1894.36(17) $\AA^{3}$

2
$1.618 \mathrm{Mg} / \mathrm{m}$
-1
5.261 mm

916
colorless
3
$0.198 \times 0.166 \times 0.096 \mathrm{~mm}$
1.835 to $28.689^{\circ}$
$-13 \leq h \leq 14,-14 \leq k \leq 15,0 \leq l \leq 22$
9521
99.9 \%

Numerical
0.431789 and 0.329664

Full-matrix least-squares on $\mathrm{F}^{2}$
9521 / 0 / 410
1.035
$\mathrm{R} 1=0.0269, \mathrm{wR} 2=0.0619$
$R 1=0.0340, w R 2=0.0650$
1.587 and - 0.997 e. $\AA^{-3}$

Table S7. Selected bond lengths $[\AA]$ and angles $\left[{ }^{\circ}\right]$ for 5-Lu(hex).

|  | 5-Lu(hex) |  | $\mathbf{5 - L u}(\mathbf{h e x})$ |  | 5-Lu(hex) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Lu}(1)-\mathrm{Cnt} 1$ | 2.300 | $\mathrm{Lu}(2)-\mathrm{Cnt} 3$ | 2.288 | $\mathrm{~S}(1)-\mathrm{Lu}(1)-\mathrm{Cnt} 1$ | 111.2 |
| $\mathrm{Lu}(1)-\mathrm{Cnt} 2$ | 2.300 | $\mathrm{Lu}(2)-\mathrm{Cnt} 4$ | 2.297 | $\mathrm{~S}(1)-\mathrm{Lu}(1)-\mathrm{Cnt} 2$ | 108.4 |
| $\mathrm{Lu}(1)-\mathrm{S}(1)$ | $2.4868(10)$ | $\mathrm{Lu}(2)-\mathrm{S}(1)$ | $2.4974(10)$ | $\mathrm{Cnt1-Lu}(1)-\mathrm{Cnt} 2$ | 140.4 |
| $\mathrm{Lu}(1)-\mathrm{C}(1)$ | $2.578(4)$ | $\mathrm{Lu}(2)-\mathrm{C}(21)$ | $2.591(4)$ | $\mathrm{S}(1)-\mathrm{Lu}(2)-\mathrm{Cnt} 3$ | 109.5 |
| $\mathrm{Lu}(1)-\mathrm{C}(2)$ | $2.618(4)$ | $\mathrm{Lu}(2)-\mathrm{C}(22)$ | $2.599(4)$ | $\mathrm{S}(1)-\mathrm{Lu}(2)-\mathrm{Cnt} 4$ | 110.9 |
| $\mathrm{Lu}(1)-\mathrm{C}(3)$ | $2.602(4)$ | $\mathrm{Lu}(2)-\mathrm{C}(23)$ | $2.567(4)$ | $\mathrm{Cnt3-Lu}(2)-\mathrm{Cnt} 4$ | 139.7 |
| $\mathrm{Lu}(1)-\mathrm{C}(4)$ | $2.613(4)$ | $\mathrm{Lu}(2)-\mathrm{C}(24)$ | $2.591(4)$ | $\mathrm{Lu}(1)-\mathrm{S}(1)-\mathrm{Lu}(2)$ | $166.68(5)$ |
| $\mathrm{Lu}(1)-\mathrm{C}(5)$ | $2.582(4)$ | $\mathrm{Lu}(2)-\mathrm{C}(25)$ | $2.589(4)$ |  |  |
| $\mathrm{Lu}(1)-\mathrm{C}(11)$ | $2.615(4)$ | $\mathrm{Lu}(2)-\mathrm{C}(31)$ | $2.562(4)$ |  |  |
| $\mathrm{Lu}(1)-\mathrm{C}(12)$ | $2.583(4)$ | $\mathrm{Lu}(2)-\mathrm{C}(32)$ | $2.608(4)$ |  |  |
| $\mathrm{Lu}(1)-\mathrm{C}(13)$ | $2.572(4)$ | $\mathrm{Lu}(2)-\mathrm{C}(33)$ | $2.601(4)$ |  |  |
| $\mathrm{Lu}(1)-\mathrm{C}(14)$ | $2.605(4)$ | $\mathrm{Lu}(2)-\mathrm{C}(34)$ | $2.610(4)$ |  |  |
| $\mathrm{Lu}(1)-\mathrm{C}(15)$ | $2.614(4)$ | $\mathrm{Lu}(2)-\mathrm{C}(35)$ | $2.586(4)$ |  |  |
| $\mathrm{C}(1)-\mathrm{C}(2)$ | $1.426(6)$ | $\mathrm{C}(21)-\mathrm{C}(22)$ | $1.411(5)$ |  |  |
| $\mathrm{C}(2)-\mathrm{C}(3)$ | $1.413(6)$ | $\mathrm{C}(22)-\mathrm{C}(23)$ | $1.428(6)$ |  |  |
| $\mathrm{C}(3)-\mathrm{C}(4)$ | $1.427(6)$ | $\mathrm{C}(23)-\mathrm{C}(24)$ | $1.422(6)$ |  |  |
| $\mathrm{C}(4)-\mathrm{C}(5)$ | $1.421(6)$ | $\mathrm{C}(24)-\mathrm{C}(25)$ | $1.419(6)$ |  |  |
| $\mathrm{C}(1)-\mathrm{C}(5)$ | $1.427(6)$ | $\mathrm{C}(21)-\mathrm{C}(25)$ | $1.424(5)$ |  |  |
| $\mathrm{C}(11)-\mathrm{C}(12)$ | $1.423(5)$ | $\mathrm{C}(31)-\mathrm{C}(32)$ | $1.430(6)$ |  |  |
| $\mathrm{C}(12)-\mathrm{C}(13)$ | $1.422(6)$ | $\mathrm{C}(32)-\mathrm{C}(33)$ | $1.417(6)$ |  |  |
| $\mathrm{C}(13)-\mathrm{C}(14)$ | $1.420(6)$ | $\mathrm{C}(33)-\mathrm{C}(34)$ | $1.419(6)$ |  |  |
| $\mathrm{C}(14)-\mathrm{C}(15)$ | $1.415(6)$ | $\mathrm{C}(34)-\mathrm{C}(35)$ | $1.425(6)$ |  |  |
| $\mathrm{C}(11)-\mathrm{C}(15)$ | $1.415(6)$ | $\mathrm{C}(31)-\mathrm{C}(35)$ | $1.422(6)$ |  |  |
|  |  |  |  |  |  |

Computational Details. The initial structure optimizations of 3-Lu, 3-Y, and 4-Y, starting from the available crystal data, ${ }^{15}$ were performed using the TPSSh $^{16}$ hybrid meta-GGA functional. Split valence basis sets with polarization functions on non-hydrogen atoms (SV(P)) were used for light atoms and the triple-zeta valence basis sets with two sets of polarization functions (def2TZVP) for Y and Lu. ${ }^{17,18}$ TPSSh was chosen due to its established performance for transition metal compounds, reductive Ln chemistry, and Ln photochemistry. ${ }^{19-22}$ Relativistic small-core pseudopotentials ${ }^{23}$ were employed for Y and Lu. Vibrational frequencies were computed at the $\mathrm{TPSSh} / \mathrm{SV}(\mathrm{P})$ level, and all ground state structures were confirmed to be minima by the absence of imaginary modes. ${ }^{24}$ A further optimization using larger triple-zeta valence basis sets (def2TZVP ${ }^{18}$ ) for all atoms was then performed. The differences in bond lengths between the $\operatorname{SV}(\mathrm{P})$ and the TZVP structures were typically $0.02 \AA$ or less. Fine quadrature grids (size m4) ${ }^{25}$ were used throughout. SCF energies and density matrices were converged to $10^{-7}$ a.u. All calculations were performed using the Turbomole quantum chemistry software. ${ }^{26}$ All molecular orbital plots were computed with $\operatorname{SV}(\mathrm{P})$ basis sets using contour values of 0.06 . Molecular orbital plots of the HOMO and LUMO of $\mathbf{4 - Y}$ are shown in Figure S6. Theoretical, zero temperature gasphase UV-visible spectra were generated from time dependent density functional theory (TDDFT) excitation energy calculations. ${ }^{27}$ The excitation energies and oscillator strengths for selected transitions of 3-Lu, 3-Y and 4-Y are given in Table S10.


Figure S5. Molecular orbital plots of (a) the HOMO and (b) the LUMO of 4-Y, using a contour value of 0.06 .

Table S8. Computed excitation energies using TPSSH and SV(P) basis sets. Ground state SCF energies and one-electron density matrix were converged to $10^{-7}$.

| Compound | Wavelength (nm) | Oscillator Strength (a.u.) | Dominan <br> occupied | t Contribution <br> virtual | \% comp |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-Y | 391 | 0.014 | 92a (HOMO) | 93a (LUMO) | 89.4 |
|  | 369 | 0.021 | 91a (HOMO-1) | 93a (LUMO) | 91.8 |
|  | 346 | 0.003 | 90a (HOMO-2) | 93a (LUMO) | 99.1 |
|  | 344 | 0.005 | 89a (HOMO-3) | 93a (LUMO) | 98.3 |
| 3-Lu | 389 | 0.005 | 108a (HOMO) | 109a (LUMO) | 91 |
|  | 361 | 0.010 | 107a (HOMO-1) | 109a (LUMO) | 94.5 |
|  | 358 | 0.021 | 106a (HOMO-2) | 109a (LUMO) | 91.2 |
|  | 338 | 0.002 | 104a (HOMO-4) | 109a (LUMO) | 70.6 |
|  |  |  | 105a (HOMO-3) | 109a (LUMO) | 28.6 |
|  | 336 | 0.006 | 105a (HOMO-3) | 109a (LUMO) | 70.5 |
|  |  |  | 104a (HOMO-4) | 109a (LUMO) | 28.7 |
| $4-Y$ | 389 | 0.018 | 96a (HOMO) | 97a (LUMO) | 93.1 |
|  | 362 | 0.011 | 95a (HOMO-1) | 97a (LUMO) | 68.9 |
|  |  |  | 94a (HOMO-2) | 97a (LUMO) | 26.9 |
|  | 357 | 0.002 | 94a (HOMO-2) | 97a (LUMO) | 70.2 |
|  |  |  | 95a (HOMO-1) | 97a (LUMO) | 28.9 |
|  | 335 | 0.004 | 93a (HOMO-3) | 97a (LUMO) | 73.3 |
|  |  |  | 92a (HOMO-4) | 97a (LUMO) | 25.9 |

## Elemental Analysis Attempts for 5-Ln

5-Y Calcd for $\mathrm{C}_{40} \mathrm{H}_{60} \mathrm{SY}_{2}: \mathrm{C}, 63.99 ; \mathrm{H}, 8.06$.
Found: 1) C, 63.14; H, 8.26
2) C, $65.11 ; \mathrm{H}, 8.79$
3) C, $65.62 ; \mathrm{H}, 8.71$
4) C, $65.01 ; \mathrm{H}, 8.83$
5) C, $64.68 ; \mathrm{H}, 8.10$
6) C, 66.68 ; H, 8.91
7) C, 64.72; H, 8.41
8) C, 64.51 ; H, 8.50

5-Lu Anal. Calcd for $\mathrm{C}_{40} \mathrm{H}_{60} \mathrm{SLu}_{2}$ : C 52.06 H 6.55 .
Found: 1) C 54.72 H 6.84
2) C 54.17 H 6.96
3) C 54.11 H 6.71
4) C 54.08 H 6.29
5) C 53.75 H 6.32 .

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Definitions:

$$
\begin{aligned}
& \mathrm{wR} 2=\left[\Sigma\left[\mathrm{w}\left(\mathrm{~F}_{\mathrm{o}}^{2}-\mathrm{F}_{\mathrm{c}}^{2}\right)^{2}\right] / \Sigma\left[\mathrm{w}\left(\mathrm{~F}_{\mathrm{o}}^{2}\right)^{2}\right]\right]^{1 / 2} \\
& \mathrm{R} 1=\Sigma| | \mathrm{F}_{\mathrm{o}}\left|-\left|\mathrm{F}_{\mathrm{c}}\right|\right| \Sigma\left|\mathrm{F}_{\mathrm{o}}\right|
\end{aligned}
$$

Goof $=\mathrm{S}=\left[\Sigma\left[\mathrm{w}\left(\mathrm{F}_{\mathrm{o}}{ }^{2}-\mathrm{F}_{\mathrm{c}}{ }^{2}\right)^{2}\right] /(\mathrm{n}-\mathrm{p})\right]^{1 / 2}$ where n is the number of reflections and p is the total number of parameters refined.

