

# **Role of $\text{Na}^+$ Interstitials and Dopants in Enhancing the $\text{Na}^+$ Conductivity of the Cubic $\text{Na}_3\text{PS}_4$ Superionic Conductor**

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Table S1: Average site occupancies for pristine t-Na<sub>3</sub>PS<sub>4</sub>, pristine and doped c-Na<sub>3</sub>PS<sub>4</sub> compounds with different dopant concentrations  $x$  at 800K. To compare with the case of c-Na<sub>3</sub>PS<sub>4</sub>, we artificially label the Na sites in t-Na<sub>3</sub>PS<sub>4</sub> as Na1, whereas the middle points between any two neighboring Na sites are labeled as Na2.

	Structures	$x$	Na1 site occupancy	Na2 site occupancy
t-Na <sub>3</sub> PS <sub>4</sub>	pristine		0.88	0.06
	pristine		0.84	0.08
	Na <sup>+</sup> excess		0.68	0.17
c-Na <sub>3</sub> PS <sub>4</sub>	Si-doped	0.0625	0.76	0.13
	Ge-doped	0.0625	0.62	0.20
	Sn-doped	0.0625	0.79	0.12

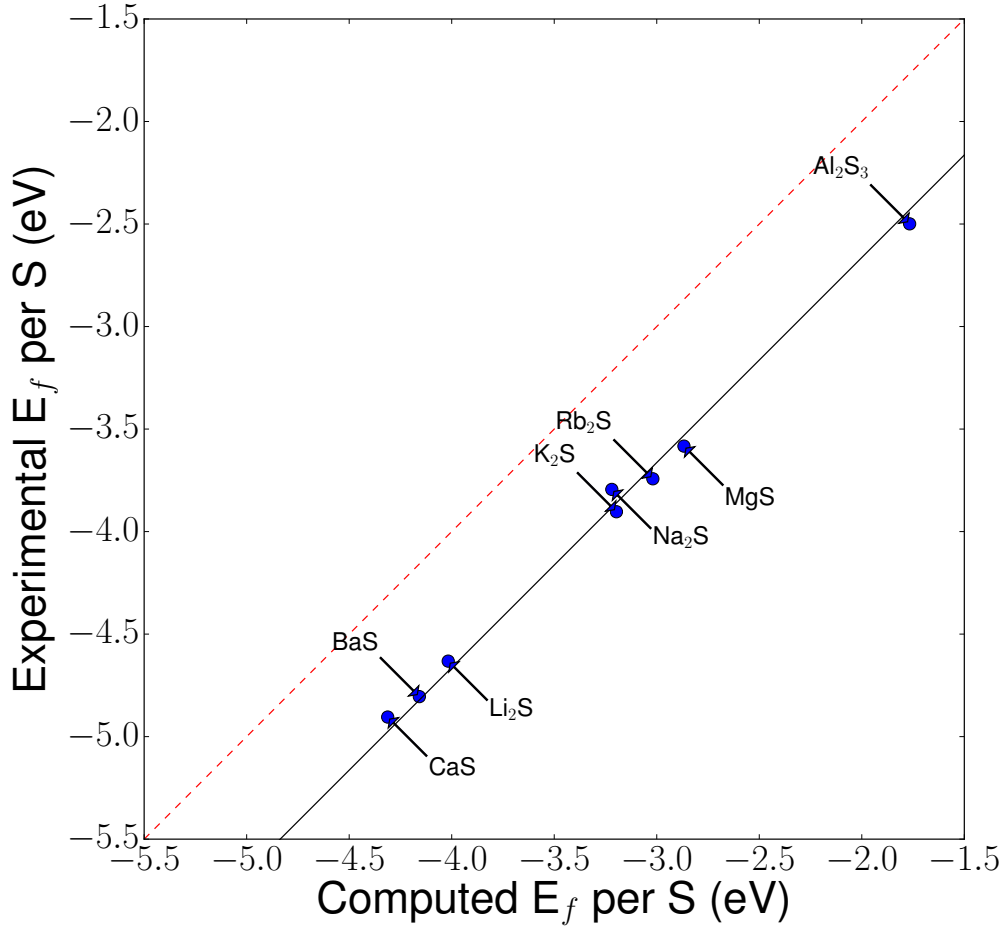
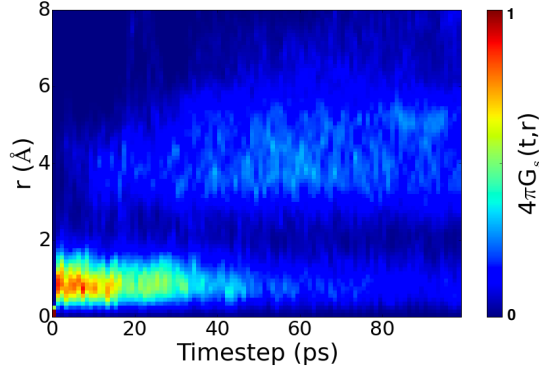
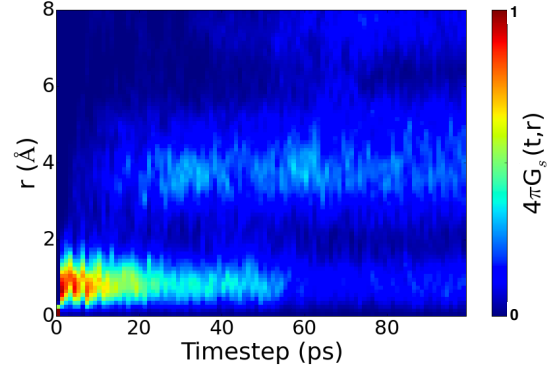


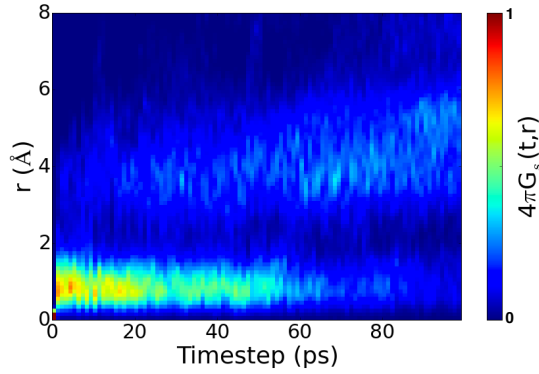
Figure S1: (Color online) Determination of energy difference constant (0.66 eV per S atom) between the DFT and experimental formation energies for sulfides.



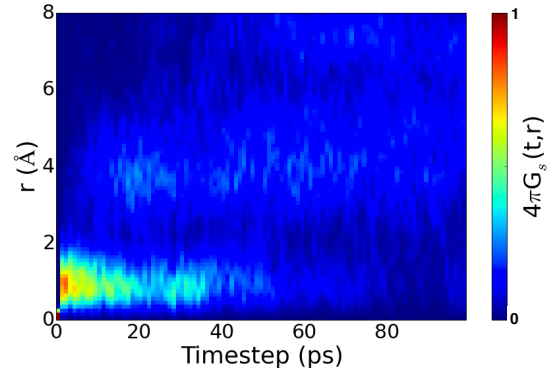
(a) M=Si,  $x=0.0625$



(b) M=Ge,  $x=0.0625$



(c) M=Sn,  $x=0.0625$



(d) M=Si,  $x=0.125$

Figure S2: (Color online) Plots of the self-part of the van Hove correlation function ( $G_s$ ) for  $\text{Na}_{3+x}\text{M}_x\text{P}_{1-x}\text{S}_4$  at 800 K.  $G_s$  is a function of the Na-Na pair distance  $r$  and time  $t$ .