

# Relative Phase Change of Nearby Resonances in Temporally Delayed Sum Frequency Spectra

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## Supporting Information

**Table 1.** List of parameters obtained by fitting experimental PPP spectra at 0 fs and 300 fs IR-visible delay (shown in Figure 1 of the main text) to Eq. (2) of the main text.

IR-Vis Delay (fs)	$A_{\text{NR}}$ (a.u.)	$\omega_{\text{g}}$ ( $\text{cm}^{-1}$ )	$\sigma_{\text{g}}$ ( $\text{cm}^{-1}$ )	$\phi_{\text{NR}}$ (rad)	$B(\text{r}^+)$ (a.u.)	$B(\text{r}^-)$ (a.u.)	$I(\text{r}^+)$ ( $\text{cm}^{-1}$ )	$I(\text{r}^-)$ ( $\text{cm}^{-1}$ )	$\omega(\text{r}^+)$ ( $\text{cm}^{-1}$ )	$\omega(\text{r}^-)$ ( $\text{cm}^{-1}$ )
0	0.07	2902	296	-1.5	-1.0	-0.63	20.0	16.5	2915	2975
300	0.04	2940	300	0.39	0.38	-0.28	14.3	14.0	2907	2979

**Table 2.** List of parameters obtained by fitting simulated PPP spectra at 0 fs and 300 fs IR-visible delay (shown in Figure 3 of the main text) to Eq. (2) of the main text.

IR-Vis Delay (fs)	$A_{\text{NR}}$ (a.u.)	$\omega_{\text{g}}$ ( $\text{cm}^{-1}$ )	$\sigma_{\text{g}}$ ( $\text{cm}^{-1}$ )	$\phi_{\text{NR}}$ (rad)	$B(\text{r}^+)$ (a.u.)	$B(\text{r}^-)$ (a.u.)	$\Gamma(\text{r}^+)$ ( $\text{cm}^{-1}$ )	$\Gamma(\text{r}^-)$ ( $\text{cm}^{-1}$ )	$\omega(\text{r}^+)$ ( $\text{cm}^{-1}$ )	$\omega(\text{r}^-)$ ( $\text{cm}^{-1}$ )
0	0.09	2904	206	-1.7	-1.0	-0.63	18.6	16.3	2917	2974
300	0.05	2917	237	-2.6	0.39	-0.50	16.7	13.6	2922	2979

**Table 3.** Wavelength  $\lambda$  and pulse duration  $\tau$  parameters used in Eqs. (9) and (10) to simulate the electric fields of the visible and IR pulses.

	$\lambda$ (nm)	$\tau$ (fs)
IR	3440	80
Visible	796	50

**Table 4.** The amplitudes  $B$ , line widths  $\Gamma$  and central frequencies  $\omega$  of the resonant response for the symmetric ( $\text{r}^+$ ) and asymmetric ( $\text{r}^-$ )  $\text{CH}_3$ -stretch vibrational modes, as well as the amplitude and phase of the nonresonant background used in the simulations (Eq. (8) of the main text).

IR-Vis Delay (fs)	$A_{\text{NR}}$ (a.u.)	$\phi_{\text{NR}}$ (deg)	$B(\text{r}^+)$ (a.u.)	$B(\text{r}^-)$ (a.u.)	$\Gamma(\text{r}^+)$ ( $\text{cm}^{-1}$ )	$\Gamma(\text{r}^-)$ ( $\text{cm}^{-1}$ )	$\omega(\text{r}^+)$ ( $\text{cm}^{-1}$ )	$\omega(\text{r}^-)$ ( $\text{cm}^{-1}$ )
0	130	245	-0.1	-0.07	12	10	2915	2964
300	$1.5 \times 10^8$	190	0.1	0.07	12	8	2915	2975

Note: the nonresonant background amplitude  $A_{\text{NR}}$  for the 300 fs delayed case is large because it represents interaction with the (very weak) leading edge of the visible pulse (see Figure 2 of the main text). The amplitude of the visible pulse at -300 fs could not be quantified as it was below our detection limit, and thus the spectra for the 300 fs delay are fit using  $A_{\text{NR}}$  as an independent adjustable parameter.