

Supporting Information

Relevance of dispersion and the electronic spin in the DFT+U approach for the description of pristine and defective TiO₂ anatase

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I. Geometry Optimization procedure

1. The volume is varied +/-15% from its original volume and 7 deformed structure calculations are performed.
2. ISIF=2 followed by ISIF=4 calculations over the preoptimized structures were performed.
3. With the computed energies at each volume an EOS fitting was performed using a Birch-Murnaghan equation at fourth order as implemented in vaspkit. (See Figure S1 a and c)
4. The equilibrium volume is extracted and used as input for the next set of calculations.
5. For optimizing the a/c ratio with constant volume a maximum physical strain ϵ is defined as the percent variation of the a/c ratio (i.e. if there is a +/-5% variation in a/c then $\epsilon = \pm 0.05$), then the a/c of the distorted structure at the maximum physical strain is determined from $(a/c) = (a/c)_{\text{initial}} \cdot (1 + \epsilon)$. Then 7 distorted structures were computed considering 7 ϵ values through variations of -5% to 5% of the a/c initial value with a step of 1.67%.
6. Then ISIF=2 calculations were computed for each distorted structure and the results of energy vs strain were plotted and fitted to a 4th order polynomial (See figure S1 b and d).

$$E(x) = ax^4 + bx^3 + cx^2 + dx + c$$

with $x = \epsilon$ and the minimum corresponds to the derivative $dE/dx = 0$, i.e:

$$0 = 4ax^3 + 3bx^2 + 2cx + d$$

Then by solving the equation we use this new value of ϵ_{min} physical strain to compute the a/c ratio and build a new structure, that will be used to optimize the ratio a/c at ISIF=2 with fixed volume followed by ISIF=7 calculation, this final structure is used to reoptimize the volume at a fixed value of the ratio a/c through an EOS fitting as explained next.

7. The step one described previously is repeated by increasing the number of deformed structures for the volume calculations to 9. The procedure is repeated by following steps 2 to 4. Then for the a/c ratio optimization 9 distorted structures were used and steps 5 to 6 were followed.
8. Finally, after completing 4 calculation cycles (1st volume optimization – 1st a/c ratio optimization - 2nd volume optimization – 2nd a/c ratio optimization) the final structure is fully relaxed by ISIF=3 calculation.
9. The convergence between the volume, lattice parameters and energy were checked at each calculation cycle and the final structure is compared to the fully relaxed structure to verify a convergence $< 1 \times 10^{-6}$ Å in the lattice parameters and $< 7 \times 10^{-4}$ eV in the energy.

The convergence data for TiO_2 is presented in Table S1.

Ti_2O_3 geometry optimization was carried out by following a similar procedure as that previously described. However, instead of a/c ratio optimization at constant volume the α angle was optimized at constant volume (see figure S2 b and d). Four calculation cycles were performed (1st volume optimization (see Figure S2 a) – 1st α angle optimization - 2nd volume optimization (see Figure S2 c) – 2nd α angle optimization) the final structure was fully relaxed by ISIF=3 calculation. The convergence data for Ti_2O_3 is presented in table S2.

The relaxed structure at U_{n-1} is used as a starting structure for the next U_n ($u=1,2,3,4$) optimization procedure. The initial structures for the TiO_2 and Ti_2O_3 $U=0$ geometry optimization were taken from Howard et.al.[63] and Straumanis et.al [64], respectively.

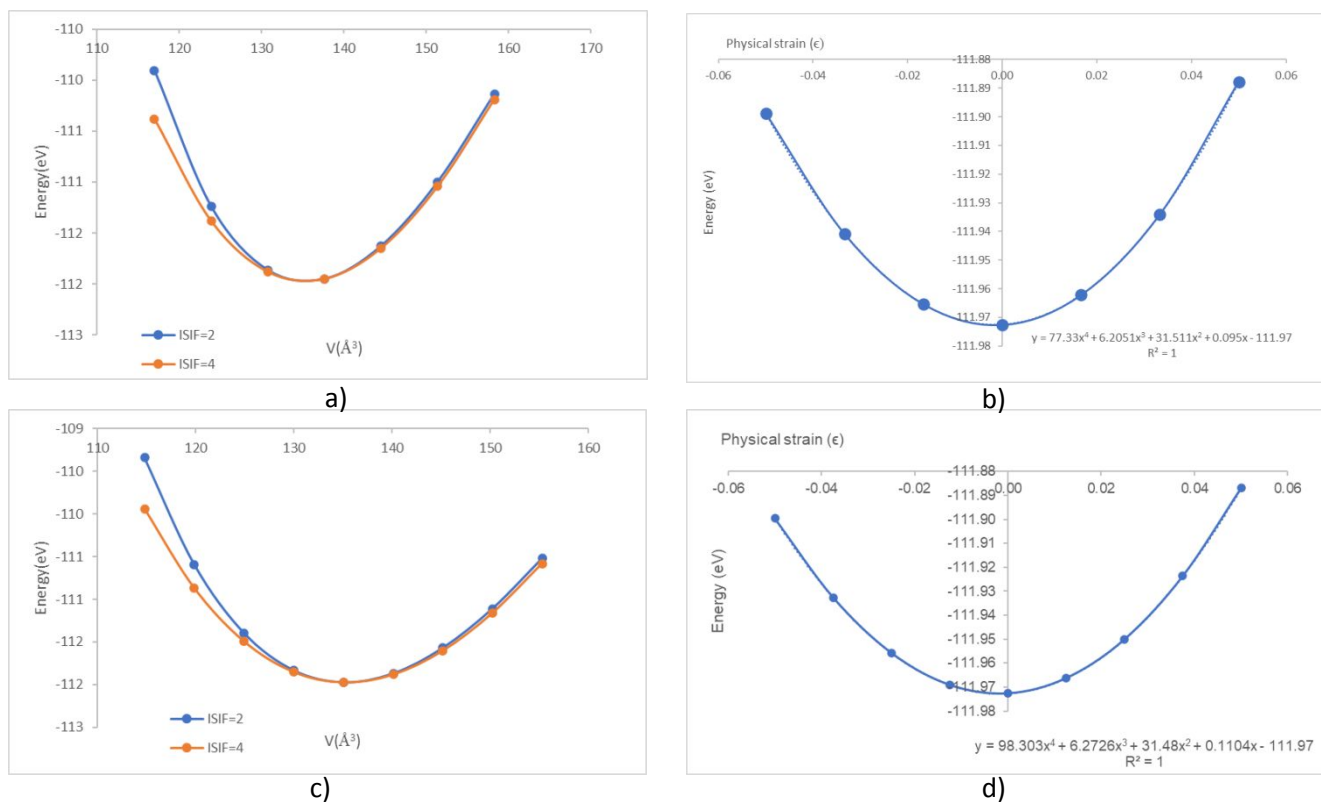


Figure S1. PBEsol U=1 Optimization steps until convergence is achieved for the geometry parameters of TiO_2 . Volume optimization steps (a,c), and a/c optimization calculations (b,d).

Table S1. Convergence data and geometry parameters along each optimization step for TiO_2

Calculation	Step	a(Å)	c(Å)	$\Delta a(\text{\AA})$	$\Delta c(\text{\AA})$	E(eV)	$\Delta E(\text{eV})$	Vol($\text{\AA}^3$)	$\Delta \text{Vol}(\text{\AA}^3)$
-	0	3.7800	9.510					136.2680	
Vopt1	1	3.7814	9.459	1.4078E-03	-5.0528E-02	-111.9726		135.2614	-1.0066E+00
1_a/c	2	3.7797	9.455	-3.0117E-04	-5.4811E-02	-111.9728	-2.0132E-04	135.0780	-1.1900E+00
Vopt2	3	3.7820	9.461	1.9674E-03	-4.9136E-02	-111.9726	2.0413E-04	135.3214	-9.4662E-01
2_a/c	4	3.7775	9.466	-2.4759E-03	-4.3629E-02	-111.9730	-3.6941E-04	135.0822	-1.1858E+00
ISIF=3	5	3.7775	9.466	-2.4760E-03	-4.3628E-02	-111.9723	6.4695E-04	135.0822	-1.1858E+00

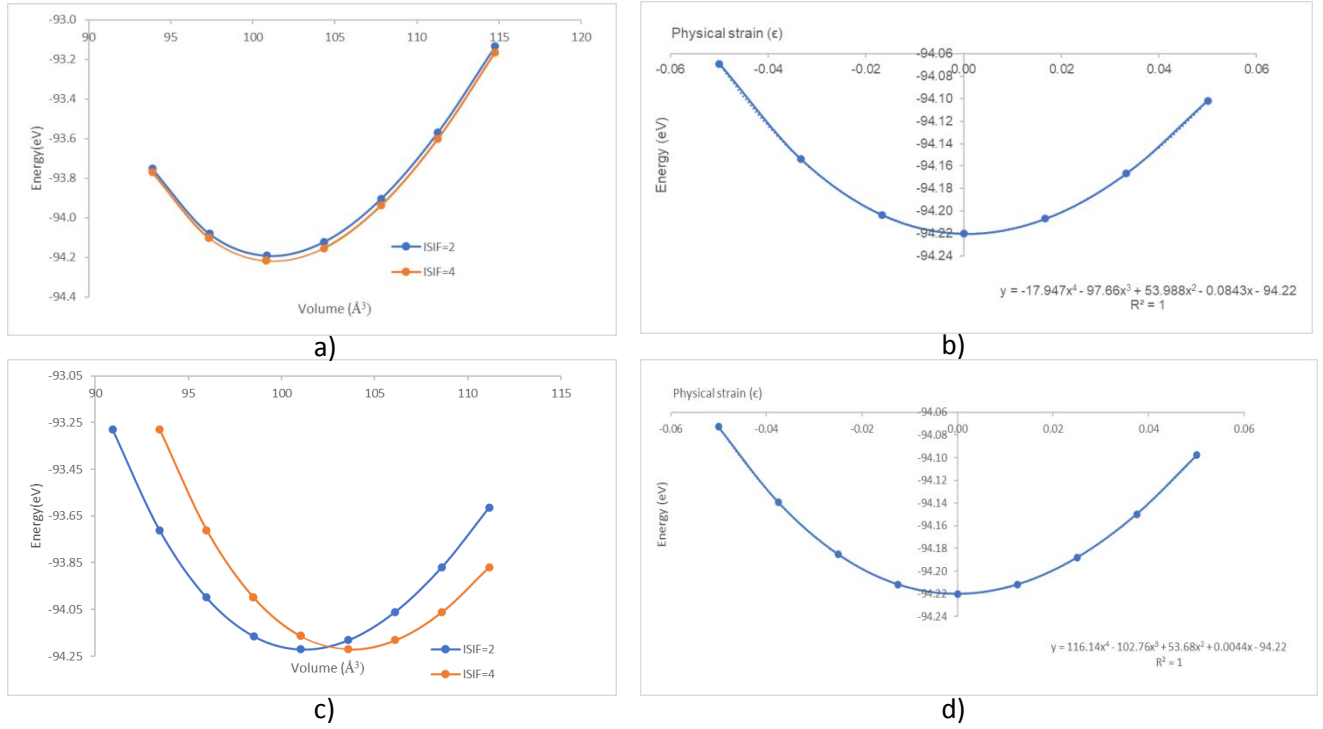


Figure S2. PBEsol U=1 Optimization steps until convergence is achieved for the geometry parameters of Ti_2O_3 . Volume optimization steps (a,c), and α angle optimization calculations (b,d).

Table S2. Convergence data and geometry parameters along each optimization step for Ti_2O_3 .

Calculation	Step	a($\text{\AA}$)	$\alpha(^{\circ})$	$\Delta a(\text{\AA})$	$\Delta \alpha(^{\circ})$	E(eV)	$\Delta E(\text{eV})$	Vol($\text{\AA}^3$)	$\Delta \text{Vol}(\text{\AA}^3)$
-	0	5.4310	56.580					104.3219	
V1opt	1	5.4381	55.264	7.1100E-03	-1.3158E+00	-94.2202		101.2000	-3.1219E+00
Ang1	2	5.4331	55.307	-5.0000E-03	4.3200E-02	-94.2203	-1.3268E-04	101.0400	-1.6000E-01
V2opt	3	5.4363	55.307	3.1900E-03	0.0000E+00	-94.2202	1.7444E-04	101.2167	1.7666E-01
Ang2	4	5.4333	55.305	-3.0300E-03	-2.3000E-03	-94.2204	-2.2510E-04	101.0400	-1.7666E-01
ISIF=3	5	5.4333	55.305	0.0000E+00	0.0000E+00	-94.2199	4.6883E-04	101.0411	1.1130E-03

II. Converged geometries of TiO₂

1. TiO₂ PBEsol U=0

Ti O2

1.0000000000000000

3.7729692360596809 0.0000000000000000 -0.0000000000000000

-0.0000000000000000 3.7729692360596809 -0.0000000000000000

0.0000000000000000 -0.0000000000000000 9.5561387893009861

Ti O

4 8

Direct

0.0000000000000000 -0.0000000000000000 -0.0000000000000000

0.5000000000000000 0.5000000000000000 0.5000000000000000

-0.0000000000000000 0.5000000000000000 0.2500000000000000

0.5000000000000000 0.0000000000000000 0.7500000000000000

-0.0000000000000000 0.0000000000000000 0.2076179618386709

0.5000000000000000 0.5000000000000000 0.7076179768386774

-0.0000000000000000 0.5000000000000000 0.4576179768386745

0.5000000000000000 0.0000000000000000 0.9576179768386774

0.5000000000000000 -0.0000000000000000 0.5423820231613226

0.0000000000000000 0.5000000000000000 0.0423820531613271

0.5000000000000000 0.5000000000000000 0.2923820231613255

0.0 -0.0000000000000000 0.7923820231613226

2. TiO₂ PBEsol U=1

Ti O2

1.0000000000000000

3.7871192869247983	0.0000000000000000	0.0000000000000000
0.0000000000000000	3.7871192869247983	0.0000000000000000
0.0000000000000000	0.0000000000000000	9.5668814005190317

Ti O

4 8

Direct

-0.0000000000000000	0.0000000000000000	-0.0000000000000000
0.5000000000000000	0.5000000000000000	0.5000000000000000
0.0000000000000000	0.5000000000000000	0.2500000000000000
0.5000000000000000	0.0000000000000000	0.7500000000000000
0.0000000000000000	0.0000000000000000	0.2076655252589770
0.5000000000000000	0.5000000000000000	0.7076655102589721
-0.0000000000000000	0.5000000000000000	0.4576655102589722
0.5000000000000000	-0.0000000000000000	0.9576655102589721
0.5000000000000000	-0.0000000000000000	0.5423344897410279
-0.0000000000000000	0.5000000000000000	0.0423345007410251
0.5000000000000000	0.5000000000000000	0.2923344897410278
-0.0000000000000000	0.0000000000000000	0.7923344897410279

3. TiO₂ PBEsol U=2

Ti O2

1.0000000000000000		
3.8008914404632632	0.0000000000000000	0.0000000000000000
0.0000000000000000	3.8008914404632632	0.0000000000000000
0.0000000000000000	0.0000000000000000	9.5772813666030334

Ti O

4 8

Direct

-0.0000000000000000	0.0000000000000000	0.0000000000000000
0.5000000000000000	0.5000000000000000	0.5000000000000000

-0.0000000000000000	0.5000000000000000	0.2500000000000000
0.5000000000000000	0.0000000000000000	0.7500000000000000
0.0000000000000000	0.0000000000000000	0.2077279904936862
0.5000000000000000	0.5000000000000000	0.7077279154936834
0.0000000000000000	0.5000000000000000	0.4577279154936835
0.5000000000000000	-0.0000000000000000	0.9577279154936834
0.5000000000000000	-0.0000000000000000	0.5422720845063166
0.0000000000000000	0.5000000000000000	0.0422720505063137
0.5000000000000000	0.5000000000000000	0.2922720845063165
0.0000000000000000	0.0000000000000000	0.7922720845063166

4. TiO_2 PBEsol U=3

Ti O2

1.0000000000000000		
3.8140727059167192	0.0000000000000000	0.0000000000000000
0.0000000000000000	3.8140727059167192	0.0000000000000000
0.0000000000000000	0.0000000000000000	9.5900726503956246

Ti O

4 8

Direct

-0.0000000000000000	0.0000000000000000	0.0000000000000000
0.5000000000000000	0.5000000000000000	0.5000000000000000
-0.0000000000000000	0.5000000000000000	0.2500000000000000
0.5000000000000000	-0.0000000000000000	0.7500000000000000
0.0000000000000000	-0.0000000000000000	0.2077591624932607
0.5000000000000000	0.5000000000000000	0.7077590574932631
0.0000000000000000	0.5000000000000000	0.4577590874932652
0.5000000000000000	-0.0000000000000000	0.9577590574932631
0.5000000000000000	0.0000000000000000	0.5422409425067369
0.0000000000000000	0.5000000000000000	0.0422408865067398

0.5000000000000000 0.5000000000000000 0.2922409125067348
0.0000000000000000 0.0000000000000000 0.7922409425067369

5. TiO_2 PBEsol U=4

Ti O2

1.0000000000000000
3.8265186425189275 0.0000000000000000 0.0000000000000000
0.0000000000000000 3.8265186425189275 -0.0000000000000000
0.0000000000000000 -0.0000000000000000 9.6072785298340868

Ti O

4 8

Direct

0.0000000000000000 -0.0000000000000000 0.0000000000000000
0.5000000000000000 0.5000000000000000 0.5000000000000000
-0.0000000000000000 0.5000000000000000 0.2500000000000000
0.5000000000000000 0.0000000000000000 0.7500000000000000
0.0000000000000000 -0.0000000000000000 0.2077300525869028
0.5000000000000000 0.5000000000000000 0.7077299185869055
0.0000000000000000 0.5000000000000000 0.4577299485869085
0.5000000000000000 -0.0000000000000000 0.9577299185869055
0.5000000000000000 0.0000000000000000 0.5422700814130945
0.0000000000000000 0.5000000000000000 0.0422700104130919
0.5000000000000000 0.5000000000000000 0.2922700514130915
-0.0000000000000000 0.0000000000000000 0.7922700814130945

6. TiO_2 PBEsol U=6

Ti O2

1.0000000000000000

3.8509222545303814 0.0000000000000000 0.0000000000000000

0.0000000000000000 3.8509222545303814 -0.0000000000000000

0.0000000000000000 -0.0000000000000000 9.6449366076142251

Ti O

4 8

Direct

-0.0000000000000000 -0.0000000000000000 -0.0000000000000000

0.5000000000000000 0.5000000000000000 0.5000000000000000

-0.0000000000000000 0.5000000000000000 0.2500000000000000

0.5000000000000000 -0.0000000000000000 0.7500000000000000

-0.0000000000000000 0.0000000000000000 0.2076555746832124

0.5000000000000000 0.5000000000000000 0.7076553656832130

0.0000000000000000 0.5000000000000000 0.4576555146832074

0.5000000000000000 -0.0000000000000000 0.9576553656832130

0.5000000000000000 0.0000000000000000 0.5423446343167870

0.0000000000000000 0.5000000000000000 0.0423444813167923

0.5000000000000000 0.5000000000000000 0.2923444853167926

0.0 -0.0000000000000000 0.7923446343167870

7. TiO_2 PBEsol-D3 U=0

Ti O2

1.0000000000000000

3.7638888359000000 0.0000000000000000 0.0000000000000000

0.0000000000000000 3.7638888359000000 0.0000000000000000

0.0000000000000000 0.0000000000000000 9.4559316634999995

Ti O

4 8

Direct

0.0000000000000000	0.0000000000000000	0.0000000000000000
0.5000000000000000	0.5000000000000000	0.5000000000000000
0.0000000000000000	0.5000000000000000	0.2500000000000000
0.5000000000000000	0.0000000000000000	0.7500000000000000
0.0000000000000000	0.0000000000000000	0.2088565079999967
0.5000000000000000	0.5000000000000000	0.7088565230000015
0.0000000000000000	0.5000000000000000	0.4588565230000015
0.5000000000000000	0.0000000000000000	0.9588565230000015
0.5000000000000000	0.0000000000000000	0.5411434769999985
0.0000000000000000	0.5000000000000000	0.0411435070000010
0.5000000000000000	0.5000000000000000	0.2911434769999985
0.0000000000000000	0.0000000000000000	0.7911434769999985

8. TiO₂ PBEsol-D3 U=1

Ti O2

1.0000000000000000		
3.7775239944000001	0.0000000000000000	0.0000000000000000
0.0000000000000000	3.7775239944000001	0.0000000000000000
0.0000000000000000	0.0000000000000000	9.4663715363000005

Ti O

4 8

Direct

0.0000000000000000	0.0000000000000000	0.0000000000000000
0.5000000000000000	0.5000000000000000	0.5000000000000000
0.0000000000000000	0.5000000000000000	0.2500000000000000
0.5000000000000000	0.0000000000000000	0.7500000000000000

0.0000000000000000	0.0000000000000000	0.2089503560000026
0.5000000000000000	0.5000000000000000	0.7089503409999978
0.0000000000000000	0.5000000000000000	0.4589503409999978
0.5000000000000000	0.0000000000000000	0.9589503409999978
0.5000000000000000	0.0000000000000000	0.5410496590000022
0.0000000000000000	0.5000000000000000	0.0410496699999996
0.5000000000000000	0.5000000000000000	0.2910496590000022
0.0000000000000000	0.0000000000000000	0.7910496590000022

9. TiO_2 PBEsol-D3 U=2

Ti O2

1.0000000000000000		
3.7906253338000000	0.0000000000000000	0.0000000000000000
0.0000000000000000	3.7906253338000000	0.0000000000000000
0.0000000000000000	0.0000000000000000	9.4809303283999995

Ti O

4 8

Direct

0.0000000000000000	0.0000000000000000	0.0000000000000000
0.5000000000000000	0.5000000000000000	0.5000000000000000
0.0000000000000000	0.5000000000000000	0.2500000000000000
0.5000000000000000	0.0000000000000000	0.7500000000000000
0.0000000000000000	0.0000000000000000	0.2089729460000029
0.5000000000000000	0.5000000000000000	0.7089728710000003
0.0000000000000000	0.5000000000000000	0.4589728710000003
0.5000000000000000	0.0000000000000000	0.9589728710000003
0.5000000000000000	0.0000000000000000	0.5410271289999997
0.0000000000000000	0.5000000000000000	0.04102709499999969
0.5000000000000000	0.5000000000000000	0.2910271289999997
0.0000000000000000	0.0000000000000000	0.7910271289999997

10. TiO_2 PBEsol-D3 U=3

Ti O2

```
1.0000000000000000
3.8034222126000001 0.0000000000000000 0.0000000000000000
0.0000000000000000 3.8034222126000001 0.0000000000000000
0.0000000000000000 0.0000000000000000 9.4984664917000003
```

Ti O

4 8

Direct

```
0.0000000000000000 0.0000000000000000 0.0000000000000000
0.5000000000000000 0.5000000000000000 0.5000000000000000
0.0000000000000000 0.5000000000000000 0.2500000000000000
0.5000000000000000 0.0000000000000000 0.7500000000000000
0.0000000000000000 0.0000000000000000 0.2089217159999990
0.5000000000000000 0.5000000000000000 0.7089216110000010
0.0000000000000000 0.5000000000000000 0.4589216410000034
0.5000000000000000 0.0000000000000000 0.9589216110000010
0.5000000000000000 0.0000000000000000 0.5410783889999990
0.0000000000000000 0.5000000000000000 0.0410783330000015
0.5000000000000000 0.5000000000000000 0.2910783589999966
0.0000000000000000 0.0000000000000000 0.7910783889999990
```

11. TiO_2 PBEsol-D3 U=4

Ti O2

```
1.0000000000000000
```

3.8157105445999999	0.0000000000000000	0.0000000000000000
0.0000000000000000	3.8157105445999999	0.0000000000000000
0.0000000000000000	0.0000000000000000	9.5184736252000004

Ti O

4 8

Direct

0.0000000000000000	0.0000000000000000	0.0000000000000000
0.5000000000000000	0.5000000000000000	0.5000000000000000
0.0000000000000000	0.5000000000000000	0.2500000000000000
0.5000000000000000	0.0000000000000000	0.7500000000000000
0.0000000000000000	0.0000000000000000	0.20885796799999967
0.5000000000000000	0.5000000000000000	0.70885783399999998
0.0000000000000000	0.5000000000000000	0.45885786400000023
0.5000000000000000	0.0000000000000000	0.95885783399999998
0.5000000000000000	0.0000000000000000	0.54114216600000002
0.0000000000000000	0.5000000000000000	0.04114209499999979
0.5000000000000000	0.5000000000000000	0.29114213599999977
0.0000000000000000	0.0000000000000000	0.79114216600000002

12. TiO₂ PBEsol-D3 U=6

Ti O2

1.0000000000000000		
3.8393427294256446	0.0000000000000000	0.0000000000000000
0.0000000000000000	3.8393427294256446	0.0000000000000000
0.0000000000000000	-0.0000000000000000	9.5641177735926011

Ti O

4 8

Direct

-0.0000000000000000	0.0000000000000000	-0.0000000000000000
---------------------	--------------------	---------------------

```

0.5000000000000000 0.5000000000000000 0.5000000000000000
-0.0000000000000000 0.5000000000000000 0.2500000000000000
0.5000000000000000 0.0000000000000000 0.7500000000000000
-0.0000000000000000 -0.0000000000000000 0.2087070713995634
0.5000000000000000 0.5000000000000000 0.7087068623995639
-0.0000000000000000 0.5000000000000000 0.4587070113995585
0.5000000000000000 -0.0000000000000000 0.9587068623995639
0.5000000000000000 -0.0000000000000000 0.5412931376004361
0.0000000000000000 0.5000000000000000 0.0412929846004412
0.5000000000000000 0.5000000000000000 0.2912929886004415
0.0 -0.0000000000000000 0.7912931376004361

```

Table S3. Optimized geometries for TiO₂ with different U values.

<i>Method</i> <i>Hubbard U value</i>	<i>a</i> (Å)	<i>PBEsol</i> <i>c</i> (Å)	<i>Vol</i> (Å ³)	<i>a</i> (Å)	<i>PBEsol- D3</i> <i>c</i> (Å)	<i>Vol</i> (Å ³)
0	3.76	9.46	133.96	3.76	9.46	133.96
1	3.79	9.57	137.21	3.78	9.47	135.08
2	3.80	9.58	138.36	3.79	9.48	136.23
3	3.81	9.59	139.51	3.80	9.50	137.41
4	3.83	9.61	140.67	3.82	9.52	138.59
6	3.85	9.64	143.03	3.84	9.56	140.98
Experimental value	3.78	9.51	136.27	3.78	9.51	136.27

III. Converged geometries of Ti₂O₃

1. Ti₂O₃ PBEsol U=0

Ti4 O6

```

1.0000000000000000
5.4642519917672097 0.0013344319898459 0.0009107456149114
3.1343915680578145 4.4758955648586687 0.0009107456147785
3.1343915680578012 1.6320471772754752 4.1677408685983188

```

Ti O

4 6

Direct

0.3454939964066505 0.3454941024066522 0.3454941514066527
0.1545058835933538 0.1545058735933530 0.1545058465933472
0.6545054145933470 0.6545057235933477 0.6545060455933530
0.8454945104066504 0.8454939934066467 0.8454941644066502
0.9381278928058702 0.5618719931941275 0.2499999489999993
0.5618718761941285 0.2500000349999993 0.9381279568058684
0.2500001040000015 0.9381278468058735 0.5618720221941264
0.0618719721941293 0.4381277678058705 0.7500001339999969
0.4381283888058686 0.7499999389999985 0.0618719811941265
0.7500000200000017 0.0618719981941315 0.4381278298058685

2. Ti_2O_3 PBEsol U=1

Ti4 O6

1.000000000000000
5.4581862984483136 0.0004643471059587 0.0003188020878418
3.0610642566751234 4.5190356825129410 0.0003188020879977
3.0610642566751234 1.6239081019411896 4.2171798726059277

Ti O

4 6

Direct

0.3437001333189599 0.3437006083189602 0.3437003373189626
0.1562995956810355 0.1562996046810398 0.1562996026810396
0.6562999316810348 0.6562999756810385 0.6562994016810336
0.8437003593189644 0.8437006203189611 0.8437006903189669
0.9352501198109636 0.5647498731890394 0.2499999209999970
0.5647500341890349 0.2499998400000010 0.9352498258109606
0.2499998850000011 0.9352504138109666 0.5647499251890366
0.0647502771890374 0.4352498778109647 0.7500002170000002

0.4352499328109657 0.7500004070000017 0.0647501121890344
 0.7500004540000020 0.0647501801890400 0.4352497858109642

3. Ti_2O_3 PBEsol U=2

Ti4 O6

1.000000000000000
 5.4581862984483136 0.0004643471059587 0.0003188020878418
 3.0610642566751234 4.5190356825129410 0.0003188020879977
 3.0610642566751234 1.6239081019411896 4.2171798726059277

Ti O

4 6

Direct

0.3437001333189599 0.3437006083189602 0.3437003373189626
 0.1562995956810355 0.1562996046810398 0.1562996026810396
 0.6562999316810348 0.6562999756810385 0.6562994016810336
 0.8437003593189644 0.8437006203189611 0.8437006903189669
 0.9352501198109636 0.5647498731890394 0.2499999209999970
 0.5647500341890349 0.2499998400000010 0.9352498258109606
 0.2499998850000011 0.9352504138109666 0.5647499251890366
 0.0647502771890374 0.4352498778109647 0.7500002170000002
 0.4352499328109657 0.7500004070000017 0.0647501121890344
 0.7500004540000020 0.0647501801890400 0.4352497858109642

4. Ti_2O_3 PBEsol U=3

Ti4 O6

1.000000000000000

5.4399007184043562 -0.0016528807938532 -0.0011411752877801

2.9848474874807880 4.5478795096712599 -0.0011411752875760

2.9848464284518750 1.6107055053492030 4.2530956146294567

Ti O

4 6

Direct

0.3427942868178331 0.3427945928178371 0.3427944398178351

0.1572055691821691 0.1572054591821671 0.1572055581821647

0.6572059871821683 0.6572057781821687 0.6572054711821682

0.8427944568178329 0.8427946828178303 0.8427951138178340

0.9343294244215328 0.5656707495784674 0.24999989999999988

0.5656712935784698 0.2499996940000031 0.9343287934215267

0.2499998669999997 0.9343289934215291 0.5656712285784680

0.0656715295784681 0.4343285984215283 0.7500005189999968

0.4343287954215268 0.7500003870000000 0.0656713435784740

0.7499999269999975 0.0656713415784739 0.4343287104215304

5. Ti_2O_3 PBEsol U=4

Ti4 O6

1.000000000000000

5.4334430732223202 -0.0007976099546275 -0.0005531206441553

2.9315567769540056 4.5747436135183728 -0.0005531206442028

2.9315583091404851 1.6029634969998634 4.2847145148939241

Ti O

4 6

Direct

0.3424327826993722 0.3424330126993699 0.3424330096993732

0.1575670913006316 0.1575670163006289 0.1575671253006273
0.6575674993006299 0.6575672913006269 0.6575670073006247
0.8424329696993699 0.8424333866993724 0.8424332846993711
0.9342825119310670 0.5657175640689321 0.2499989900000023
0.5657181320689294 0.2499997279999988 0.9342821169310663
0.2499996900000028 0.9342821809310716 0.5657183430689291
0.0657181680689323 0.4342819049310702 0.7500007060000016
0.4342823229310693 0.7500003299999989 0.0657181530689346
0.7500002210000005 0.0657180900689330 0.4342820659310658

6. Ti_2O_3 PBEsol U=6

Ti4 O6

1.000000000000000

5.4363960045795681 0.0022380481373034 0.0015626690242016
2.8593052092985305 4.6237193088848283 0.0015626690238983
2.8593067570147030 1.5944440122869035 4.3401062363304312

Ti O

4 6

Direct

0.3424307268039963 0.3424309358039958 0.3424309688039950
0.1575691641960054 0.1575690691960082 0.1575692151960061
0.6575696441960095 0.6575692911960052 0.6575690691960081
0.8424308468039921 0.8424313178039919 0.8424312648039911
0.9348931415645642 0.5651069104354330 0.2499989900000023
0.5651074574354321 0.2499996829999986 0.9348928205645625
0.2499997039999968 0.9348926075645626 0.5651077334354336
0.0651075054354363 0.4348924655645648 0.7500008020000024
0.4348928515645612 0.7500003239999984 0.0651075564354370
0.7500001619999992 0.0651074684354368 0.4348927465645632

7. Ti_2O_3 PBEsol-D3 U=0

Ti4 O6

```
1.0000000000000000
5.4294943809999996 0.0000000000000000 0.0000000000000000
3.1133676909000001 4.4481851190999997 0.0000000000000000
3.1133676909000001 1.6211002490999999 4.1422680786999999
```

Ti O

4 6

Direct

```
0.3456154570000010 0.3456155630000026 0.3456156120000031
0.1543844230000033 0.1543844130000025 0.1543843859999967
0.6543839539999965 0.6543842629999972 0.6543845850000025
0.8456159710000009 0.8456154539999972 0.8456156250000006
0.9375987129999999 0.5624011729999978 0.2499999489999993
0.5624010559999988 0.2500000349999993 0.9375987769999981
0.2500001040000015 0.9375986670000032 0.5624012019999967
0.0624011519999996 0.4375985880000002 0.7500001339999969
0.4375992089999983 0.7499999389999985 0.0624011609999968
0.7500000200000017 0.0624011780000018 0.4375986499999982
```

8. Ti_2O_3 PBEsol-D3 U=1

Ti4 O6

```
1.0000000000000000
5.4243292809000003 0.0000000000000000 0.0000000000000000
3.0416944504000001 4.4912629645999997 0.0000000000000000
3.0416944504000001 1.6136323342000001 4.1913761114000003
```

Ti O

4 6

Direct

0.3438728029999965 0.3438732779999967 0.3438730069999991
0.1561269259999989 0.1561269350000032 0.1561269330000030
0.6561272619999983 0.6561273060000019 0.6561267319999970
0.8438730499999991 0.8438733099999993 0.8438733030000023
0.9346486880000029 0.5653512820000017 0.2499999209999970
0.5653514660000027 0.2499998930000018 0.9346483639999974
0.2499999140000000 0.9346490579999980 0.5653513869999998
0.0653517590000021 0.4346484360000034 0.7500001599999990
0.4346484710000027 0.7500004070000017 0.0653515739999975
0.7500004640000029 0.0653516530000005 0.4346482959999989

9. Ti_2O_3 PBEsol-D3 U=2

Ti4 O6

1.000000000000000

5.4243292809000003 0.0000000000000000 0.0000000000000000

3.0416944504000001 4.4912629645999997 0.0000000000000000

3.0416944504000001 1.6136323342000001 4.1913761114000003

Ti O

4 6

Direct

0.3438728029999965 0.3438732779999967 0.3438730069999991
0.1561269259999989 0.1561269350000032 0.1561269330000030
0.6561272619999983 0.6561273060000019 0.6561267319999970
0.8438730499999991 0.8438733099999993 0.8438733030000023
0.9346486880000029 0.5653512820000017 0.2499999209999970
0.5653514660000027 0.2499998930000018 0.9346483639999974

0.2499999140000000 0.9346490579999980 0.5653513869999998
 0.0653517590000021 0.4346484360000034 0.7500001599999990
 0.4346484710000027 0.7500004070000017 0.0653515739999975
 0.7500004640000029 0.0653516530000005 0.4346482959999989

10. Ti_2O_3 PBEsol-D3 U=3

Ti4 O6

1.000000000000000
 5.4080031974775018 -0.0130688330168708 -0.0090055760720658
 2.9796361468976977 4.5131405707170336 -0.0090055760721928
 2.9796350979098336 1.5986109013787804 4.2205387941581103

Ti O

4 6

Direct

0.3430037870810937 0.3430040920810941 0.3430038890810951
 0.1569960909189033 0.1569959789189012 0.1569960689189015
 0.6569965129189028 0.6569963429189030 0.6569959429189054
 0.8430039500810964 0.8430042160810971 0.8430045120811003
 0.9335776354012127 0.5664225365987873 0.2499998870000013
 0.5664231265987864 0.2499997629999982 0.9335769124012133
 0.2499999560000035 0.9335772484012127 0.5664229775987847
 0.0664233025987867 0.4335768724012171 0.7500004529999984
 0.4335770154012183 0.7500004429999976 0.0664231175987820
 0.7499999939999995 0.0664231265987863 0.4335769114012168

11. Ti_2O_3 PBEsol-D3 U=4

Ti4 O6

1.0000000000000000

5.4005017281000001 0.0000000000000000 0.0000000000000000

2.9144510441000002 4.5465804761999999 0.0000000000000000

2.9144525576000002 1.5936101455000000 4.2581441859000000

Ti O

4 6

Direct

0.3426854120000016 0.3426856789999988 0.3426856230000013

0.1573144780000035 0.1573144030000009 0.1573145119999992

0.6573149049999998 0.6573146969999968 0.6573143379999991

0.8426855829999980 0.8426860000000005 0.8426858979999992

0.9335881089999987 0.5664119670000005 0.2499998990000023

0.5664125549999994 0.2499997480000005 0.9335876580000004

0.2499996900000028 0.9335877780000033 0.5664127459999975

0.0664125899999988 0.4335875220000034 0.7500006499999969

0.4335879200000008 0.7500003299999989 0.0664125560000031

0.7500003190000015 0.0664125030000022 0.4335876350000021

12. Ti_2O_3 PBEsol-D3 U=6

Ti4 O6

1.0000000000000000

5.6212225725637550 -0.0003204180604673 -0.0002179030404288

3.2663941973264299 4.5748018822344862 -0.0002179030404364

3.2663936431801330 1.6812220375613252 4.2546795023393162

Ti O

4 6

Direct

0.3517274588797734 0.3517278208797749 0.3517279588797721

0.1482721911202261 0.1482721561202268 0.1482723321202271
0.6482725691202289 0.6482722661202287 0.6482722591202246
0.8517277898797759 0.8517282418797707 0.8517284598797745
0.9508552520878701 0.5491449609121297 0.2499998859999977
0.5491450459121332 0.2499996139999965 0.9508552690878680
0.2499993260000011 0.9508550480878675 0.5491453949121301
0.0491451809121338 0.4508548580878730 0.7500007800000006
0.4508549770878722 0.7500003019999966 0.0491452749121273
0.7500000750000027 0.0491451649121324 0.4508550470878709

Table S4. Optimized geometries for Ti_2O_3 with different U values.

<i>Method Hubbard U value</i>	<i>a(Å)</i>	<i>PBEsol $\alpha(^{\circ})$</i>	<i>Vol(Å³)</i>	<i>a(Å)</i>	<i>PBEsol- D3 $\alpha(^{\circ})$</i>	<i>Vol(Å³)</i>
0	5.46	54.98	100.04	5.43	55.01	100.04
1	5.43	55.01	101.90	5.43	55.31	101.04
2	5.46	55.88	104.01	5.42	55.89	102.11
3	5.44	56.74	105.26	5.41	56.71	103.33
4	5.43	57.36	106.52	5.40	57.34	104.55
6	5.44	58.24	109.04	5.40	58.29	107.02
Experimental value	5.43	56.58	104.32	5.43	56.58	104.32

IV. Calculation parameters

INCAR TiO_2 U=3

Full optimization after preoptimization by following the procedure described in section I.

Basic setup:

ISPIN = 2

ISTART = 1

ICHARG = 1

Accuracy controls:

PREC = Accurate

Electronic loop controls:

ALGO = Fast

EDIFF = 0.000001

ENCUT = 600

NELM = 200

NELMIN = 5

NELMDL = -10

MAXMIX = -100

ISMear = 0

SIGMA = 0.05

Relaxation control:

IBRION = 1 # Conjugate gradients

NSW = 50

ISIF = 3 # Ions

EDIFFG = -0.01

Properties:

LCHARG = .TRUE.

LWAVE = .TRUE.

LELF = .FALSE.

LVTOT = .FALSE.

LVHAR = .FALSE.

GGA = PS

LDAU = .TRUE.

HUBBARD

LDAUU = 3.00 0.00

LDAUJ = 0.00 0.00

LDAUL = 2 -1

LDAUPRINT = 1

LMAXMIX = 4

LASPH = .TRUE.

V. TiO₂ (001) anatase surface

Ti O

1.0000000000000000

15.213699999999993 0.0000000000000000 0.0000000000000000

0.0000000000000000 15.213699999999993 0.0000000000000000

0.0000000000000000 0.0000000000000000 29.0000000000000000

Ti O

64 128

Selective dynamics

Direct

0.0000000000000000	0.0000000000000000	0.2750532313799594	T	T	T
0.0000000000000000	0.2499998170000026	0.2750532313799594	T	T	T
0.0000000000000000	0.4999996339999981	0.2750532313799594	T	T	T
-0.0000000000000000	0.7499994499999971	0.2750532313799594	T	T	T
0.2499998170000026	-0.0000000000000000	0.2750532313799594	T	T	T
0.2499998170000026	0.2499998170000026	0.2750532313799594	T	T	T
0.2499998170000026	0.4999996339999981	0.2750532313799594	T	T	T
0.2499998170000026	0.7499994499999971	0.2750532313799594	T	T	T
0.4999996339999981	0.0000000000000000	0.2750532313799594	T	T	T
0.4999996339999981	0.2499998170000026	0.2750532313799594	T	T	T
0.4999996339999981	0.4999996339999981	0.2750532313799594	T	T	T
0.4999996339999981	0.7499994499999971	0.2750532313799594	T	T	T
0.7499994499999971	-0.0000000000000000	0.2750532313799594	T	T	T
0.7499994499999971	0.2499998170000026	0.2750532313799594	T	T	T
0.7499994499999971	0.4999996339999981	0.2750532313799594	T	T	T
0.7499994499999971	0.7499994499999971	0.2750532313799594	T	T	T
0.1249999079999995	0.1249999079999995	0.1119448770623885	T	T	T
0.1249999079999995	0.3749997250000021	0.1119448770623885	T	T	T

0.1249999079999995	0.6249995419999976	0.1119448770623885	T	T	T
0.1249999079999995	0.8749993590000003	0.1119448770623885	T	T	T
0.3749997250000021	0.1249999079999995	0.1119448770623885	T	T	T
0.3749997250000021	0.3749997250000021	0.1119448770623885	T	T	T
0.3749997250000021	0.6249995419999976	0.1119448770623885	T	T	T
0.3749997250000021	0.8749993590000003	0.1119448770623885	T	T	T
0.6249995419999976	0.1249999079999995	0.1119448770623885	T	T	T
0.6249995419999976	0.3749997250000021	0.1119448770623885	T	T	T
0.6249995419999976	0.6249995419999976	0.1119448770623885	T	T	T
0.6249995419999976	0.8749993590000003	0.1119448770623885	T	T	T
0.8749993590000003	0.1249999079999995	0.1119448770623885	T	T	T
0.8749993590000003	0.3749997250000021	0.1119448770623885	T	T	T
0.8749993590000003	0.6249995419999976	0.1119448770623885	T	T	T
0.8749993590000003	0.8749993590000003	0.1119448770623885	T	T	T
0.0000000000000000	0.1249999079999995	0.0301591937929970	F	F	F
0.0000000000000000	0.3749997250000021	0.0301591937929970	F	F	F
0.0000000000000000	0.6249995419999976	0.0301591937929970	F	F	F
0.0000000000000000	0.8749993590000003	0.0301591937929970	F	F	F
0.2499998170000026	0.1249999079999995	0.0301591937929970	F	F	F
0.2499998170000026	0.3749997250000021	0.0301591937929970	F	F	F
0.2499998170000026	0.6249995419999976	0.0301591937929970	F	F	F
0.2499998170000026	0.8749993590000003	0.0301591937929970	F	F	F
0.4999996339999981	0.1249999079999995	0.0301591937929970	F	F	F
0.4999996339999981	0.3749997250000021	0.0301591937929970	F	F	F
0.4999996339999981	0.6249995419999976	0.0301591937929970	F	F	F
0.4999996339999981	0.8749993590000003	0.0301591937929970	F	F	F
0.7499994499999971	0.1249999079999995	0.0301591937929970	F	F	F
0.7499994499999971	0.3749997250000021	0.0301591937929970	F	F	F
0.7499994499999971	0.6249995419999976	0.0301591937929970	F	F	F
0.7499994499999971	0.8749993590000003	0.0301591937929970	F	F	F
0.1249999079999995	0.0000000000000000	0.1944816089138053	T	T	T
0.1249999079999995	0.2499998170000026	0.1944816089138053	T	T	T

0.1249999079999995	0.4999996339999981	0.1944816089138053	T	T	T
0.1249999079999995	0.7499994499999971	0.1944816089138053	T	T	T
0.3749997250000021	-0.0000000000000000	0.1944816089138053	T	T	T
0.3749997250000021	0.2499998170000026	0.1944816089138053	T	T	T
0.3749997250000021	0.4999996339999981	0.1944816089138053	T	T	T
0.3749997250000021	0.7499994499999971	0.1944816089138053	T	T	T
0.6249995419999976	0.0000000000000000	0.1944816089138053	T	T	T
0.6249995419999976	0.2499998170000026	0.1944816089138053	T	T	T
0.6249995419999976	0.4999996339999981	0.1944816089138053	T	T	T
0.6249995419999976	0.7499994499999971	0.1944816089138053	T	T	T
0.8749993590000003	-0.0000000000000000	0.1944816089138053	T	T	T
0.8749993590000003	0.2499998170000026	0.1944816089138053	T	T	T
0.8749993590000003	0.4999996339999981	0.1944816089138053	T	T	T
0.8749993590000003	0.7499994499999971	0.1944816089138053	T	T	T
0.0000000000000000	0.0000000000000000	0.0167046872410026	F	F	F
0.0000000000000000	0.2499998170000026	0.0167046872410026	F	F	F
0.0000000000000000	0.4999996339999981	0.0167046872410026	F	F	F
0.0000000000000000	0.7499994499999971	0.0167046872410026	F	F	F
0.2499998170000026	0.0000000000000000	0.0167046872410026	F	F	F
0.2499998170000026	0.2499998170000026	0.0167046872410026	F	F	F
0.2499998170000026	0.4999996339999981	0.0167046872410026	F	F	F
0.2499998170000026	0.7499994499999971	0.0167046872410026	F	F	F
0.4999996339999981	0.0000000000000000	0.0167046872410026	F	F	F
0.4999996339999981	0.2499998170000026	0.0167046872410026	F	F	F
0.4999996339999981	0.4999996339999981	0.0167046872410026	F	F	F
0.4999996339999981	0.7499994499999971	0.0167046872410026	F	F	F
0.7499994499999971	0.0000000000000000	0.0167046872410026	F	F	F
0.7499994499999971	0.2499998170000026	0.0167046872410026	F	F	F
0.7499994499999971	0.4999996339999981	0.0167046872410026	F	F	F
0.7499994499999971	0.7499994499999971	0.0167046872410026	F	F	F
0.1249999079999995	0.1249999079999995	0.1803623868732818	T	T	T
0.1249999079999995	0.3749997250000021	0.1803623868732818	T	T	T

0.1249999079999995	0.6249995419999976	0.1803623868732818	T	T	T
0.1249999079999995	0.8749993590000003	0.1803623868732818	T	T	T
0.3749997250000021	0.1249999079999995	0.1803623868732818	T	T	T
0.3749997250000021	0.3749997250000021	0.1803623868732818	T	T	T
0.3749997250000021	0.6249995419999976	0.1803623868732818	T	T	T
0.3749997250000021	0.8749993590000003	0.1803623868732818	T	T	T
0.6249995419999976	0.1249999079999995	0.1803623868732818	T	T	T
0.6249995419999976	0.3749997250000021	0.1803623868732818	T	T	T
0.6249995419999976	0.6249995419999976	0.1803623868732818	T	T	T
0.6249995419999976	0.8749993590000003	0.1803623868732818	T	T	T
0.8749993590000003	0.1249999079999995	0.1803623868732818	T	T	T
0.8749993590000003	0.3749997250000021	0.1803623868732818	T	T	T
0.8749993590000003	0.6249995419999976	0.1803623868732818	T	T	T
0.8749993590000003	0.8749993590000003	0.1803623868732818	T	T	T
0.0000000000000000	0.1249999079999995	0.0985879896550017	F	F	F
0.0000000000000000	0.3749997250000021	0.0985879896550017	F	F	F
0.0000000000000000	0.6249995419999976	0.0985879896550017	F	F	F
0.0000000000000000	0.8749993590000003	0.0985879896550017	F	F	F
0.2499998170000026	0.1249999079999995	0.0985879896550017	F	F	F
0.2499998170000026	0.3749997250000021	0.0985879896550017	F	F	F
0.2499998170000026	0.6249995419999976	0.0985879896550017	F	F	F
0.2499998170000026	0.8749993590000003	0.0985879896550017	F	F	F
0.4999996339999981	0.1249999079999995	0.0985879896550017	F	F	F
0.4999996339999981	0.3749997250000021	0.0985879896550017	F	F	F
0.4999996339999981	0.6249995419999976	0.0985879896550017	F	F	F
0.4999996339999981	0.8749993590000003	0.0985879896550017	F	F	F
0.7499994499999971	0.1249999079999995	0.0985879896550017	F	F	F
0.7499994499999971	0.3749997250000021	0.0985879896550017	F	F	F
0.7499994499999971	0.6249995419999976	0.0985879896550017	F	F	F
0.7499994499999971	0.8749993590000003	0.0985879896550017	F	F	F
0.1249999079999995	0.0000000000000000	0.2624964526750593	T	T	T
0.1249999079999995	0.2499998170000026	0.2624964526750593	T	T	T

0.1249999079999995	0.4999996339999981	0.2624964526750593	T	T	T
0.1249999079999995	0.7499994499999971	0.2624964526750593	T	T	T
0.3749997250000021	-0.0000000000000000	0.2624964526750593	T	T	T
0.3749997250000021	0.2499998170000026	0.2624964526750593	T	T	T
0.3749997250000021	0.4999996339999981	0.2624964526750593	T	T	T
0.3749997250000021	0.7499994499999971	0.2624964526750593	T	T	T
0.6249995419999976	-0.0000000000000000	0.2624964526750593	T	T	T
0.6249995419999976	0.2499998170000026	0.2624964526750593	T	T	T
0.6249995419999976	0.4999996339999981	0.2624964526750593	T	T	T
0.6249995419999976	0.7499994499999971	0.2624964526750593	T	T	T
0.8749993590000003	0.0000000000000000	0.2624964526750593	T	T	T
0.8749993590000003	0.2499998170000026	0.2624964526750593	T	T	T
0.8749993590000003	0.4999996339999981	0.2624964526750593	T	T	T
0.8749993590000003	0.7499994499999971	0.2624964526750593	T	T	T
0.1249999079999995	-0.0000000000000000	0.1260453038172506	T	T	T
0.1249999079999995	0.2499998170000026	0.1260453038172506	T	T	T
0.1249999079999995	0.4999996339999981	0.1260453038172506	T	T	T
0.1249999079999995	0.7499994499999971	0.1260453038172506	T	T	T
0.3749997250000021	-0.0000000000000000	0.1260453038172506	T	T	T
0.3749997250000021	0.2499998170000026	0.1260453038172506	T	T	T
0.3749997250000021	0.4999996339999981	0.1260453038172506	T	T	T
0.3749997250000021	0.7499994499999971	0.1260453038172506	T	T	T
0.6249995419999976	-0.0000000000000000	0.1260453038172506	T	T	T
0.6249995419999976	0.2499998170000026	0.1260453038172506	T	T	T
0.6249995419999976	0.4999996339999981	0.1260453038172506	T	T	T
0.6249995419999976	0.7499994499999971	0.1260453038172506	T	T	T
0.8749993590000003	0.0000000000000000	0.1260453038172506	T	T	T
0.8749993590000003	0.2499998170000026	0.1260453038172506	T	T	T
0.8749993590000003	0.4999996339999981	0.1260453038172506	T	T	T
0.8749993590000003	0.7499994499999971	0.1260453038172506	T	T	T
-0.0000000000000000	0.1249999079999995	0.2916580201061817	T	T	T
0.0000000000000000	0.3749997250000021	0.2916580201061817	T	T	T

0.0000000000000000	0.6249995419999976	0.2916580201061817	T	T	T
-0.0000000000000000	0.8749993590000003	0.2916580201061817	T	T	T
0.2499998170000026	0.1249999079999995	0.2916580201061817	T	T	T
0.2499998170000026	0.3749997250000021	0.2916580201061817	T	T	T
0.2499998170000026	0.6249995419999976	0.2916580201061817	T	T	T
0.2499998170000026	0.8749993590000003	0.2916580201061817	T	T	T
0.4999996339999981	0.1249999079999995	0.2916580201061817	T	T	T
0.4999996339999981	0.3749997250000021	0.2916580201061817	T	T	T
0.4999996339999981	0.6249995419999976	0.2916580201061817	T	T	T
0.4999996339999981	0.8749993590000003	0.2916580201061817	T	T	T
0.7499994499999971	0.1249999079999995	0.2916580201061817	T	T	T
0.7499994499999971	0.3749997250000021	0.2916580201061817	T	T	T
0.7499994499999971	0.6249995419999976	0.2916580201061817	T	T	T
0.7499994499999971	0.8749993590000003	0.2916580201061817	T	T	T
0.1249999079999995	0.1249999079999995	0.0436137220689972	F	F	F
0.1249999079999995	0.3749997250000021	0.0436137220689972	F	F	F
0.1249999079999995	0.6249995419999976	0.0436137220689972	F	F	F
0.1249999079999995	0.8749993590000003	0.0436137220689972	F	F	F
0.3749997250000021	0.1249999079999995	0.0436137220689972	F	F	F
0.3749997250000021	0.3749997250000021	0.0436137220689972	F	F	F
0.3749997250000021	0.6249995419999976	0.0436137220689972	F	F	F
0.3749997250000021	0.8749993590000003	0.0436137220689972	F	F	F
0.6249995419999976	0.1249999079999995	0.0436137220689972	F	F	F
0.6249995419999976	0.3749997250000021	0.0436137220689972	F	F	F
0.6249995419999976	0.6249995419999976	0.0436137220689972	F	F	F
0.6249995419999976	0.8749993590000003	0.0436137220689972	F	F	F
0.8749993590000003	0.1249999079999995	0.0436137220689972	F	F	F
0.8749993590000003	0.3749997250000021	0.0436137220689972	F	F	F
0.8749993590000003	0.6249995419999976	0.0436137220689972	F	F	F
0.8749993590000003	0.8749993590000003	0.0436137220689972	F	F	F
-0.0000000000000000	0.0000000000000000	0.2082683807298407	T	T	T
-0.0000000000000000	0.2499998170000026	0.2082683807298407	T	T	T

0.0000000000000000	0.4999996339999981	0.2082683807298407	T	T	T
0.0000000000000000	0.7499994499999971	0.2082683807298407	T	T	T
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0.2499998170000026	0.2499998170000026	0.2082683807298407	T	T	T
0.2499998170000026	0.4999996339999981	0.2082683807298407	T	T	T
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0.4999996339999981	0.0000000000000000	0.2082683807298407	T	T	T
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0.4999996339999981	0.4999996339999981	0.2082683807298407	T	T	T
0.4999996339999981	0.7499994499999971	0.2082683807298407	T	T	T
0.7499994499999971	-0.0000000000000000	0.2082683807298407	T	T	T
0.7499994499999971	0.2499998170000026	0.2082683807298407	T	T	T
0.7499994499999971	0.4999996339999981	0.2082683807298407	T	T	T
0.7499994499999971	0.7499994499999971	0.2082683807298407	T	T	T

VI. Geometries comparison

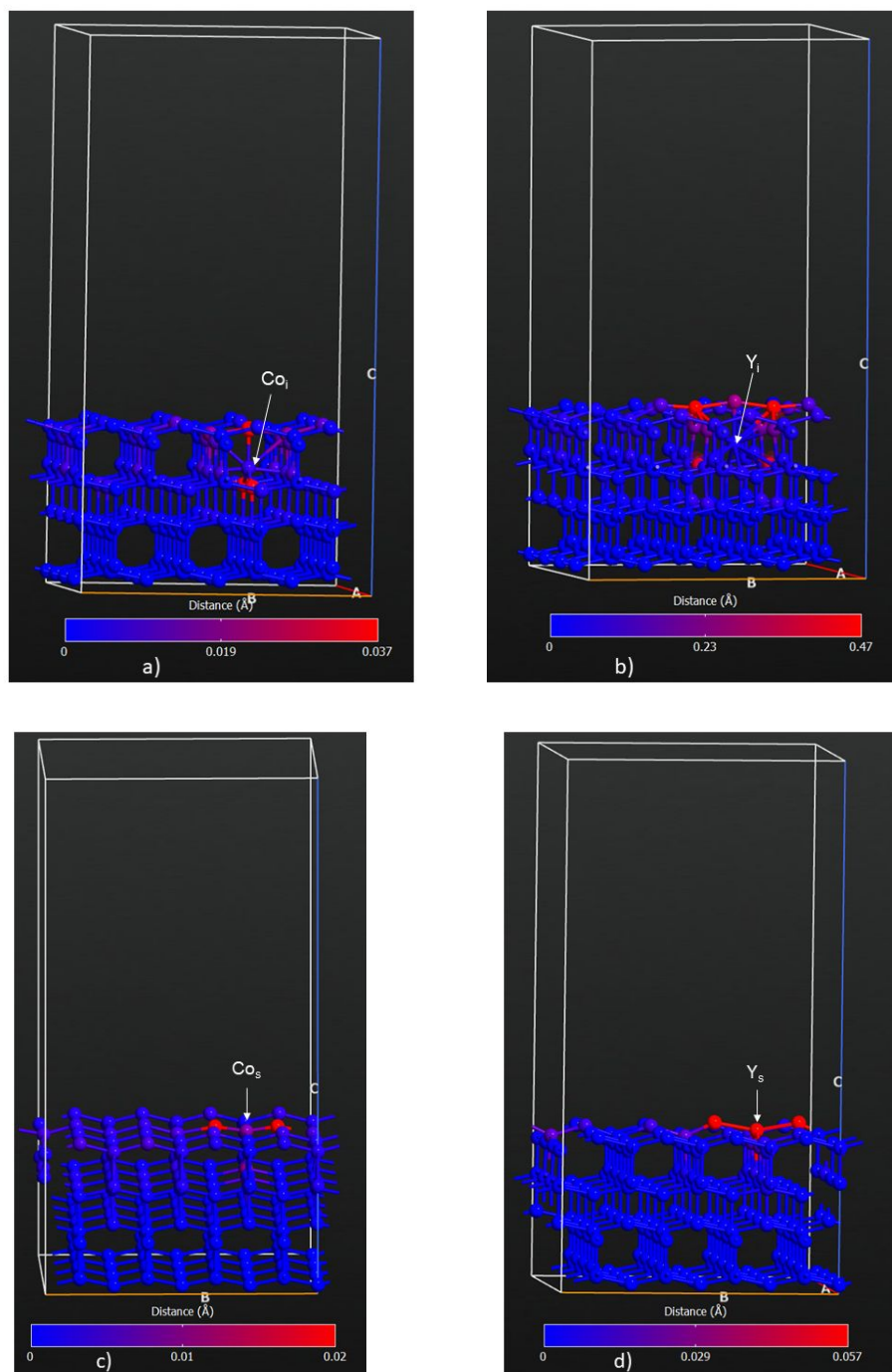


Figure S3. Geometries comparison between U=0 and U=3 optimized geometries for cobalt and yttrium interstitially doped (a and b, respectively) TiO_2 (001) anatase surface. The substitutional Co and Y doped structures are shown in c and d. Red in the color gradient and in the TiO_2 surface shows the highest change in the bond distances.

VII. CO₂ adsorption energy over the TiO₂(001) anatase surface

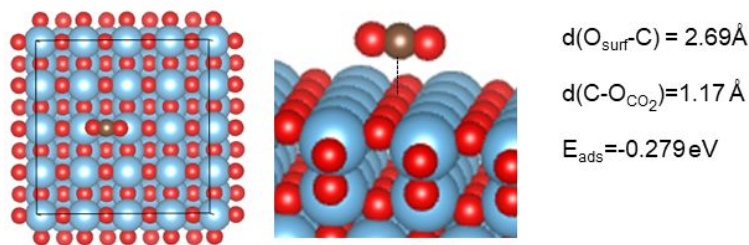


Figure S4. Adsorption of a CO₂ molecule over a TiO₂ (001) surface, some geometry parameters are presented.

The adsorption energy (E_{ads}) of a CO₂ molecule over a TiO₂ (001) surface was computed at PBEsol-D3(BJ) with $U=3$ in a similar configuration as that reported by Araujo et al.¹ The adsorption energy is in agreement with that previously reported by Araujo et al.¹ and Huygh et al.²

VIII. DOS plot of the pristine TiO₂(001) anatase

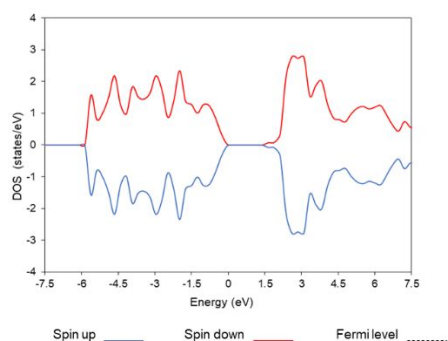


Figure S5. Density of states plot of the TiO₂ (001) anatase pristine surface.

References

- (1) Araujo-Lopez, E.; Varilla, L. A.; Seriani, N.; Montoya, J. A. TiO₂ Anatase's Bulk and (001) Surface, Structural and Electronic Properties: A DFT Study on the Importance of Hubbard and van Der Waals Contributions. *Surf. Sci.* **2016**, *653*, 187–196. <https://doi.org/10.1016/j.susc.2016.07.003>.
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