## Supporting Information

## From order to disorder: Computational design of triblock amphiphiles with 1-nm domains

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## Additional Details on the Force Field and Calculation of Structure Factors

The parameters for non-bonded Lennard-Jones (LJ) and Coulomb interactions taken from the TraPPE-UA force field ${ }^{1-4}$ are listed in Table S1. Here, $\mathrm{CH}_{q}$ groups are presented as pseudo-atoms, whereas the polar hydrogen belonging to a hydroxyl group is modelled explicitly, but does not carry a LJ site.
A short-range repulsive potential is applied for 1-5 interactions between hydrogen and oxygen atoms in hydroxyl groups that are separated by four bonds, to control the strength of the intramolecular H -bond for neighboring hydroxyl groups that do not involve a 1-4 O-O LJ interaction but a 1-4 Coulomb interactions scaled by a factor of $0.5 .^{3}$ The repulsive potential $U_{\text {repulsive }}\left(r_{i j}\right)$ is as follows:

$$
\begin{equation*}
U_{\text {repulsive }}\left(r_{i j}\right) / k_{\mathrm{B}}=\frac{7.5 \times 10^{7} \mathrm{~K} \cdot \AA^{12}}{r_{i j}^{12}} \tag{S1}
\end{equation*}
$$

where $r_{\mathrm{ij}}$ is the 1-5 distance between hydrogen and oxygen atoms.
The other bonded interactions include bond stretching, angle bending, and torsional potentials. The corresponding interaction parameters are listed in Table S2, and the following functional forms are implemented to calculate the potentials:

$$
\begin{gather*}
u_{\text {stretching }}(r)=\frac{k_{\mathrm{s}}}{2}\left(r-r_{0}\right)^{2}  \tag{S2}\\
u_{\text {bending }}(\theta)=\frac{k_{\mathrm{b}}}{2}\left(\theta-\theta_{0}\right)^{2}  \tag{S3}\\
u_{\text {torsion }}(\phi)=c_{0}+c_{1}[1+\cos (\phi)]+c_{2}[1-\cos (2 \phi)]+c_{3}[1+\cos (3 \phi)] \tag{S4}
\end{gather*}
$$

In the standard TraPPE-UA force field used for Monte Carlo simulations, the bond lengths are fixed. In modern MD algorithms, this choice is computationally inefficient. Therefore, the bonds are allowed to stretch in MD, where the bond stretching force constants are taken from the OPLS force field. ${ }^{5}$ The p-LINCS algorithm was used to constrain the $\mathrm{O}-\mathrm{H}$ bond length, which allowed for the use of the larger time step. ${ }^{6}$ The parameters for bending and torsional potentials are taken from the TraPPE-UA force field. ${ }^{1-4}$

The structure factor $S(\mathbf{q})$ was calculated by:

$$
\begin{equation*}
S(\mathbf{q})=\frac{\left(\sum_{j}^{N_{\text {site }}} f_{j}(\mathbf{q}) \cos \left(\mathbf{q} \cdot \boldsymbol{r}_{\boldsymbol{j}}\right)\right)^{2}+\left(\sum_{j}^{N_{\text {site }}} f_{j}(\mathbf{q}) \sin \left(\mathbf{q} \cdot \boldsymbol{r}_{\boldsymbol{j}}\right)\right)^{2}}{\sum_{j}^{N_{\text {site }}} f_{j}^{2}(\mathbf{q})} \tag{S5}
\end{equation*}
$$

where $\mathbf{q}$ is the scattering wave vector, $\boldsymbol{r}_{\boldsymbol{j}}$ is the position vector of the interaction site $j, N_{\text {site }}$ is the number of interaction sites in the simulation box, and $f_{j}(\mathbf{q})$ is the atomic form factor as a function of the magnitude of $\mathbf{q}$. For $\mathrm{CH}_{q}$ pseudo-atoms, the atomic form factor for carbon is used, whereas the atomic form factors for oxygen and hydrogen are used for the hydroxy oxygen and hydrogen, respectively. All the functional forms of the atomic form factors are taken from the International Tables for Crystallography. ${ }^{7}$ The possible wave vectors included by the simulation box were computed using the following relationship:

$$
\begin{equation*}
\mathbf{q}=\frac{2 \pi}{L_{x}} n_{x} \boldsymbol{e}_{x}+\frac{2 \pi}{L_{y}} n_{y} \boldsymbol{e}_{\boldsymbol{y}}+\frac{2 \pi}{L_{z}} n_{z} \boldsymbol{e}_{z} \tag{S6}
\end{equation*}
$$

where $L_{x}, L_{y}$, and $L_{z}$ are the lengths of the simulation box in $x, y$, and $z$ direction, with $\boldsymbol{e}_{x}, \boldsymbol{e}_{y}$, and $\boldsymbol{e}_{z}$ being unit basis vectors in these directions (i.e. $\boldsymbol{e}_{x}=\left[\begin{array}{lll}1 & 0 & 0\end{array}\right]$ in the orthorhombic system). The reported $S(q)$ data were obtained by taking the average values of $S(\mathbf{q})$ with the same magnitude of the wave vector, $|\mathbf{q}|$. Uncertainties of $S(\mathbf{q})$ are reported as $95 \%$ confidence interval.

## Supplementary Tables

Table S1. Non-bonded Lennard-Jones parameters and partial charges ${ }^{1-4}$ for the interaction sites (pseudo-atoms) highlighted in bold.

| interaction site | $\sigma[\AA \AA]$ | $\varepsilon / k_{\mathrm{B}}[\mathrm{K}]$ | $q[\|\mathrm{e}\|]$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{C H}_{\mathbf{3}}$ | 3.75 | 98 | 0 |
| $\mathrm{CH}_{x}-\mathbf{C H}_{\mathbf{2}}-\mathrm{CH}_{x}$ | 3.95 | 46 | 0 |
| $\mathrm{CH}_{x}-\mathbf{C H}_{\mathbf{2}}-\mathrm{O}-\mathrm{H}$ | 3.95 | 46 | 0.265 |
| $\left(\mathrm{CH}_{x}\right)_{2}-\mathbf{C H}-\mathrm{O}-\mathrm{H}$ | 4.33 | 10 | 0.265 |
| $\mathbf{O}$ | 3.02 | 93 | -0.700 |
| $\mathbf{H}$ | N/A | N/A | 0.435 |

Table S2. Bonded interaction parameters. ${ }^{1-5}$

| stretching | $r_{0}[\AA]$ | $k_{\mathrm{s}} / k_{\mathrm{B}}[\mathrm{K}]$ |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CH}_{x}-\mathrm{CH}_{y}$ | 1.54 | 270000 |  |  |
| $\mathrm{CH}_{\sim}-\mathrm{O}$ | 1.43 | 322000 |  |  |
| O-H | 0.945 | constrained |  |  |
| bending | $\phi_{0}{ }^{\circ}{ }^{\circ}$ | $k_{\mathrm{b}} / k_{\mathrm{B}}[\mathrm{K}]$ |  |  |
| $\mathrm{CH}_{x}-\left(\mathrm{CH}_{2}\right)-\mathrm{CH}_{y}$ | 114 | 62500 |  |  |
| $\mathrm{CH}_{x}-(\mathrm{CH})-\mathrm{CH}_{y}$ | 112 | 62500 |  |  |
| $\mathrm{CH}_{x}-(\mathrm{O})$ - H | 108.5 | 55400 |  |  |
| $\mathrm{CH}_{x}-(\mathrm{CH})-\mathrm{O}$ | 109.5 | 50400 |  |  |
| torsion | $c_{0} / k_{\mathrm{B}}[\mathrm{K}]$ | $c_{1} / k_{\mathrm{B}}[\mathrm{K}]$ | $c_{2} / k_{\mathrm{B}}[\mathrm{K}]$ | $c_{3} / k_{\mathrm{B}}[\mathrm{K}]$ |
| *- $\mathrm{CH}_{2}-\mathrm{CH}_{2}$-* | 0.0 | 355.03 | -68.19 | 791.32 |
| *-CH ${ }_{x}$-CH-* | -251.06 | 428.73 | -111.85 | 441.27 |
| $\mathrm{CH}_{4}-\mathrm{CH}_{2}-\mathrm{O}-\mathrm{H}$ | 0.0 | 209.82 | -29.17 | 187.93 |
| $\mathrm{CH}_{x}$ - $\mathrm{CH}-\mathrm{O}-\mathrm{H}$ | 215.89 | 197.33 | 31.46 | -173.92 |

Table S3. Lengths of simulation trajectories ( $\mu \mathrm{s}$ ) and number of molecules in all systems.

| $\begin{aligned} & T_{\text {SIM }} \\ & {[\mathrm{K}]} \end{aligned}$ | ABA |  |  |  |  |  |  |  |  | BAB |  | AB |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{A}_{2} \mathrm{~B}_{2} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{4} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{5} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{6} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{7} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{8} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{10} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{2}$ | $\mathrm{A}_{3} \mathrm{~B}_{12} \mathrm{~A}_{3}$ | $\mathrm{B}_{6} \mathrm{~A}_{4} \mathrm{~B}_{6}$ | $\mathrm{B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6}$ | $\mathrm{A}_{2} \mathrm{~B}_{6}$ | $\mathrm{A}_{3} \mathrm{~B}_{6}$ | $\mathrm{A}_{4} \mathrm{~B}_{12}$ | $\mathrm{A}_{6} \mathrm{~B}_{12}$ |
| 340 | 2.2 | 2.0 | 9.6 | 2.3 | 3.0 | 2.0 |  |  |  |  |  | 1.0 |  |  |  |
|  | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 |  |  |  |  |  | 1000 |  |  |  |
| 370 | 1.8 | 1.6 | 10.0 | 3.2 | 3.0 | 2.0 | 2.0 | 3.2 |  |  |  | 1.0 | 1.2 |  |  |
|  | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 |  |  |  | 1000 | 1000 |  |  |
| 400 |  | 1.6 | 10.5 | 3.0 | 3.0 | 2.0 | 2.0 | 3.1 |  |  |  | 1.0 | 1.2 |  |  |
|  |  | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 |  |  |  | 1000 | 1000 |  |  |
| 430 |  |  |  | 3.0 | 3.0 | 2.0 | 2.0 | 3.1 | 2.0 | 4.5 |  | 1.0 | 1.2 |  |  |
|  |  |  |  | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1504 |  | 1000 | 1000 |  |  |
| 440 |  |  |  |  |  |  |  |  |  | $\begin{array}{\|c\|} \hline 4.3 \\ 1504 \end{array}$ |  |  |  |  |  |
| 460 |  |  |  | 2.0 | 1.4 | 1.2 | 2.0 | 1.9 | 2.3 | 4.7 |  |  | 1.2 | 1.8 |  |
|  |  |  |  | 1000 | 1000 | 1000 | 1000 | 2000 | 1000 | 1504 |  |  | 1000 | 1000 |  |
| 490 |  |  |  |  |  |  |  | 2.8 | 2.2 | 3.0 | 2.2 |  | 1.2 | 1.3 | 1.9 |
|  |  |  |  |  |  |  |  | 1000 | 2000 | 1504 | 1000 |  | 1000 | 1000 | 1000 |
| 520 |  |  |  |  |  |  |  | 3.2 | 2.6 | 2.2 | 2.2 |  |  | 1.2 | 2.2 |
|  |  |  |  |  |  |  |  | 1000 | 1000 | 1504 | 1000 |  |  | 1000 | 1000 |
| 550 |  |  |  |  |  |  |  |  | 2.5 |  | 2.2 |  |  | 1.3 | 1.3 |
|  |  |  |  |  |  |  |  |  | 1000 |  | 1000 |  |  | 1000 | 1000 |
| 580 |  |  |  |  |  |  |  |  |  |  | 2.2 |  |  | 1.5 | 2.1 |
|  |  |  |  |  |  |  |  |  |  |  | $1000$ |  |  | 1000 | 1000 |
| 610 |  |  |  |  |  |  |  |  |  |  | 2.2 |  |  |  | 1.7 |
|  |  |  |  |  |  |  |  |  |  |  | 1000 |  |  |  | 1000 |
| 640 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 1.2 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 1000 |
| 670 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 1.1 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 1000 |

Table S4. Lengths of simulation trajectories ( $\mu \mathrm{s}$ ) and number of molecules in $\mathrm{A}_{1} \mathrm{~B}_{y} \mathrm{~A}_{1}$ triblock, triblock/pentablock, and disperse triblock systems.

| $\begin{aligned} & \hline \hline T_{\mathrm{SIM}} \\ & {[\mathrm{~K}]} \end{aligned}$ | $\mathrm{A}_{1} \mathrm{~B}_{y} \mathrm{~A}_{1}$ | ABA/ABAABA | ABAdisperse | BABdisperse |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{A}_{1} \mathrm{~B}_{12} \mathrm{~A}_{1}$ | $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{2} / \mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{4} \mathrm{~B}_{12} \mathrm{~A}_{2}$ | $\mathrm{A}_{3} \mathrm{~B}_{10} \mathrm{~A}_{3} / \mathrm{A}_{3} \mathrm{~B}_{12} \mathrm{~A}_{3} / \mathrm{A}_{3} \mathrm{~B}_{14} \mathrm{~A}_{3}$ | $\mathrm{B}_{5} \mathrm{~A}_{6} \mathrm{~B}_{5} / \mathrm{B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6} / \mathrm{B}_{7} \mathrm{~A}_{6} \mathrm{~B}_{7}$ |  |
| 400 | $\begin{gathered} \hline 1.2 \\ 1000 \end{gathered}$ |  |  |  |  |
| 430 | $\begin{gathered} \hline 1.2 \\ 1000 \end{gathered}$ | $\begin{gathered} 2.0 \\ 980 / 20 \end{gathered}$ |  |  |  |
| 460 | $\begin{gathered} 1.2 \\ 1000 \end{gathered}$ |  |  |  |  |
| 490 |  |  | 1.6 1.6 1.6 <br>    <br> $100 / 800 / 100$ $250 / 500 / 250$ $500 / 0 / 500$ |  |  |
| 520 |  |  |  | $\begin{array}{cc\|} \hline 2.0 & 2.0 \\ 100 / 800 / 100 & 250 / 500 / 250 \end{array}$ | $\begin{gathered} 2.0 \\ 500 / 0 / 500 \end{gathered}$ |

Table S5. Average number of intermolecular H-bonds per hydroxyl group for all oligomers. Data for ordered morphologies are highlighted in bold font.

| $T_{\text {SIM }}$ | ABA |  |  |  |  |  |  |  |  | BAB |  | AB |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| [K] | $\mathrm{A}_{2} \mathrm{~B}_{2} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{4} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{5} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{6} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{7} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{8} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{10} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{2}$ | $\mathrm{A}_{3} \mathrm{~B}_{12} \mathrm{~A}_{3}$ | $\mathrm{B}_{6} \mathrm{~A}_{4} \mathrm{~B}_{6}$ | $\mathrm{B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6}$ | $\mathrm{A}_{2} \mathrm{~B}_{6}$ | $\mathrm{A}_{3} \mathrm{~B}_{6}$ | $\mathrm{A}_{4} \mathrm{~B}_{12}$ | $\mathrm{A}_{6} \mathrm{~B}_{12}$ |
| 340 | 1.06 | 1.06 | 1.06 | 1.05 | 1.06 |  |  |  |  |  |  | 1.11 |  |  |  |
| 370 | 1.02 | 1.00 | 1.00 | 1.03 | 1.05 | 1.03 | 1.02 | 1.09 |  |  |  | 1.02 | 0.90 |  |  |
| 400 |  | 0.96 | 0.94 | 1.00 | 1.00 | 1.00 | 0.99 | 1.09 |  |  |  | 0.92 | 0.88 |  |  |
| 430 |  |  |  | 0.94 | 0.93 | 0.94 | 0.94 | 1.00 | 0.81 | 0.83 |  | 0.79 | 0.88 |  |  |
| 440 |  |  |  |  |  |  |  |  |  | 0.83 |  |  |  |  |  |
| 460 |  |  |  | 0.82 | 0.79 | 0.79 | 0.81 | 0.92 | 0.81 | 0.79 |  |  | 0.75 | 0.71 |  |
| 490 |  |  |  |  |  |  |  | 0.74 | 0.76 | 0.71 | 0.80 |  | 0.68 | 0.77 | 0.81 |
| 520 |  |  |  |  |  |  |  | 0.65 | 0.70 | 0.64 | 0.74 |  |  | 0.71 | 0.75 |
| 550 |  |  |  |  |  |  |  |  | 0.58 |  | 0.68 |  |  | 0.64 | 0.70 |
| 580 |  |  |  |  |  |  |  |  |  |  | 0.61 |  |  | 0.55 | 0.66 |
| 610 |  |  |  |  |  |  |  |  |  |  | 0.52 |  |  |  | 0.61 |
| 640 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 0.59 |
| 670 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 0.52 |

Table S6. Molar volumes [ $\left.\mathrm{cm}^{3} / \mathrm{mol}\right]$ of triblock and diblock amphiphiles at various simulation temperatures Data for ordered morphologies are highlighted in bold font.

| $T_{\text {SIM }}$ | ABA |  |  |  |  |  |  |  |  | BAB |  | AB |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| [K] | $\mathrm{A}_{2} \mathrm{~B}_{2} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{4} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{5} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{6} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{7} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{8} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{10} \mathrm{~A}_{2}$ | $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{2}$ | $\mathrm{A}_{3} \mathrm{~B}_{12} \mathrm{~A}_{3}$ | $\mathrm{B}_{6} \mathrm{~A}_{4} \mathrm{~B}_{6}$ | $\mathrm{B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6}$ | $\mathrm{A}_{2} \mathrm{~B}_{6}$ | $\mathrm{A}_{3} \mathrm{~B}_{6}$ | $\mathrm{A}_{4} \mathrm{~B}_{12}$ | $\mathrm{A}_{6} \mathrm{~B}_{12}$ |
| 340 | 119.74 | 153.38 | 170.67 | 187.86 | 203.44 |  |  |  |  |  |  | 163.53 |  |  |  |
| 370 | $121.0_{7}$ | $155.9_{7}$ | $173_{1}$ | 1881 | 203.26 | 221.25 | 2561 | 286.97 |  |  |  | 167.92 | $182.1_{7}$ |  |  |
| 400 |  | 158.47 | 176.86 | 188.66 | 206.03 | $221.6_{8}$ | 256.0 ${ }_{3}$ | 2871 |  |  |  | $171.2_{1}$ | 185.04 |  |  |
| 430 |  |  |  | $191.9_{7}$ | 209.94 | 226.06 | 259.87 | 286.73 | $339_{1}$ | $319_{1}$ |  | $176.0_{1}$ | 189.14 |  |  |
| 440 |  |  |  |  |  |  |  |  |  | 318.7 ${ }_{7}$ |  |  |  |  |  |
| 460 |  |  |  | 2021 | 222.13 | 240.73 | 275.75 | 294.04 | 344.24 | 3251 |  |  | 196.82 | 3351 |  |
| 490 |  |  |  |  |  |  |  | 316.75 | 350.0 ${ }_{3}$ | 337.26 | 337.49 |  | 202.92 | 335.34 | 3581 |
| 520 |  |  |  |  |  |  |  | 325.52 | 356.49 | 347.75 | 3481 |  |  | 3361 | $371{ }_{1}$ |
| 550 |  |  |  |  |  |  |  |  | $373.1_{3}$ |  | 3651 |  |  | 3481 | $3788_{1}$ |
| 580 |  |  |  |  |  |  |  |  |  |  | 381 ${ }_{1}$ |  |  | 364.27 | 386.78 |
| 610 |  |  |  |  |  |  |  |  |  |  | $401{ }_{1}$ |  |  |  | 395.38 |
| 640 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | $404.3{ }^{2}$ |
| 670 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 426.15 |

Table S7. Fraction and type of intermolecular hydrogen bonds between each pair of hydroxy oxygens for $\mathrm{A}_{2} \mathrm{~B}_{6} \mathrm{~A}_{2}$ at $T_{\text {SIM }}=430 \mathrm{~K}$.

|  | $\mathrm{O}_{i}$ | $\mathrm{O}_{j}$ | fraction | H-bond type |
| :---: | :---: | :---: | :---: | :---: |
|  | 2 | 2 | 0.066 | pri-pri |
|  | 2 | 5 | 0.065 | pri-sec |
|  | 2 | 14 | 0.068 | pri-sec |
|  | 2 | 17 | 0.069 | pri-pri |
|  | 5 | 2 | 0.066 | pri-sec |
|  | 5 | 5 | 0.048 | sec-sec |
|  | 5 | 14 | 0.050 | sec-sec |
|  | 5 | 17 | 0.069 | pri-sec |
|  | 14 | 2 | 0.069 | pri-sec |
|  | 14 | 5 | 0.049 | sec-sec |
|  | 14 | 14 | 0.048 | sec-sec |
|  | 14 | 17 | 0.066 | pri-sec |
|  | 17 | 2 | 0.068 | pri-pri |
|  | 17 | 5 | 0.067 | pri-sec |
|  | 17 | 14 | 0.065 | pri-sec |
|  | 17 | 17 | 0.066 | pri-pri |

Table S8. Fraction and type of intermolecular hydrogen bonds between each pair of hydroxy oxygens for $\mathrm{A}_{2} \mathrm{~B}_{8} \mathrm{~A}_{2}$ at $T_{\text {SIM }}=430 \mathrm{~K}$.

|  | $\mathrm{O}_{i}$ | $\mathrm{O}_{j}$ | fraction | H-bond type |
| :---: | :---: | :---: | :---: | :---: |
|  | 2 | 2 | 0.067 | pri-pri |
|  | 2 | 5 | 0.066 | pri-sec |
|  | 2 | 16 | 0.066 | pri-sec |
|  | 2 | 19 | 0.067 | pri-pri |
|  | 5 | 2 | 0.067 | pri-sec |
|  | 5 | 5 | 0.049 | sec-sec |
|  | 5 | 16 | 0.048 | sec-sec |
|  | 5 | 19 | 0.066 | pri-sec |
|  | 16 | 2 | 0.067 | pri-sec |
|  | 16 | 5 | 0.049 | sec-sec |
|  | 16 | 16 | 0.050 | sec-sec |
|  | 16 | 19 | 0.067 | pri-sec |
|  | 19 | 2 | 0.068 | pri-pri |
|  | 19 | 5 | 0.068 | pri-sec |
|  | 19 | 16 | 0.067 | pri-sec |
|  | 19 | 19 | 0.067 | pri-pri |

Table S9. Fraction and type of intermolecular hydrogen bonds between each pair of hydroxy oxygens for $\mathrm{A}_{2} \mathrm{~B}_{10} \mathrm{~A}_{2}$ at $T_{\text {SIM }}=430 \mathrm{~K}$.

|  | $\mathrm{O}_{i}$ | $\mathrm{O}_{j}$ | fraction | H-bond type |
| :---: | :---: | :---: | :---: | :---: |
|  | 2 | 2 | 0.067 | pri-pri |
|  | 2 | 5 | 0.066 | pri-sec |
|  | 2 | 18 | 0.066 | pri-sec |
| 56 | 2 | 21 | 0.067 | pri-pri |
|  | 5 | 2 | 0.066 | pri-sec |
| $\begin{array}{lllllllll} \\ 4^{4} & 9 & 11 & 13 & 15 & \mathrm{OH}_{2122}\end{array}$ | 5 | 5 | 0.050 | sec-sec |
| ${ }_{1819}$ | 5 | 18 | 0.049 | sec-sec |
|  | 5 | 21 | 0.066 | pri-sec |
|  | 18 | 2 | 0.068 | pri-sec |
|  | 18 | 5 | 0.050 | sec-sec |
|  | 18 | 18 | 0.050 | sec-sec |
|  | 18 | 21 | 0.067 | pri-sec |
|  | 21 | 2 | 0.068 | pri-pri |
|  | 21 | 5 | 0.067 | pri-sec |
|  | 21 | 18 | 0.066 | pri-sec |
|  | 21 | 21 | 0.066 | pri-pri |

Table S10. Fraction and type of intermolecular hydrogen bonds between each pair of hydroxy oxygens for $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{2}$ at $T_{\text {SIM }}=430 \mathrm{~K}$.

|  | $\mathrm{O}_{i}$ | $\mathrm{O}_{j}$ | fraction | H-bond type |
| :---: | :---: | :---: | :---: | :---: |
|  | 2 | 2 | 0.072 | pri-pri |
|  | 2 | 5 | 0.062 | pri-sec |
|  | 2 | 20 | 0.060 | pri-sec |
|  | 2 | 23 | 0.077 | pri-pri |
|  | 5 | 2 | 0.061 | pri-sec |
|  | 5 | 5 | 0.053 | sec-sec |
|  | 5 | 20 | 0.050 | sec-sec |
|  | 5 | 23 | 0.064 | pri-sec |
|  | 20 | 2 | 0.060 | pri-sec |
|  | 20 | 5 | 0.050 | sec-sec |
|  | 20 | 20 | 0.043 | sec-sec |
|  | 20 | 23 | 0.065 | pri-sec |
|  | 23 | 2 | 0.078 | pri-pri |
|  | 23 | 5 | 0.065 | pri-sec |
|  | 23 | 20 | 0.065 | pri-sec |
|  | 23 | 23 | 0.075 | pri-pri |

## Supplementary Figures



Figure S1. Radial-angular distribution functions (RADFs) for hydroxy groups of $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{2}$, $\mathrm{A}_{3} \mathrm{~B}_{12} \mathrm{~A}_{3}, \mathrm{~B}_{6} \mathrm{~A}_{4} \mathrm{~B}_{6}$, and $\mathrm{B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6}$ amphiphiles at their lowest $T_{\text {SIM }}$ above $T_{\text {SIM,ODT. }}$. The radial and angular distributions are shown as 2-D projections of the RADF surfaces on vertical panes. The resulting RADF is normalized by a random distribution, with the Jacobian matrix corrected in the angular direction.


Figure S2. Radial-angular distribution functions (RADFs) for hydroxy groups of $\mathrm{A}_{2} \mathrm{~B}_{x} \mathrm{~A}_{2}$ bolaamphiphiles at their lowest $T_{\text {SIM }}$ above $T_{\text {SIM,ODT. }}$. The radial and angular distributions are shown as 2-D projections of the RADF surfaces on vertical panes. The resulting RADF is normalized by a random distribution, with the Jacobian matrix corrected in the angular direction.


Figure S3. Histograms of the sum of intermolecular $\mathrm{CH}_{q}-\mathrm{CH}_{q}$ Lennard-Jones interaction energies between the nonpolar parts (B blocks) for a pair of molecules in the DIS state obtained for ABA and BAB triblock and AB diblock amphiphiles. For example, the sum consists of 144 site-site energies for a pair of $\mathrm{B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6}$ molecules containing each $12 \mathrm{CH}_{q}$ units and accounts for the difference in the well depths of $\mathrm{CH}_{3}$ and $\mathrm{CH}_{2}$ units. The peak at $U_{\text {pair }} / k_{\mathrm{B}} \approx 0 \mathrm{~K}$ corresponds to spatially well separated molecules. The small fraction of molecules with $U_{\text {pair }} / k_{\mathrm{B}}>0 \mathrm{~K}$ corresponds to molecules in close contact. The slope in these histograms is relatively small at $U_{\text {pair }} / k_{\mathrm{B}}=-T$.


Figure S4. Mean square displacements (MSDs) in log-log and linear-linear scales for $\mathrm{A}_{3} \mathrm{~B}_{12} \mathrm{~A}_{3}$ and $\mathrm{A}_{2} \mathrm{~B}_{6} \mathrm{~A}_{2}$ molecules at temperatures yielding GL, LAM, and DIS morphologies. These two compounds are at the low- and high-end of the molecular weight range for ABA triblock amphiphiles investigated here. Data are shown for the final 400 ns of the trajectories because molecules are sometimes more mobile during the initial phase of trajectory that is started from a highly-disordered structure. In the log-log plot, the dash-dotted black lines show a slope of unity. Over a 100 ns interval, the MSDs for the GL and DIS phases are significantly smaller and larger, respectively, than $d^{2}$ observed for the LAM phase (where $d$ is the domain spacing).


Figure S5. Probability distributions of the end-to-end lengths of the alkyl tails for $A_{4} B_{12}$ and $A_{6} B_{12}$ diblock amphiphiles at $T_{\text {SIM }}=520 \mathrm{~K}$. The average lengths are 11.2 and $11.1 \AA$ for $\mathrm{A}_{4} \mathrm{~B}_{12}$ and $\mathrm{A}_{6} \mathrm{~B}_{12}$, respectively.


Figure S6. Composition profiles along the normal of the lamellar planes for $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{2}$ at $T_{\text {SIM }}=460 \mathrm{~K}, \mathrm{~A}_{3} \mathrm{~B}_{12} \mathrm{~A}_{3}$ at $460 \mathrm{~K}, \mathrm{~B}_{6} \mathrm{~A}_{4} \mathrm{~B}_{6}$ at $440 \mathrm{~K}, \mathrm{~B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6}$ at 520 K , and $\mathrm{A}_{3} \mathrm{~B}_{6}$ at 430 K . Polar and nonpolar mass fractions are shown red and blue, respectively.


Figure S7. Angular distributions of the end-to-end vectors of neighboring B blocks for (top) the LAM phases of ABA amphiphiles, (middle) the PL and HPL phases of BAB amphiphiles, and (bottom) the LAM phases of AB amphiphiles. The schematics are drawn to guide the eye. Two B blocks are considered as neighbors when their center-of-mass distance is less than or equal to $8 \AA$, consistent with the neighbor definition in Chen et al..$^{8}$ The angle between two neighboring ABA amphiphile can only range from 0 to $90^{\circ}$.


Figure S8. Voronoi tessellation of one perforated layer for the $\mathrm{B}_{6} \mathrm{~A}_{4} \mathrm{~B}_{6}$ amphiphile at $T_{\text {SIM }}=$ 440 K at different times during the trajectory. The parallelogram-shaped frame contains two repeat units (indicated by the dashed lines). The blue, red, and green dots indicate pentagons, hexagons, and heptagons, respectively.


Figure S9. Perpendicular views from the reference layer (Layer 1) in the $\mathrm{B}_{6} \mathrm{~A}_{4} \mathrm{~B}_{6}$ system at $T_{\text {SIM }}=$ 440 K . To access more details of the perforations, the box is replicated three times in each dimension using periodic images.


Figure S10. Structure factors and simulation snapshots for $A_{3} B_{12} A_{3}$ amphiphiles and $\mathrm{A}_{3} \mathrm{~B}_{10} \mathrm{~A}_{3} / \mathrm{A}_{3} \mathrm{~B}_{12} \mathrm{~A}_{3} / \mathrm{A}_{3} \mathrm{~B}_{14} \mathrm{~A}_{3}$ mixtures at $T_{\text {SIM }}=490 \mathrm{~K}$; "loops" are highlighted in green and "bridges" are shown with transparent alkyl chains.


Figure S11. Structure factors and simulation snapshots for $\mathrm{B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6}$ amphiphiles and $\mathrm{B}_{5} \mathrm{~A}_{6} \mathrm{~B}_{5} / \mathrm{B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6} / \mathrm{B}_{7} \mathrm{~A}_{6} \mathrm{~B}_{7}$ mixtures at $T_{\mathrm{SIM}}=520 \mathrm{~K}$. For neat $\mathrm{B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6}$ and the $1: 2: 1$ mixture, alkyl chains connected by polar "bridges" are highlighted in yellow and those connected by polar "loops" are shown as transparent.


Figure S12. Left: structure factors for $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{2}$ amphiphiles $(N=1000)$ and the mixture of $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{2}$ triblock $(N=980)$ and $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{4} \mathrm{~B}_{12} \mathrm{~A}_{2}$ pentablock $(N=20)$ at $T_{\mathrm{SIM}}=430 \mathrm{~K}$. Right: simulation snapshot of the $\mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{2} / \mathrm{A}_{2} \mathrm{~B}_{12} \mathrm{~A}_{4} \mathrm{~B}_{12} \mathrm{~A}_{2}$ mixture, with all of the pentablocks highlighted. Conformations include "bridge-bridge" in the same domain (green), "bridge-bridge" spanning two domains (yellow), and "bridge-loop" (magenta).


Figure S13. Molar volumes of ordered phases obtained for $A B A, B A B$, and $A B$ amphiphiles versus molar volumes predicted by multiple-linear regression using the equation:

$$
V_{\mathrm{MLR}}=\left(n_{\mathrm{CH}_{2} \mathrm{OH}} V_{\mathrm{CH}_{2} \mathrm{OH}}+n_{\mathrm{CHOH}} V_{\mathrm{CHOH}}+n_{\mathrm{CH}_{3}} V_{\mathrm{CH}_{3}}+n_{\mathrm{CH}_{2}} V_{\mathrm{CH}_{2}}\right)\left(1+\alpha\left(T_{\mathrm{SIM}}-370\right)\right)
$$

The fitting coefficients are: $V_{\mathrm{CH}_{2} \mathrm{OH}}=24.4 \mathrm{~cm}^{3} / \mathrm{mol}, ~ V_{\mathrm{CHOH}}=23.9 \mathrm{~cm}^{3} / \mathrm{mol}, V_{\mathrm{CH}_{3}}=$ $20.1 \mathrm{~cm}^{3} / \mathrm{mol}, V_{\mathrm{CH}_{2}}=15.6 \mathrm{~cm}^{3} / \mathrm{mol}$, and $\alpha=0.00066 \mathrm{~K}^{-1}$.


Figure S14. Cumulative distribution functions for the probability of finding $\mathrm{A}_{3} \mathrm{~B}_{12} \mathrm{~A}_{3}, \mathrm{~B}_{6} \mathrm{~A}_{4} \mathrm{~B}_{6}$, and $\mathrm{B}_{6} \mathrm{~A}_{6} \mathrm{~B}_{6}$ triblock amphiphiles and $\mathrm{A}_{x} \mathrm{~B}_{y}$ diblock amphiphiles in a hydrogen-bonded (top) and nonpolar (bottom) aggregate of size of $N$ for the disordered phases near $T_{\text {оdt }}$. For $\mathrm{B}_{6} \mathrm{~A}_{4} \mathrm{~B}_{6}, N$ is scaled by $1000 / 1504$ to account for the different number of molecules.

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