

Supporting Information for:
Trends in the Stability and Dissociation Kinetics of
Lanthanide(III) Complexes with Cyclen-Based Ligands
Across the Lanthanide Series

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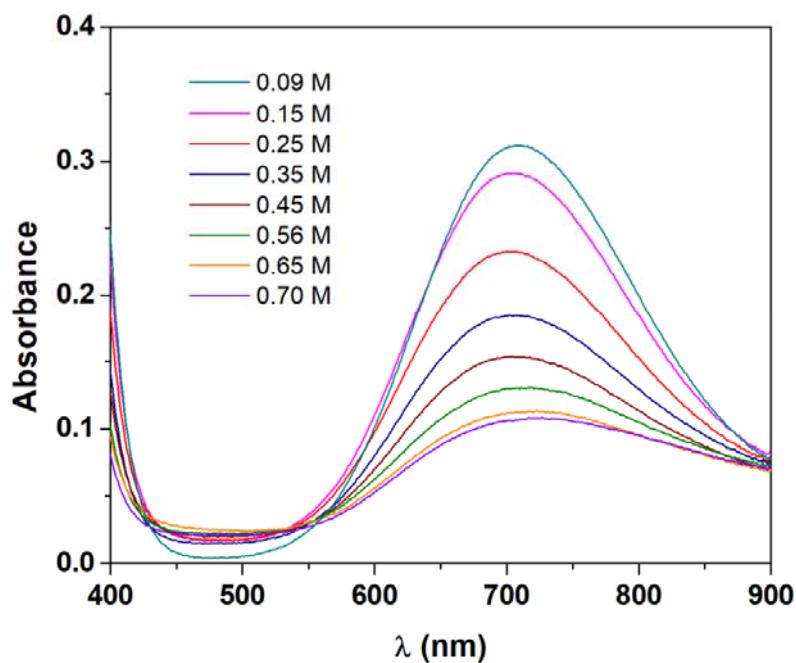


Figure S1. VIS spectra of the solutions containing nearly equimolar amounts of Cu^{2+} and 1,7-DO2APA³⁻ ($c_{\text{Cu}^{2+}}=2.50 \text{ mM}$, $c_{\text{Lig}}=2.51 \text{ mM}$) as a function of acid concentration (93.2, 149.1, 251.7, 354.2, 447.4, 559.3, 652.5 and 699.1 mM in 1.0 M NaCl).

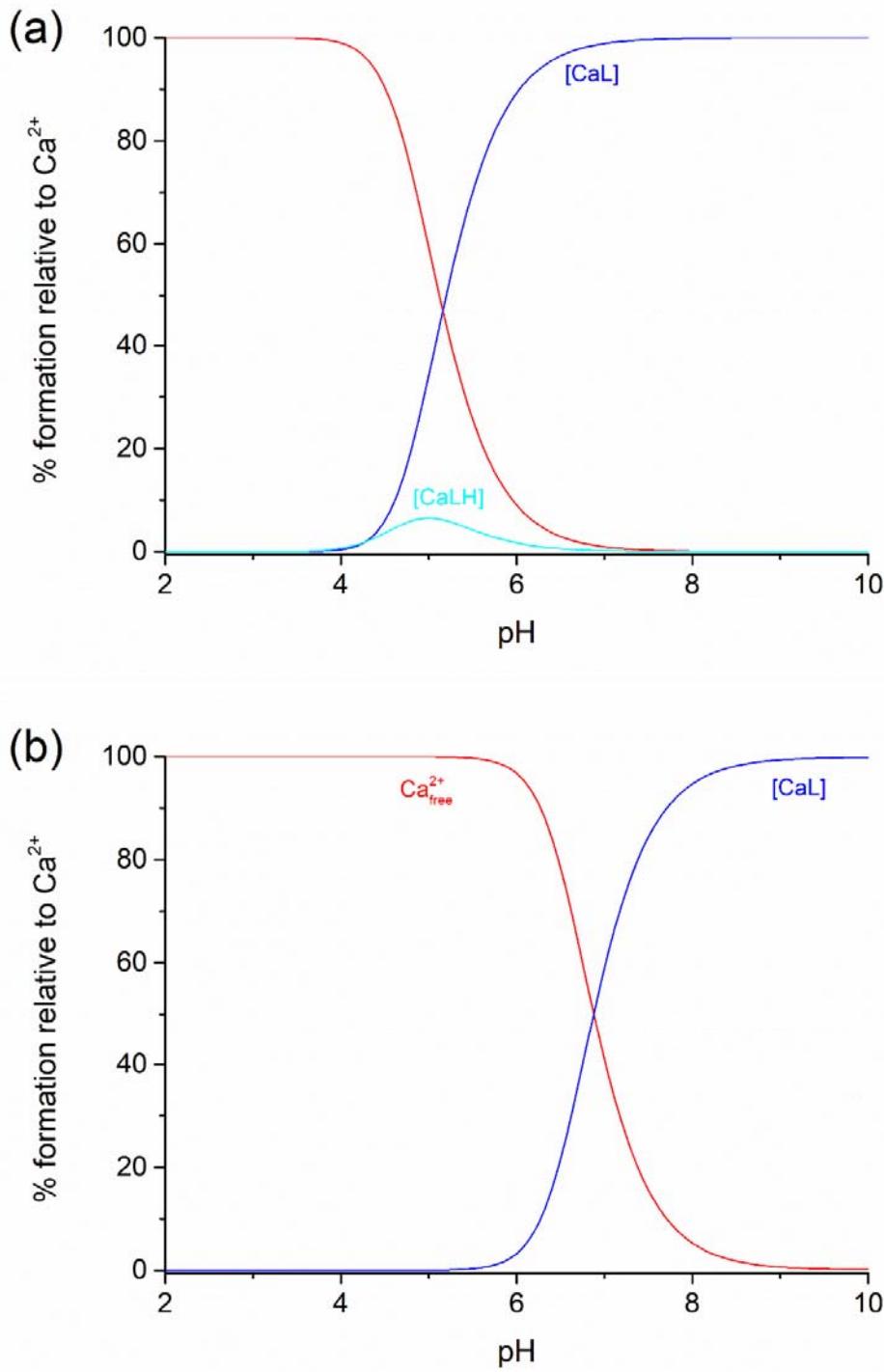


Figure S2. Speciation diagrams calculated for the $\text{Ca}^{2+}:1,4\text{-DO2APA}^{3-}$ (a) and $\text{Ca}^{2+}:1,7\text{-DO2APA}^{3-}$ (b) systems ($c_{\text{Ca}^{2+}}=c_{\text{Lig}}=1.0 \text{ mM}$, 25°C , 0.15 M NaCl , 25°C , 0.15 M NaCl).

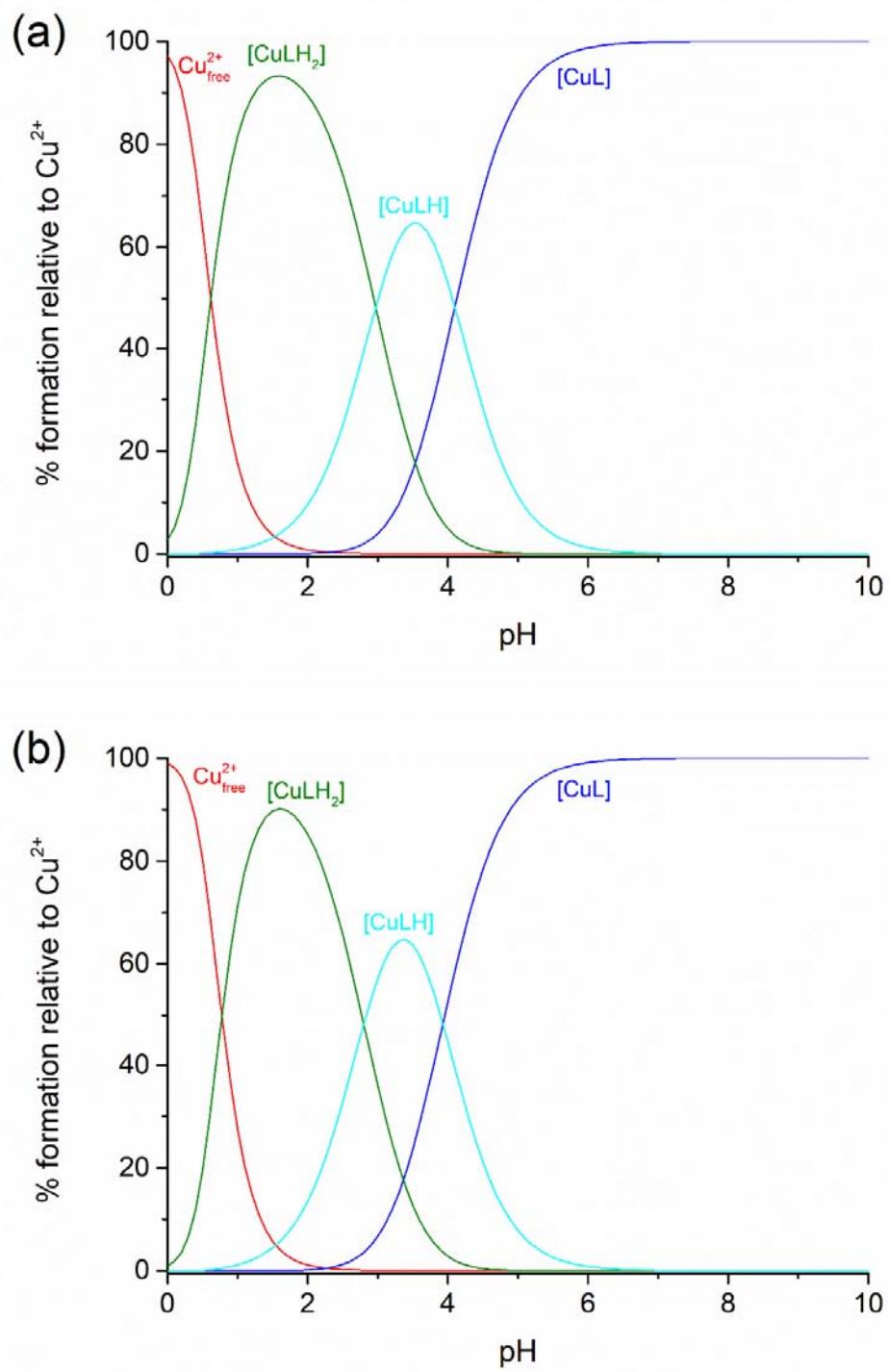


Figure S3. Speciation diagrams calculated for the $\text{Cu}^{2+}:1,4\text{-DO}_2\text{APA}^{3-}$ (a) and $\text{Cu}^{2+}:1,7\text{-DO}_2\text{APA}^{3-}$ (b) systems ($c_{\text{Cu}^{2+}}=c_{\text{Lig}}=1.0 \text{ mM}$, 25°C , 0.15 M NaCl).

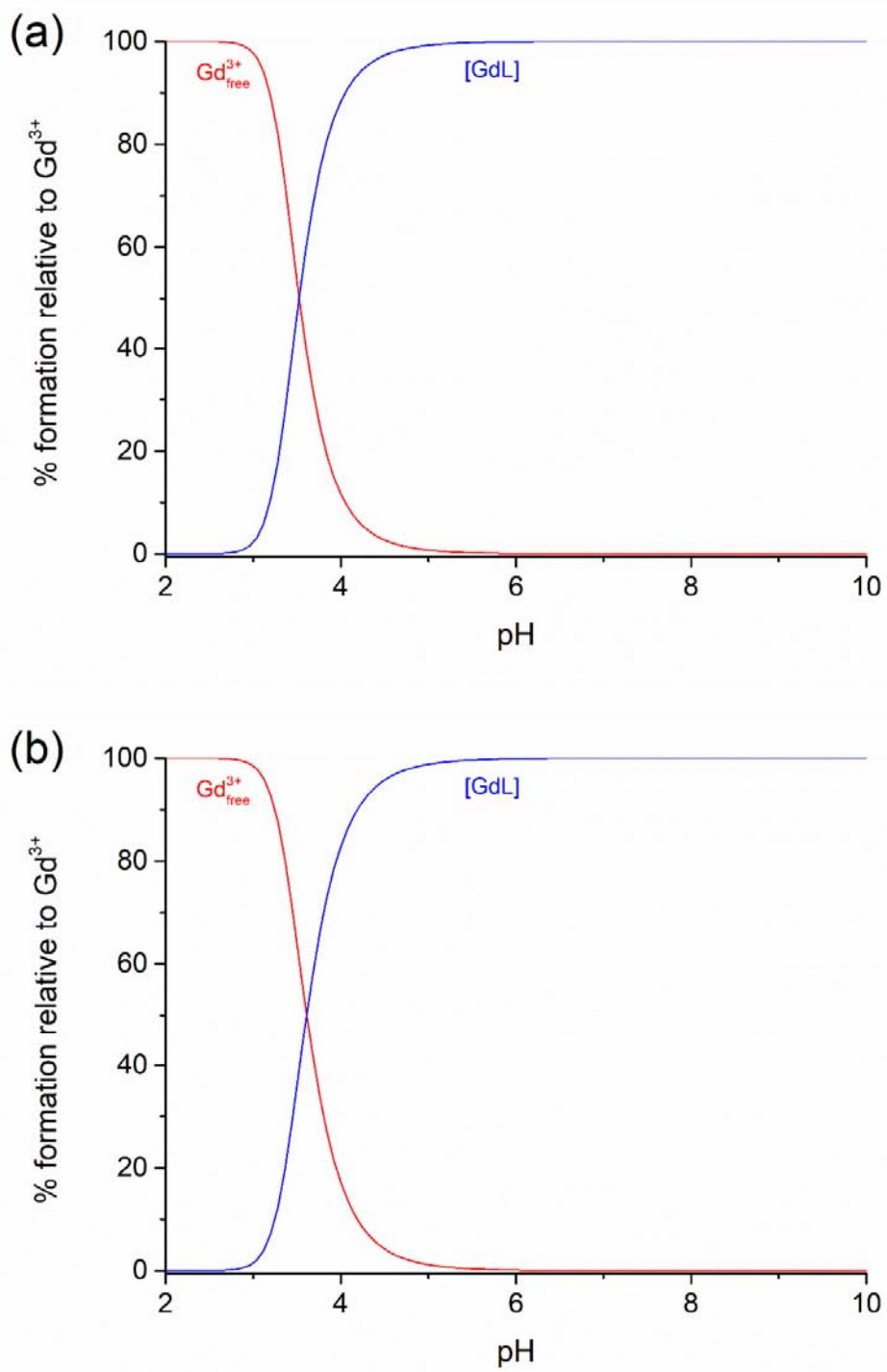


Figure S4. Speciation diagrams calculated for the $\text{Gd}^{3+}:1,4\text{-DO2APA}^{3-}$ (a) and $\text{Gd}^{3+}:1,7\text{-DO2APA}^{3-}$ (b) systems ($c_{\text{Gd}^{3+}}=c_{\text{Lig}}=1.0 \text{ mM}$, 25°C , 0.15 M NaCl).

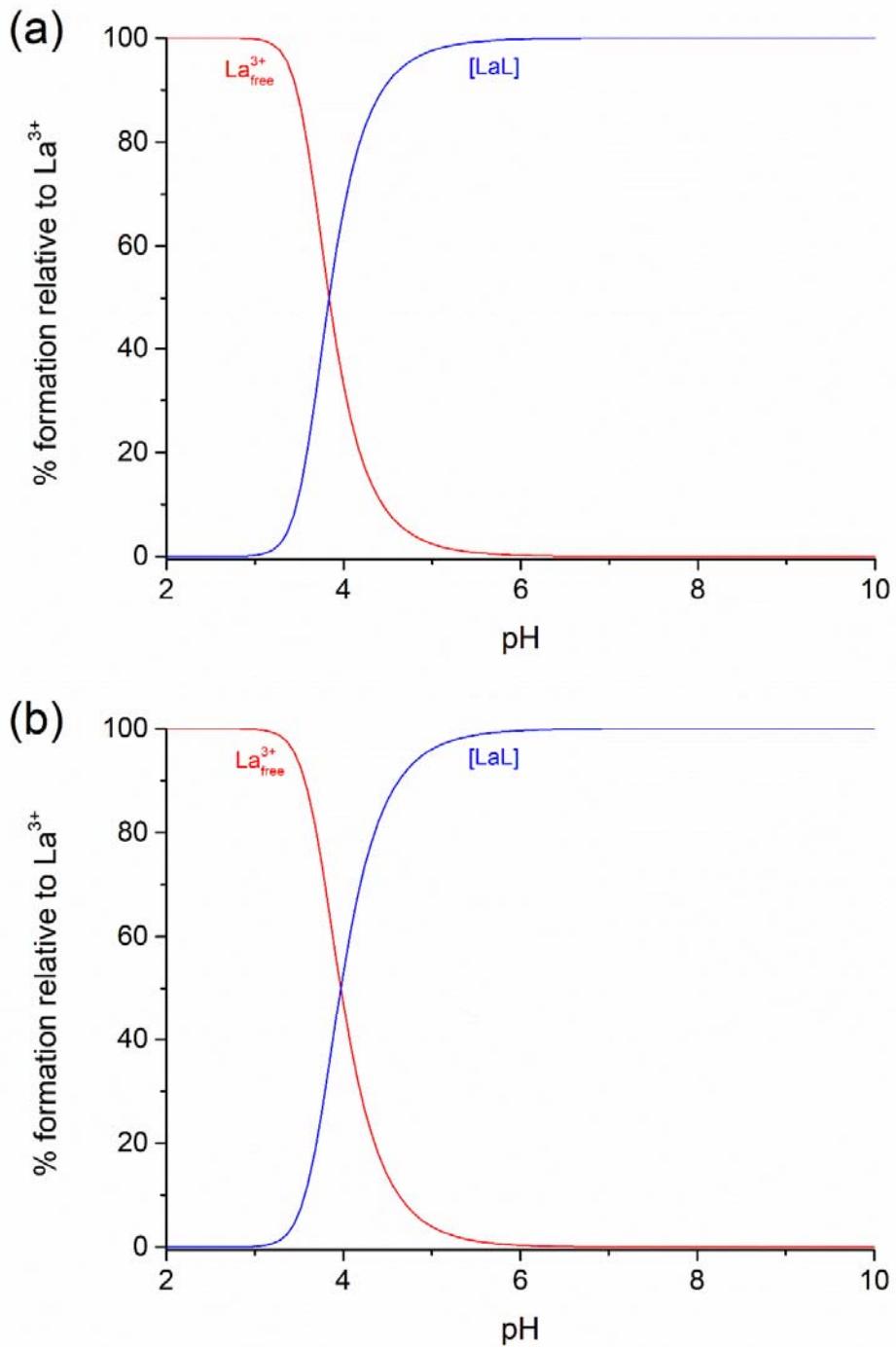


Figure S5. Speciation diagrams calculated for the $\text{La}^{3+}:1,4\text{-DO2APA}^{3-}$ (a) and $\text{La}^{3+}:1,7\text{-DO2APA}^{3-}$ (b) systems ($c_{\text{La}^{3+}}=c_{\text{Lig}}=1.0 \text{ mM}$, 25°C , 0.15 M NaCl).

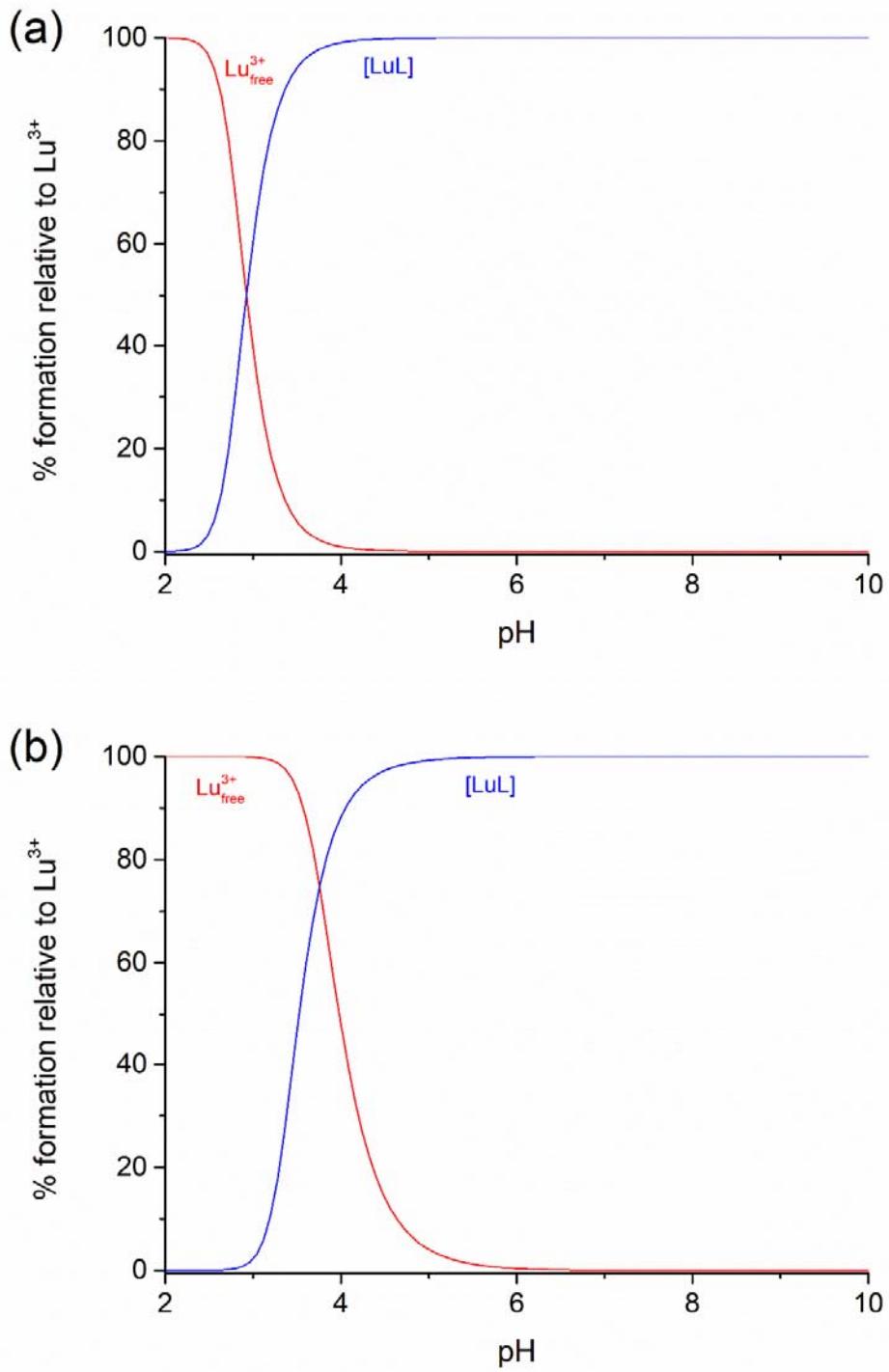


Figure S6. Speciation diagrams calculated for the Lu³⁺:1,4-DO2APA³⁻ (a) and Lu³⁺:1,7-DO2APA³⁻ (b) systems ($c_{\text{Lu}^{3+}} = c_{\text{Lig}} = 1.0 \text{ mM}$, 25 °C, 0.15 M NaCl).

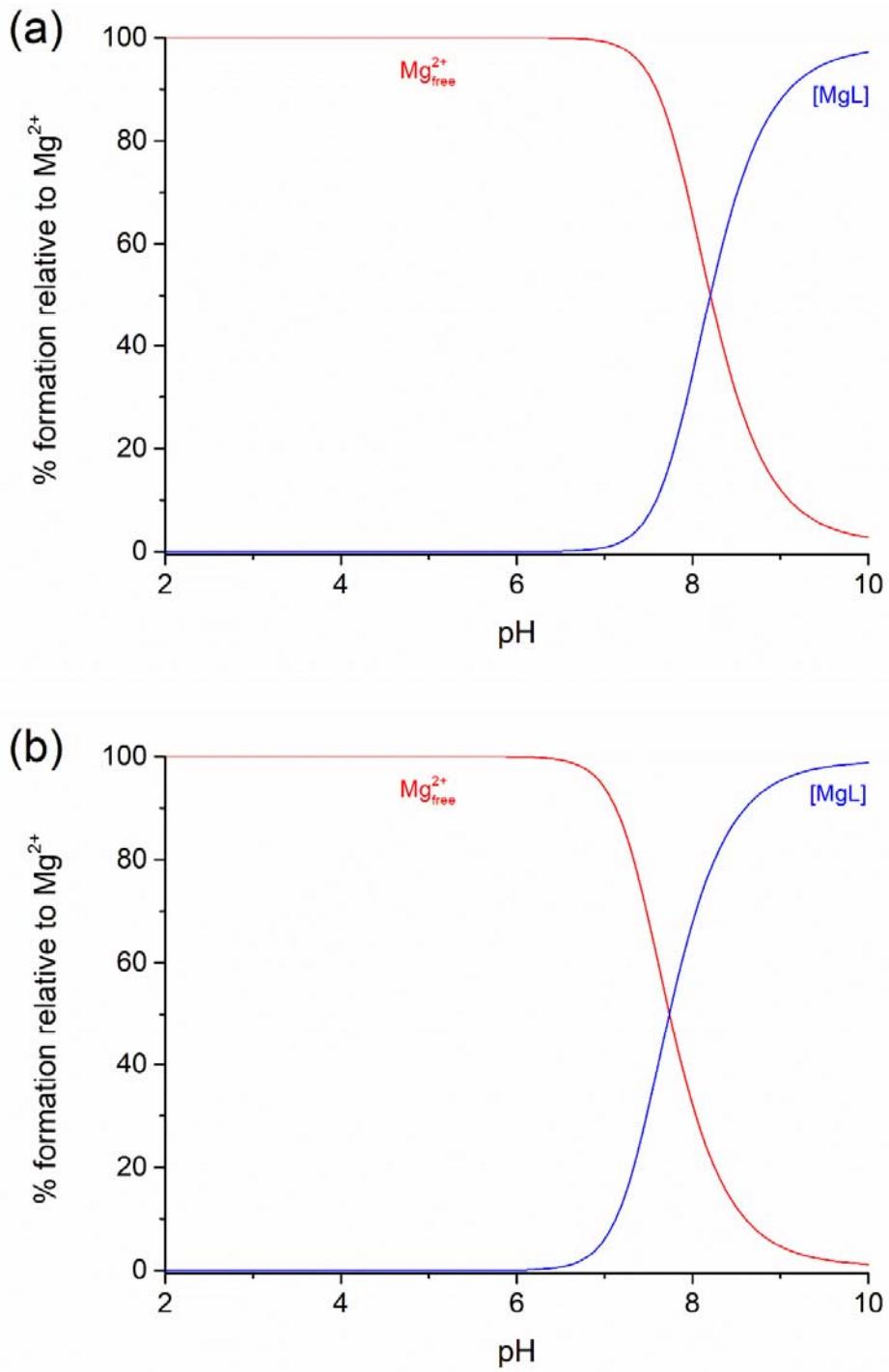


Figure S7. Speciation diagrams calculated for the $Mg^{2+}:1,4\text{-DO2APA}^{3-}$ (a) and $Mg^{2+}:1,7\text{-DO2APA}^{3-}$ (b) systems ($c_{Mg^{2+}}=c_{Lig}=1.0\text{ mM}$, $25\text{ }^{\circ}\text{C}$, 0.15 M NaCl).

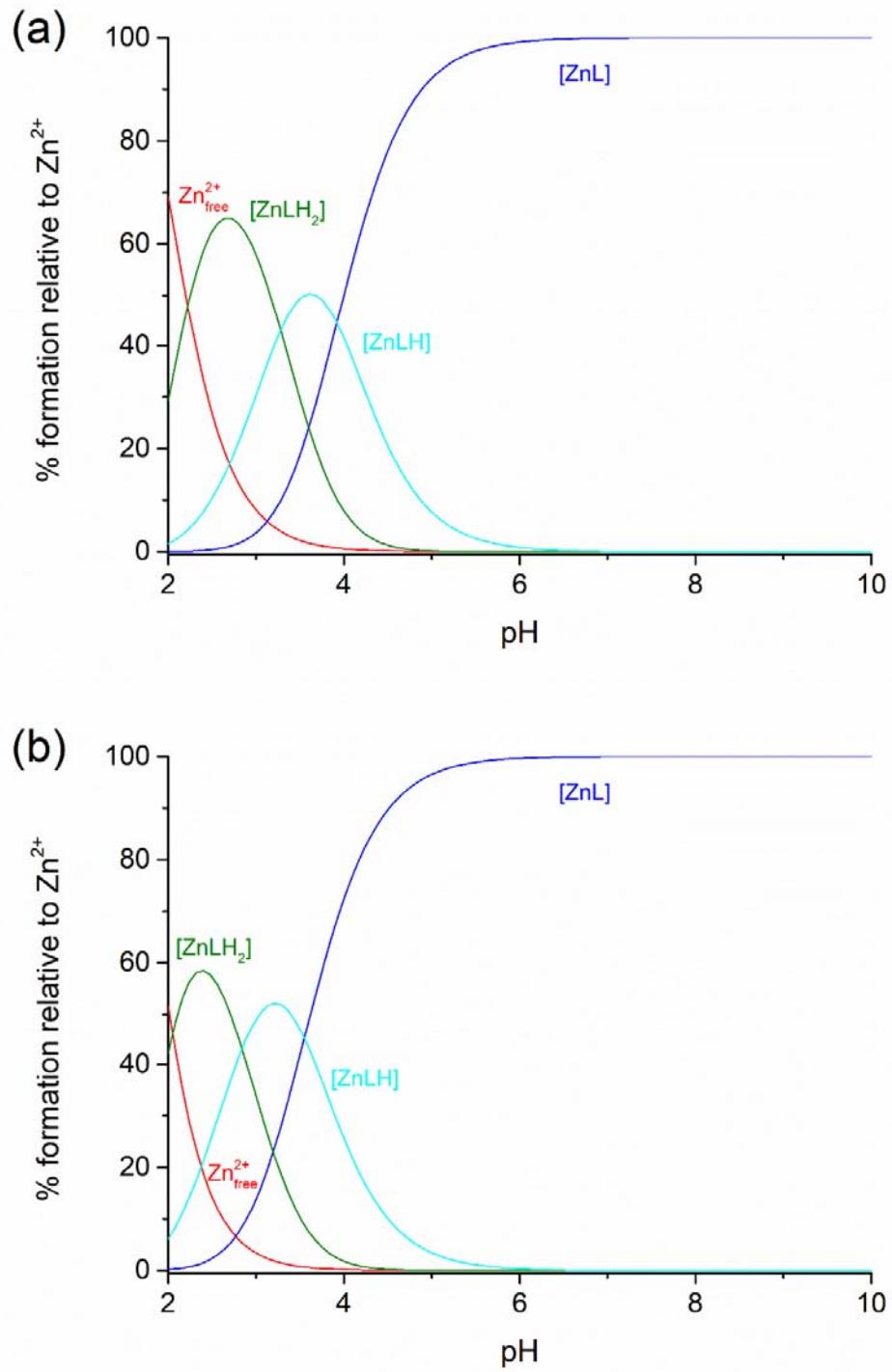


Figure S8. Speciation diagrams calculated for the $\text{Zn}^{2+}:1,4\text{-DO2APA}^{3-}$ (a) and $\text{Zn}^{2+}:1,7\text{-DO2APA}^{3-}$ (b) systems ($c_{\text{Zn}^{2+}}=c_{\text{Lig}}=1.0 \text{ mM}$, 25°C , 0.15 M NaCl).

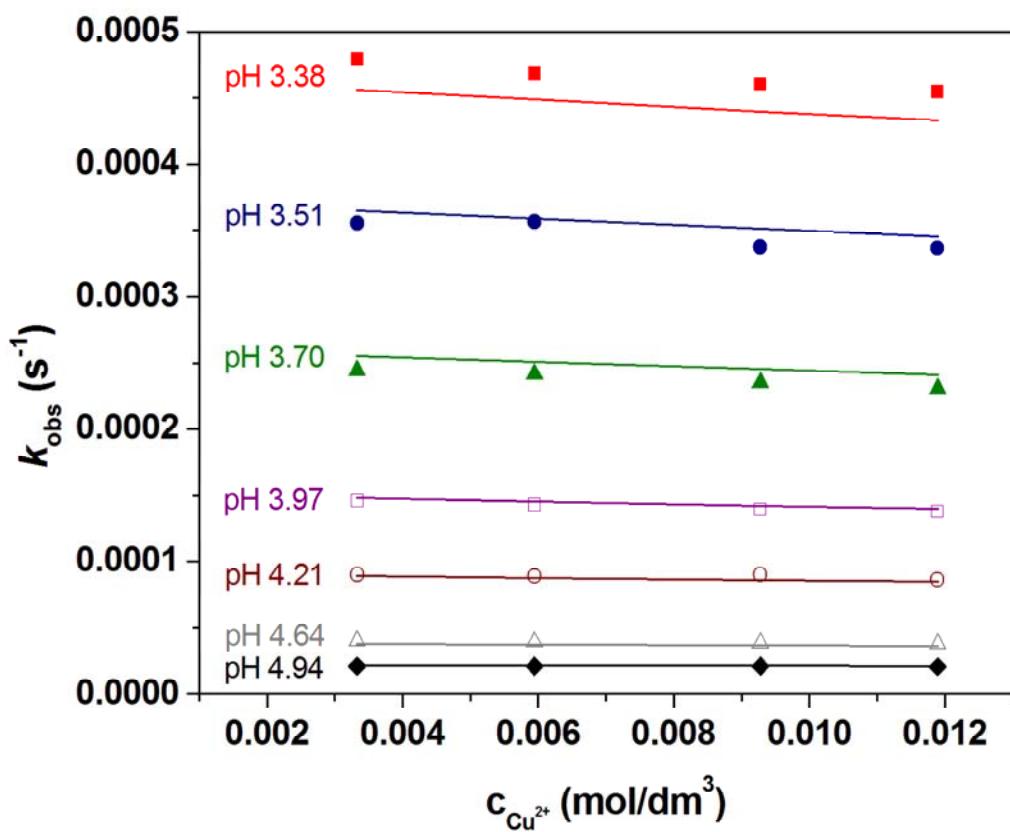


Figure S9. Pseudo-first-order rate constants of dissociation of the [Gd(1,4-DO2APA)] complex (2.9×10^{-4} M) as a function of Cu^{2+} ion concentration obtained at different pH values.

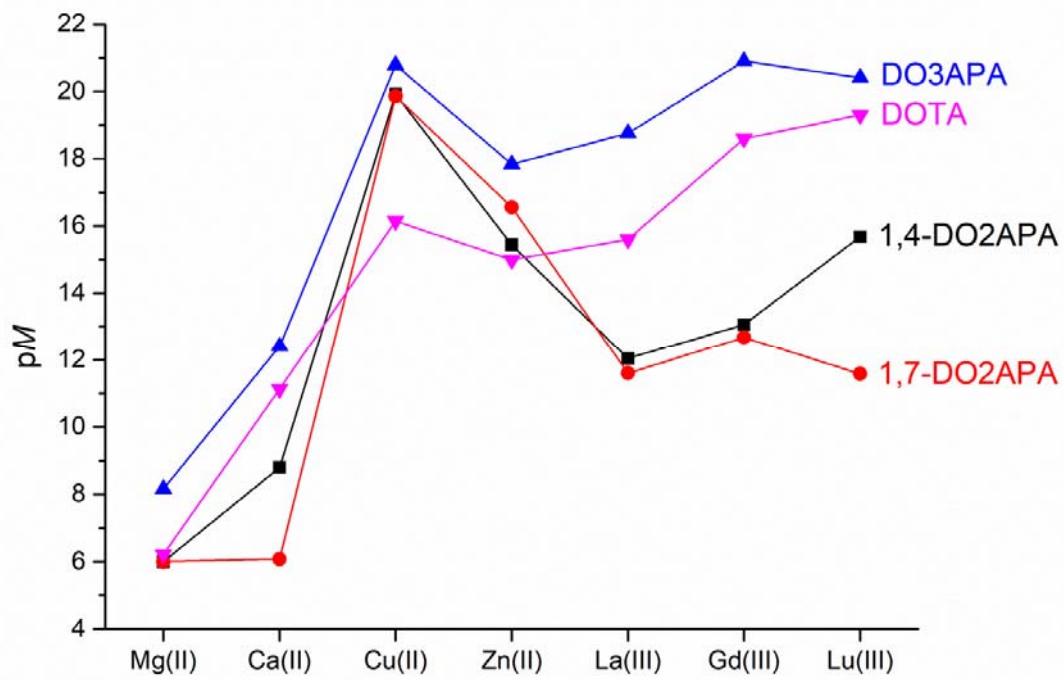


Figure S10. Plot of the pM values calculated for the complexes investigated in this work and related systems (pM are defined as $-\log[M]_{\text{free}}$ for $[M]_{\text{tot}} = 1 \mu\text{M}$ and $[L]_{\text{tot}} = 10 \mu\text{M}$).

Table S1. Calculated bond distances (\AA), Electron Densities (ρ_{BCP} , au) and Laplacian of the electron densities ($\nabla^2\rho_{\text{BCP}}$) at the Bond Critical Points (BCP) of $[\text{Ln}(1,4\text{-DO2APA})(\text{H}_2\text{O})]\cdot 2\text{H}_2\text{O}$ ($\text{Ln} = \text{La, Gd}$), $[\text{Yb}(1,4\text{-DO2APA})]$ and $[\text{Ln}(1,7\text{-DO2APA})(\text{H}_2\text{O})]\cdot 2\text{H}_2\text{O}$ ($\text{Ln} = \text{La, Gd, Yb}$) complexes.

| $[\text{La}(1,4\text{-DO2APA})(\text{H}_2\text{O})]\cdot 2\text{H}_2\text{O}$ | | | $[\text{La}(1,7\text{-DO2APA})(\text{H}_2\text{O})]\cdot 2\text{H}_2\text{O}$ | | | |
|---|---------------------|-----------------------------|---|---------------------|-----------------------------|------------|
| Dist. / \AA | ρ_{BCP} | $\nabla^2\rho_{\text{BCP}}$ | Dist. / \AA | ρ_{BCP} | $\nabla^2\rho_{\text{BCP}}$ | |
| N1 | 2.837 | 0.02752338 | 0.0832050 | 2.847 | 0.02792989 | 0.0830502 |
| N2 | 2.920 | 0.0236401 | 0.0706025 | 2.842 | 0.027788 | 0.0846408 |
| N3 | 2.894 | 0.0251662 | 0.07475026 | 2.784 | 0.0313689 | 0.0965942 |
| N4 | 2.844 | 0.0275234 | 0.0832050 | 2.869 | 0.0267946 | 0.0794231 |
| N5 | 2.776 | 0.0297587 | 0.101439 | 2.558 | 0.034166 | 0.118171 |
| O1 | 2.433 | 0.0517792 | 0.214607 | 2.471 | 0.0473895 | 0.2007997 |
| O2 | 2.498 | 0.0448113 | 0.184735 | 2.513 | 0.0440699 | 0.181166 |
| O3 | 2.535 | 0.041089 | 0.168724 | 2.515 | 0.0435705 | 0.175213 |
| O1w | 2.621 | 0.0348560 | 0.134331 | 2.598 | 0.0382708 | 0.141548 |
| $[\text{Gd}(1,4\text{-DO2APA})(\text{H}_2\text{O})]\cdot 2\text{H}_2\text{O}$ | | | $[\text{Gd}(1,7\text{-DO2APA})(\text{H}_2\text{O})]\cdot 2\text{H}_2\text{O}$ | | | |
| Dist. / \AA | ρ_{BCP} | ∇_{BCP} | Dist. / \AA | ρ_{BCP} | ∇_{BCP} | |
| N1 | 2.723 | 0.0293270 | 0.0938556 | 2.718 | 0.0298887 | 0.09447919 |
| N2 | 2.783 | 0.02571104 | 0.0807451 | 2.753 | 0.02747341 | 0.08717076 |
| N3 | 2.839 | 0.0232795 | 0.0697569 | 2.726 | 0.0293295 | 0.0930299 |
| N4 | 2.772 | 0.0265157 | 0.082573 | 2.765 | 0.02720199 | 0.0840305 |
| N5 | 2.594 | 0.03558967 | 0.1320789 | 2.558 | 0.0381876 | 0.1433595 |
| O1 | 2.322 | 0.055531 | 0.254203 | 2.350 | 0.0514536 | 0.2383966 |
| O2 | 2.360 | 0.05021481 | 0.231004 | 2.394 | 0.04700327 | 0.212644 |
| O3 | 2.426 | 0.0435386 | 0.192338 | 2.437 | 0.0428661 | 0.18303587 |
| O1w | 2.554 | 0.03350747 | 0.1325180 | 2.473 | 0.04101868 | 0.168487 |
| $[\text{Yb}(1,4\text{-DO2APA})]^a$ | | | $[\text{Yb}(1,7\text{-DO2APA})(\text{H}_2\text{O})]\cdot 2\text{H}_2\text{O}$ | | | |
| Dist. / \AA | ρ_{BCP} | ∇_{BCP} | Dist. / \AA | ρ_{BCP} | ∇_{BCP} | |
| N1 | 2.576 | 0.0352872 | 0.118595 | 2.653 | 0.03005709 | 0.0957879 |
| N2 | 2.623 | 0.0317077 | 0.1053925 | 2.715 | 0.0262230 | 0.08262397 |
| N3 | 2.651 | 0.0303518 | 0.09680357 | 2.690 | 0.0278973 | 0.0875377 |
| N4 | 2.591 | 0.0341603 | 0.113992 | 2.734 | 0.0255916 | 0.0776646 |
| N5 | 2.461 | 0.04196239 | 0.163681 | 2.490 | 0.0389719 | 0.1490742 |
| O1 | 2.237 | 0.0595699 | 0.286277 | 2.278 | 0.0534523 | 0.2561475 |
| O2 | 2.255 | 0.05715818 | 0.274277 | 2.320 | 0.0487189 | 0.227996 |
| O3 | 2.285 | 0.0531969 | 0.2514386 | 2.385 | 0.0423149 | 0.1830415 |
| O1w | | | | 2.390 | 0.0430668 | 0.1842383 |

^a Calculations performed on the $[\text{Yb}(1,4\text{-DO2APA})]\cdot 3\text{H}_2\text{O}$ provide very similar results, with ρ_{BCP} values of 0.0603, 0.05685 and 0.05098 au for the Yb-O1, Yb-O2 and Yb-O3 bonds, respectively.

Table S2. Optimised Cartesian coordinates (\AA) obtained with DFT calculations for the [La(1,4-DO2APA)(H₂O)]·2H₂O system (0 imaginary frequencies).

| Center Number | Atomic Number | | Coordinates (Angstroms) | | |
|------------------|------------------|---|-------------------------|-----------|-----------|
| | | | X | Y | Z |
| 1 | 7 | 0 | -0.988124 | -2.358955 | -0.429876 |
| 2 | 6 | 0 | -0.054286 | -3.237134 | -1.191240 |
| 3 | 6 | 0 | 1.386524 | -3.156607 | -0.702625 |
| 4 | 7 | 0 | 1.993967 | -1.810704 | -0.830394 |
| 5 | 6 | 0 | 3.244750 | -1.761030 | -0.027351 |
| 6 | 6 | 0 | 2.981941 | -1.621215 | 1.469704 |
| 7 | 7 | 0 | 2.204466 | -0.412030 | 1.858153 |
| 8 | 6 | 0 | 1.565677 | -0.646895 | 3.183589 |
| 9 | 6 | 0 | 0.354604 | -1.574730 | 3.098937 |
| 10 | 7 | 0 | -0.779367 | -0.995518 | 2.333100 |
| 11 | 6 | 0 | -1.758392 | -2.059255 | 1.984779 |
| 12 | 6 | 0 | -1.296295 | -3.004602 | 0.877197 |
| 13 | 6 | 0 | 2.297570 | -1.508756 | -2.249128 |
| 14 | 6 | 0 | 1.090508 | -1.019693 | -3.071437 |
| 15 | 8 | 0 | 1.089747 | -1.221008 | -4.293481 |
| 16 | 8 | 0 | 0.178886 | -0.371229 | -2.413325 |
| 17 | 6 | 0 | 3.084782 | 0.780414 | 1.919291 |
| 18 | 6 | 0 | 3.295975 | 1.462525 | 0.558131 |
| 19 | 8 | 0 | 4.115367 | 2.408531 | 0.500809 |
| 20 | 8 | 0 | 2.571603 | 1.057088 | -0.414839 |
| 21 | 6 | 0 | -1.475135 | -0.002554 | 3.185170 |
| 22 | 1 | 0 | 2.757648 | -2.368270 | -2.756746 |
| 23 | 1 | 0 | 3.017200 | -0.683730 | -2.257934 |
| 24 | 1 | 0 | 4.059406 | 0.545425 | 2.370162 |
| 25 | 1 | 0 | 2.608002 | 1.527190 | 2.563160 |
| 26 | 1 | 0 | -2.320994 | 0.411290 | 2.637552 |
| 27 | 1 | 0 | -1.835380 | -0.469059 | 4.115061 |
| 28 | 1 | 0 | -0.106061 | -2.950217 | -2.242719 |
| 29 | 1 | 0 | -0.381631 | -4.286806 | -1.132416 |
| 30 | 1 | 0 | 1.980377 | -3.896442 | -1.263830 |
| 31 | 1 | 0 | 1.437638 | -3.451804 | 0.348540 |
| 32 | 1 | 0 | 3.843617 | -2.672395 | -0.183441 |
| 33 | 1 | 0 | 3.831886 | -0.916476 | -0.384640 |
| 34 | 1 | 0 | 3.949570 | -1.624083 | 1.994706 |
| 35 | 1 | 0 | 2.437262 | -2.497481 | 1.827313 |
| 36 | 1 | 0 | 2.287213 | -1.074292 | 3.896098 |
| 37 | 1 | 0 | 1.262068 | 0.324285 | 3.582488 |
| 38 | 1 | 0 | 0.641632 | -2.516705 | 2.626781 |
| 39 | 1 | 0 | 0.030355 | -1.822744 | 4.122181 |
| 40 | 1 | 0 | -2.686038 | -1.563330 | 1.695339 |
| 41 | 1 | 0 | -1.986590 | -2.671202 | 2.872883 |
| 42 | 1 | 0 | -0.397027 | -3.531855 | 1.203380 |
| 43 | 1 | 0 | -2.070842 | -3.775442 | 0.743523 |
| 44 | 57 | 0 | 0.225796 | 0.271947 | -0.067067 |
| 45 | 6 | 0 | -2.211391 | -2.202183 | -1.254373 |
| 46 | 1 | 0 | -1.874836 | -1.948467 | -2.265509 |
| 47 | 1 | 0 | -2.772407 | -3.146820 | -1.313215 |
| 48 | 6 | 0 | -3.124409 | -1.085925 | -0.809451 |
| 49 | 6 | 0 | -4.514927 | -1.167104 | -0.953979 |
| 50 | 6 | 0 | -3.279900 | 1.093770 | -0.027319 |
| 51 | 6 | 0 | -5.293804 | -0.053267 | -0.636789 |
| 52 | 1 | 0 | -4.970601 | -2.083908 | -1.312692 |
| 53 | 6 | 0 | -4.666699 | 1.106601 | -0.178389 |
| 54 | 1 | 0 | -6.372954 | -0.091589 | -0.745490 |
| 55 | 1 | 0 | -5.219605 | 2.004113 | 0.071774 |

| | | | | | |
|----|---|---|-----------|----------|-----------|
| 56 | 7 | 0 | -2.525573 | 0.021551 | -0.340107 |
| 57 | 6 | 0 | -2.510619 | 2.291189 | 0.492542 |
| 58 | 8 | 0 | -3.079996 | 3.409529 | 0.497402 |
| 59 | 8 | 0 | -1.311995 | 2.057113 | 0.867498 |
| 60 | 1 | 0 | -0.803254 | 0.818654 | 3.437441 |
| 61 | 8 | 0 | 0.419675 | 2.599963 | -1.254752 |
| 62 | 1 | 0 | -0.080840 | 3.371422 | -0.879908 |
| 63 | 1 | 0 | 1.343545 | 2.933413 | -1.405235 |
| 64 | 8 | 0 | 2.915957 | 3.737659 | -1.593437 |
| 65 | 8 | 0 | -0.883599 | 4.831047 | -0.293282 |
| 66 | 1 | 0 | 2.835048 | 4.642262 | -1.256760 |
| 67 | 1 | 0 | 3.439636 | 3.260058 | -0.896177 |
| 68 | 1 | 0 | -1.688772 | 4.423988 | 0.119992 |
| 69 | 1 | 0 | -1.226253 | 5.298775 | -1.069254 |

E(RTPSSh) = -1765.4330318 Hartree
 Zero-point correction = 0.566665 (/Particle)
 Thermal correction to Energy = 0.603155
 Thermal correction to Enthalpy = 0.604099
 Thermal correction to Gibbs Free Energy = 0.501653
 Sum of electronic and zero-point Energies = -1764.866366
 Sum of electronic and thermal Energies = -1764.829877
 Sum of electronic and thermal Enthalpies = -1764.828932
 Sum of electronic and thermal Free Energies = -1764.931379

Table S3. Optimised Cartesian coordinates (\AA) obtained with DFT calculations for the [La(1,7-DO2APA)(H₂O)]·2H₂O system (0 imaginary frequencies).

| Center Number | Atomic Number | | Coordinates (Angstroms) | | |
|------------------|------------------|---|-------------------------|-----------|-----------|
| | | | X | Y | Z |
| 1 | 7 | 0 | 0.348358 | -1.218903 | -2.225744 |
| 2 | 6 | 0 | -0.623901 | -2.343135 | -2.402208 |
| 3 | 6 | 0 | -2.070129 | -1.983606 | -2.078791 |
| 4 | 7 | 0 | -2.317812 | -1.691455 | -0.641279 |
| 5 | 6 | 0 | -3.617409 | -0.977274 | -0.483137 |
| 6 | 6 | 0 | -3.600654 | 0.453292 | -1.017919 |
| 7 | 7 | 0 | -2.654652 | 1.338044 | -0.288818 |
| 8 | 6 | 0 | -2.336872 | 2.538543 | -1.106296 |
| 9 | 6 | 0 | -1.347156 | 2.265435 | -2.234545 |
| 10 | 7 | 0 | -0.002800 | 1.809015 | -1.782371 |
| 11 | 6 | 0 | 0.722254 | 1.183391 | -2.926119 |
| 12 | 6 | 0 | 0.175923 | -0.196279 | -3.297474 |
| 13 | 6 | 0 | -2.333048 | -2.947672 | 0.165094 |
| 14 | 6 | 0 | -1.110357 | -3.102759 | 1.082939 |
| 15 | 8 | 0 | -1.213692 | -3.821693 | 2.098667 |
| 16 | 8 | 0 | -0.051377 | -2.458177 | 0.740392 |
| 17 | 6 | 0 | 0.768827 | 2.963477 | -1.255903 |
| 18 | 6 | 0 | 0.417317 | 3.359036 | 0.191775 |
| 19 | 8 | 0 | 0.593400 | 4.527641 | 0.549285 |
| 20 | 8 | 0 | 0.005386 | 2.384859 | 0.950120 |
| 21 | 1 | 0 | -2.384777 | -3.826001 | -0.492260 |
| 22 | 1 | 0 | -3.228819 | -2.972949 | 0.789256 |
| 23 | 1 | 0 | 1.829016 | 2.686514 | -1.245431 |
| 24 | 1 | 0 | 0.664569 | 3.842897 | -1.904830 |
| 25 | 1 | 0 | -0.299227 | -3.146016 | -1.736971 |
| 26 | 1 | 0 | -0.585061 | -2.722294 | -3.434274 |
| 27 | 1 | 0 | -2.706766 | -2.819502 | -2.406698 |
| 28 | 1 | 0 | -2.379620 | -1.116499 | -2.664577 |
| 29 | 1 | 0 | -4.427424 | -1.527757 | -0.985660 |
| 30 | 1 | 0 | -3.846469 | -0.964115 | 0.585379 |
| 31 | 1 | 0 | -4.623034 | 0.856627 | -0.951694 |
| 32 | 1 | 0 | -3.338720 | 0.461731 | -2.078176 |
| 33 | 1 | 0 | -3.255566 | 2.951269 | -1.552288 |
| 34 | 1 | 0 | -1.945019 | 3.300334 | -0.430227 |
| 35 | 1 | 0 | -1.758290 | 1.504637 | -2.900926 |
| 36 | 1 | 0 | -1.241813 | 3.181635 | -2.835070 |
| 37 | 1 | 0 | 1.775915 | 1.102855 | -2.646024 |
| 38 | 1 | 0 | 0.673427 | 1.828141 | -3.816416 |
| 39 | 1 | 0 | -0.887687 | -0.123505 | -3.530287 |
| 40 | 1 | 0 | 0.671076 | -0.528145 | -4.221509 |
| 41 | 6 | 0 | 1.722070 | -1.792455 | -2.300436 |
| 42 | 1 | 0 | 1.674773 | -2.805737 | -1.888078 |
| 43 | 1 | 0 | 2.047800 | -1.887211 | -3.344745 |
| 44 | 6 | 0 | 2.768123 | -1.068636 | -1.483985 |
| 45 | 6 | 0 | 4.108136 | -0.996453 | -1.881541 |
| 46 | 6 | 0 | 3.279223 | -0.170163 | 0.600648 |
| 47 | 6 | 0 | 5.048395 | -0.476820 | -0.988708 |
| 48 | 1 | 0 | 4.405079 | -1.348645 | -2.863591 |
| 49 | 6 | 0 | 4.634350 | -0.075430 | 0.282462 |
| 50 | 1 | 0 | 6.092368 | -0.405255 | -1.276674 |
| 51 | 1 | 0 | 5.324685 | 0.299937 | 1.028330 |
| 52 | 7 | 0 | 2.367881 | -0.629403 | -0.279038 |
| 53 | 6 | 0 | 2.756426 | 0.164022 | 1.990603 |
| 54 | 8 | 0 | 3.556599 | 0.570990 | 2.843751 |
| 55 | 8 | 0 | 1.487202 | -0.043894 | 2.158856 |

| | | | | | |
|----|----|---|-----------|-----------|----------|
| 56 | 6 | 0 | -3.303309 | 1.803406 | 0.960219 |
| 57 | 1 | 0 | -2.583922 | 2.383937 | 1.538549 |
| 58 | 1 | 0 | -4.181827 | 2.427329 | 0.736876 |
| 59 | 1 | 0 | -3.616445 | 0.947797 | 1.558597 |
| 60 | 8 | 0 | -1.519171 | -0.176484 | 2.531856 |
| 61 | 1 | 0 | -1.391543 | 0.700613 | 2.990276 |
| 62 | 1 | 0 | -1.025986 | -0.842881 | 3.096626 |
| 63 | 8 | 0 | 0.080219 | -1.939899 | 3.743501 |
| 64 | 8 | 0 | -0.823935 | 2.250382 | 3.489693 |
| 65 | 1 | 0 | 0.789383 | -1.493000 | 3.234369 |
| 66 | 1 | 0 | -0.170209 | -2.728620 | 3.205472 |
| 67 | 1 | 0 | -1.491527 | 2.918345 | 3.702123 |
| 68 | 1 | 0 | -0.454464 | 2.508650 | 2.602005 |
| 69 | 57 | 0 | -0.203106 | -0.032378 | 0.296671 |

E(RTPSSh) = -1765.431957 Hartree
 Zero-point correction = 0.567510
 Thermal correction to Energy = 0.603661
 Thermal correction to Enthalpy = 0.604605
 Thermal correction to Gibbs Free Energy = 0.502671
 Sum of electronic and zero-point Energies = -1764.864447
 Sum of electronic and thermal Energies = -1764.828296
 Sum of electronic and thermal Enthalpies = -1764.827352
 Sum of electronic and thermal Free Energies = -1764.929286

Table S4. Optimised Cartesian coordinates (\AA) obtained with DFT calculations for the [Gd(1,4-DO2APA)(H₂O)]·2H₂O system (0 imaginary frequencies).

| Center Number | Atomic Number | | Coordinates (Angstroms) | | |
|------------------|------------------|---|-------------------------|-----------|-----------|
| | | | X | Y | Z |
| 1 | 7 | 0 | -0.917942 | -2.356764 | -0.438020 |
| 2 | 6 | 0 | 0.059910 | -3.246388 | -1.129149 |
| 3 | 6 | 0 | 1.466755 | -3.125678 | -0.556593 |
| 4 | 7 | 0 | 2.032788 | -1.759939 | -0.670863 |
| 5 | 6 | 0 | 3.235817 | -1.646700 | 0.196319 |
| 6 | 6 | 0 | 2.881025 | -1.468582 | 1.669244 |
| 7 | 7 | 0 | 2.030366 | -0.281723 | 1.959638 |
| 8 | 6 | 0 | 1.325631 | -0.489854 | 3.254081 |
| 9 | 6 | 0 | 0.160273 | -1.468396 | 3.125186 |
| 10 | 7 | 0 | -0.941621 | -0.949304 | 2.272083 |
| 11 | 6 | 0 | -1.863540 | -2.056311 | 1.904150 |
| 12 | 6 | 0 | -1.306688 | -3.003300 | 0.847507 |
| 13 | 6 | 0 | 2.399891 | -1.471642 | -2.078207 |
| 14 | 6 | 0 | 1.212897 | -1.028661 | -2.948403 |
| 15 | 8 | 0 | 1.262435 | -1.221472 | -4.170254 |
| 16 | 8 | 0 | 0.251586 | -0.426089 | -2.318240 |
| 17 | 6 | 0 | 2.851453 | 0.954091 | 2.003346 |
| 18 | 6 | 0 | 3.060205 | 1.574811 | 0.614121 |
| 19 | 8 | 0 | 3.844486 | 2.539867 | 0.492190 |
| 20 | 8 | 0 | 2.360870 | 1.079826 | -0.339288 |
| 21 | 6 | 0 | -1.724815 | 0.023353 | 3.071222 |
| 22 | 1 | 0 | 2.903380 | -2.326955 | -2.549394 |
| 23 | 1 | 0 | 3.096431 | -0.627891 | -2.068315 |
| 24 | 1 | 0 | 3.823351 | 0.784195 | 2.486853 |
| 25 | 1 | 0 | 2.320597 | 1.701994 | 2.601590 |
| 26 | 1 | 0 | -2.572720 | 0.375270 | 2.484567 |
| 27 | 1 | 0 | -2.099393 | -0.448437 | 3.992680 |
| 28 | 1 | 0 | 0.063836 | -2.989629 | -2.189368 |
| 29 | 1 | 0 | -0.260055 | -4.296680 | -1.057638 |
| 30 | 1 | 0 | 2.115539 | -3.853080 | -1.069964 |
| 31 | 1 | 0 | 1.463002 | -3.402851 | 0.500758 |
| 32 | 1 | 0 | 3.870393 | -2.541299 | 0.101219 |
| 33 | 1 | 0 | 3.816759 | -0.795160 | -0.155698 |
| 34 | 1 | 0 | 3.813736 | -1.409610 | 2.250440 |
| 35 | 1 | 0 | 2.351763 | -2.354590 | 2.026094 |
| 36 | 1 | 0 | 2.018000 | -0.860224 | 4.024759 |
| 37 | 1 | 0 | 0.958855 | 0.482034 | 3.593308 |
| 38 | 1 | 0 | 0.511796 | -2.411781 | 2.701634 |
| 39 | 1 | 0 | -0.220556 | -1.700144 | 4.132361 |
| 40 | 1 | 0 | -2.792625 | -1.602893 | 1.554648 |
| 41 | 1 | 0 | -2.117197 | -2.654519 | 2.794356 |
| 42 | 1 | 0 | -0.420874 | -3.506535 | 1.241650 |
| 43 | 1 | 0 | -2.051927 | -3.791642 | 0.662943 |
| 44 | 64 | 0 | 0.201364 | 0.165698 | -0.075290 |
| 45 | 6 | 0 | -2.091878 | -2.188136 | -1.333964 |
| 46 | 1 | 0 | -1.695555 | -1.968442 | -2.330606 |
| 47 | 1 | 0 | -2.679214 | -3.115492 | -1.397127 |
| 48 | 6 | 0 | -2.984233 | -1.033234 | -0.949035 |
| 49 | 6 | 0 | -4.368360 | -1.052817 | -1.159640 |
| 50 | 6 | 0 | -3.093027 | 1.131896 | -0.107821 |
| 51 | 6 | 0 | -5.115778 | 0.084256 | -0.849097 |
| 52 | 1 | 0 | -4.844161 | -1.943084 | -1.556657 |
| 53 | 6 | 0 | -4.469429 | 1.202482 | -0.317496 |
| 54 | 1 | 0 | -6.189112 | 0.092359 | -1.008976 |
| 55 | 1 | 0 | -5.001582 | 2.107653 | -0.050712 |

| | | | | | |
|----|---|---|-----------|----------|-----------|
| 56 | 7 | 0 | -2.367344 | 0.044371 | -0.435666 |
| 57 | 6 | 0 | -2.301452 | 2.258652 | 0.523302 |
| 58 | 8 | 0 | -2.835800 | 3.388466 | 0.616368 |
| 59 | 8 | 0 | -1.117936 | 1.951382 | 0.901388 |
| 60 | 1 | 0 | -1.111539 | 0.885310 | 3.331668 |
| 61 | 8 | 0 | 0.200777 | 2.328560 | -1.434296 |
| 62 | 1 | 0 | -0.125468 | 3.132423 | -0.952956 |
| 63 | 1 | 0 | 1.129424 | 2.576231 | -1.679209 |
| 64 | 8 | 0 | 2.723987 | 3.430706 | -1.947431 |
| 65 | 8 | 0 | -0.597136 | 4.700280 | -0.228964 |
| 66 | 1 | 0 | 2.584584 | 4.377198 | -1.795935 |
| 67 | 1 | 0 | 3.193492 | 3.116712 | -1.133988 |
| 68 | 1 | 0 | -1.410557 | 4.370299 | 0.229846 |
| 69 | 1 | 0 | -0.937519 | 5.246850 | -0.952741 |

E(RTPSSh) = -1769.7412537 Hartree
 Zero-point correction = 0.567662
 Thermal correction to Energy = 0.603848
 Thermal correction to Enthalpy = 0.604793
 Thermal correction to Gibbs Free Energy = 0.503672
 Sum of electronic and zero-point Energies = -1769.173592
 Sum of electronic and thermal Energies = -1769.137405
 Sum of electronic and thermal Enthalpies = -1769.136461
 Sum of electronic and thermal Free Energies = -1769.237581

Table S5. Optimised Cartesian coordinates (\AA) obtained with DFT calculations for the [Gd(1,7-DO2APA)(H₂O)]·2H₂O system (0 imaginary frequencies).

| Center Number | Atomic Number | | Coordinates (Angstroms) | | |
|------------------|------------------|---|-------------------------|-----------|-----------|
| | | | X | Y | Z |
| 1 | 7 | 0 | 0.083849 | -1.516634 | -2.029671 |
| 2 | 6 | 0 | -1.070545 | -2.459868 | -2.108894 |
| 3 | 6 | 0 | -2.414535 | -1.784856 | -1.866032 |
| 4 | 7 | 0 | -2.565988 | -1.224375 | -0.496054 |
| 5 | 6 | 0 | -3.689354 | -0.244559 | -0.476508 |
| 6 | 6 | 0 | -3.336627 | 1.067548 | -1.168236 |
| 7 | 7 | 0 | -2.229529 | 1.784742 | -0.481293 |
| 8 | 6 | 0 | -1.632805 | 2.801203 | -1.388214 |
| 9 | 6 | 0 | -0.726750 | 2.208472 | -2.459606 |
| 10 | 7 | 0 | 0.454449 | 1.461101 | -1.938712 |
| 11 | 6 | 0 | 0.983011 | 0.600155 | -3.032765 |
| 12 | 6 | 0 | 0.126754 | -0.646244 | -3.236745 |
| 13 | 6 | 0 | -2.824623 | -2.309171 | 0.492292 |
| 14 | 6 | 0 | -1.587898 | -2.727244 | 1.299783 |
| 15 | 8 | 0 | -1.757005 | -3.462909 | 2.292360 |
| 16 | 8 | 0 | -0.454659 | -2.248114 | 0.921122 |
| 17 | 6 | 0 | 1.494931 | 2.415364 | -1.484557 |
| 18 | 6 | 0 | 1.214230 | 2.996126 | -0.089993 |
| 19 | 8 | 0 | 1.662290 | 4.105847 | 0.210997 |
| 20 | 8 | 0 | 0.542750 | 2.206568 | 0.697436 |
| 21 | 1 | 0 | -3.249988 | -3.196330 | 0.003641 |
| 22 | 1 | 0 | -3.567990 | -1.963459 | 1.214091 |
| 23 | 1 | 0 | 2.444527 | 1.873686 | -1.411612 |
| 24 | 1 | 0 | 1.633273 | 3.234166 | -2.202682 |
| 25 | 1 | 0 | -0.908076 | -3.228330 | -1.351133 |
| 26 | 1 | 0 | -1.099134 | -2.955070 | -3.090730 |
| 27 | 1 | 0 | -3.209286 | -2.521084 | -2.058625 |
| 28 | 1 | 0 | -2.564005 | -0.976530 | -2.584236 |
| 29 | 1 | 0 | -4.588251 | -0.669538 | -0.947234 |
| 30 | 1 | 0 | -3.926539 | -0.050376 | 0.571765 |
| 31 | 1 | 0 | -4.235588 | 1.701586 | -1.203605 |
| 32 | 1 | 0 | -3.046145 | 0.887056 | -2.205603 |
| 33 | 1 | 0 | -2.427403 | 3.372751 | -1.893074 |
| 34 | 1 | 0 | -1.080781 | 3.508677 | -0.767344 |
| 35 | 1 | 0 | -1.303452 | 1.526661 | -3.087958 |
| 36 | 1 | 0 | -0.385292 | 3.022961 | -3.115887 |
| 37 | 1 | 0 | 2.005744 | 0.316402 | -2.774974 |
| 38 | 1 | 0 | 1.033378 | 1.157600 | -3.979618 |
| 39 | 1 | 0 | -0.896268 | -0.358877 | -3.486882 |
| 40 | 1 | 0 | 0.512490 | -1.208371 | -4.099715 |
| 41 | 6 | 0 | 1.338725 | -2.311351 | -1.959277 |
| 42 | 1 | 0 | 1.124638 | -3.209191 | -1.370201 |
| 43 | 1 | 0 | 1.652335 | -2.643393 | -2.957947 |
| 44 | 6 | 0 | 2.470001 | -1.610984 | -1.244791 |
| 45 | 6 | 0 | 3.815773 | -1.808621 | -1.573783 |
| 46 | 6 | 0 | 3.054386 | -0.447610 | 0.683519 |
| 47 | 6 | 0 | 4.798426 | -1.263856 | -0.743743 |
| 48 | 1 | 0 | 4.082462 | -2.382254 | -2.454830 |
| 49 | 6 | 0 | 4.415805 | -0.591919 | 0.419382 |
| 50 | 1 | 0 | 5.848470 | -1.390769 | -0.986938 |
| 51 | 1 | 0 | 5.135248 | -0.199681 | 1.128231 |
| 52 | 7 | 0 | 2.108797 | -0.899095 | -0.164158 |
| 53 | 6 | 0 | 2.527780 | 0.095374 | 2.002018 |
| 54 | 8 | 0 | 3.325552 | 0.581747 | 2.814896 |
| 55 | 8 | 0 | 1.252723 | -0.066422 | 2.161860 |

| | | | | | |
|----|----|---|-----------|-----------|----------|
| 56 | 6 | 0 | -2.791717 | 2.514706 | 0.680897 |
| 57 | 1 | 0 | -1.975955 | 2.976463 | 1.236722 |
| 58 | 1 | 0 | -3.494041 | 3.292877 | 0.347395 |
| 59 | 1 | 0 | -3.312100 | 1.822343 | 1.341876 |
| 60 | 8 | 0 | -1.589119 | 0.285385 | 2.307498 |
| 61 | 1 | 0 | -1.297083 | 1.153913 | 2.705132 |
| 62 | 1 | 0 | -1.255846 | -0.399670 | 2.961404 |
| 63 | 8 | 0 | -0.383764 | -1.533562 | 3.864613 |
| 64 | 8 | 0 | -0.396173 | 2.543989 | 3.185303 |
| 65 | 1 | 0 | 0.403224 | -1.232371 | 3.359114 |
| 66 | 1 | 0 | -0.672873 | -2.361383 | 3.418345 |
| 67 | 1 | 0 | -0.855532 | 3.391167 | 3.275791 |
| 68 | 1 | 0 | 0.087446 | 2.590147 | 2.316977 |
| 69 | 64 | 0 | -0.252863 | -0.005909 | 0.246912 |

E(RTPSSh) = -1769.7458379 Hartree

Zero-point correction = 0.568350

Thermal correction to Energy = 0.604124

Thermal correction to Enthalpy = 0.605068

Thermal correction to Gibbs Free Energy = 0.504950

Sum of electronic and zero-point Energies = -1769.177488

Sum of electronic and thermal Energies = -1769.141714

Sum of electronic and thermal Enthalpies = -1769.140770

Sum of electronic and thermal Free Energies = -1769.240888

Table S6. Optimised Cartesian coordinates (\AA) obtained with DFT calculations for the [Yb(1,4-DO2APA)(H₂O)]·2H₂O system (0 imaginary frequencies).

| Center Number | Atomic Number | | Coordinates (Angstroms) | | |
|------------------|------------------|---|-------------------------|-----------|-----------|
| | | | X | Y | Z |
| 1 | 7 | 0 | -0.359115 | -2.572392 | -0.011558 |
| 2 | 6 | 0 | -1.685231 | -3.003622 | -0.549683 |
| 3 | 6 | 0 | -2.829704 | -2.133715 | -0.025548 |
| 4 | 7 | 0 | -2.692821 | -0.699957 | -0.395645 |
| 5 | 6 | 0 | -3.571131 | 0.155123 | 0.449442 |
| 6 | 6 | 0 | -3.002813 | 0.374106 | 1.845597 |
| 7 | 7 | 0 | -1.645334 | 0.995535 | 1.865281 |
| 8 | 6 | 0 | -1.021597 | 0.720842 | 3.192878 |
| 9 | 6 | 0 | -0.511052 | -0.711126 | 3.306095 |
| 10 | 7 | 0 | 0.602346 | -0.976234 | 2.361851 |
| 11 | 6 | 0 | 0.825318 | -2.435750 | 2.223436 |
| 12 | 6 | 0 | -0.225269 | -3.125425 | 1.366382 |
| 13 | 6 | 0 | -3.039841 | -0.508157 | -1.825411 |
| 14 | 6 | 0 | -1.890861 | -0.864087 | -2.775448 |
| 15 | 8 | 0 | -2.141957 | -1.183118 | -3.942335 |
| 16 | 8 | 0 | -0.701221 | -0.741059 | -2.262301 |
| 17 | 6 | 0 | -1.729205 | 2.466044 | 1.645440 |
| 18 | 6 | 0 | -1.592732 | 2.879866 | 0.174837 |
| 19 | 8 | 0 | -1.597822 | 4.095179 | -0.099253 |
| 20 | 8 | 0 | -1.430093 | 1.929674 | -0.677819 |
| 21 | 6 | 0 | 1.838747 | -0.397906 | 2.936621 |
| 22 | 1 | 0 | -3.943713 | -1.067205 | -2.100904 |
| 23 | 1 | 0 | -3.236887 | 0.557260 | -1.978247 |
| 24 | 1 | 0 | -2.657546 | 2.882820 | 2.059185 |
| 25 | 1 | 0 | -0.902433 | 2.944606 | 2.177088 |
| 26 | 1 | 0 | 2.680804 | -0.605199 | 2.275407 |
| 27 | 1 | 0 | 2.049984 | -0.841003 | 3.922108 |
| 28 | 1 | 0 | -1.643508 | -2.960426 | -1.638034 |
| 29 | 1 | 0 | -1.888076 | -4.049275 | -0.277558 |
| 30 | 1 | 0 | -3.779527 | -2.537584 | -0.407050 |
| 31 | 1 | 0 | -2.877282 | -2.198961 | 1.064509 |
| 32 | 1 | 0 | -4.574803 | -0.284700 | 0.544740 |
| 33 | 1 | 0 | -3.676028 | 1.112576 | -0.062043 |
| 34 | 1 | 0 | -3.704984 | 0.997319 | 2.418410 |
| 35 | 1 | 0 | -2.939598 | -0.581982 | 2.369590 |
| 36 | 1 | 0 | -1.736513 | 0.918196 | 4.004492 |
| 37 | 1 | 0 | -0.190023 | 1.417541 | 3.317108 |
| 38 | 1 | 0 | -1.319170 | -1.417425 | 3.101893 |
| 39 | 1 | 0 | -0.189297 | -0.894362 | 4.343428 |
| 40 | 1 | 0 | 1.818399 | -2.576917 | 1.791164 |
| 41 | 1 | 0 | 0.838065 | -2.924754 | 3.210808 |
| 42 | 1 | 0 | -1.201971 | -3.042946 | 1.848305 |
| 43 | 1 | 0 | 0.007668 | -4.199372 | 1.317928 |
| 44 | 70 | 0 | -0.230731 | 0.071480 | -0.162486 |
| 45 | 6 | 0 | 0.730884 | -3.077433 | -0.895562 |
| 46 | 1 | 0 | 0.396751 | -2.927633 | -1.927003 |
| 47 | 1 | 0 | 0.899538 | -4.152420 | -0.744424 |
| 48 | 6 | 0 | 2.029828 | -2.313230 | -0.731663 |
| 49 | 6 | 0 | 3.291370 | -2.878003 | -0.956754 |
| 50 | 6 | 0 | 2.990549 | -0.232246 | -0.265387 |
| 51 | 6 | 0 | 4.420795 | -2.064038 | -0.844956 |
| 52 | 1 | 0 | 3.383358 | -3.928701 | -1.209285 |
| 53 | 6 | 0 | 4.276096 | -0.717432 | -0.495188 |
| 54 | 1 | 0 | 5.407972 | -2.480733 | -1.016987 |
| 55 | 1 | 0 | 5.126253 | -0.054955 | -0.385361 |

| | | | | | |
|----|---|---|-----------|-----------|-----------|
| 56 | 7 | 0 | 1.906351 | -1.019524 | -0.400321 |
| 57 | 6 | 0 | 2.696732 | 1.190948 | 0.184415 |
| 58 | 8 | 0 | 3.627966 | 2.025340 | 0.138729 |
| 59 | 8 | 0 | 1.501908 | 1.410888 | 0.599608 |
| 60 | 1 | 0 | 1.743035 | 0.681777 | 3.039716 |
| 61 | 8 | 0 | 0.939435 | 1.232022 | -2.019849 |
| 62 | 1 | 0 | 0.416009 | 0.833327 | -2.736316 |
| 63 | 1 | 0 | 0.754107 | 2.223181 | -2.016985 |
| 64 | 8 | 0 | 0.585191 | 3.879841 | -1.945511 |
| 65 | 8 | 0 | 2.600670 | 4.522806 | -0.189633 |
| 66 | 1 | 0 | 1.305184 | 4.154136 | -1.319038 |
| 67 | 1 | 0 | -0.242991 | 4.007708 | -1.429619 |
| 68 | 1 | 0 | 2.977989 | 3.627420 | 0.023659 |
| 69 | 1 | 0 | 3.292508 | 4.951964 | -0.714254 |

E(RTPSSh) = -1773.2544264 Hartree
 Zero-point correction = 0.568391
 Thermal correction to Energy = 0.603976
 Thermal correction to Enthalpy = 0.604920
 Thermal correction to Gibbs Free Energy = 0.505134
 Sum of electronic and zero-point Energies = -1772.686036
 Sum of electronic and thermal Energies = -1772.650450
 Sum of electronic and thermal Enthalpies = -1772.649506
 Sum of electronic and thermal Free Energies = -1772.749292

Table S7. Optimised Cartesian coordinates (\AA) obtained with DFT calculations for the [Yb(1,7-DO2APA)(H₂O)]·2H₂O system (0 imaginary frequencies).

| Center Number | Atomic Number | | Coordinates (Angstroms) | | |
|------------------|------------------|---|-------------------------|-----------|-----------|
| | | | X | Y | Z |
| 1 | 7 | 0 | 0.036081 | -1.499935 | -2.026419 |
| 2 | 6 | 0 | -1.109814 | -2.452605 | -2.080617 |
| 3 | 6 | 0 | -2.444359 | -1.780744 | -1.791036 |
| 4 | 7 | 0 | -2.530362 | -1.185741 | -0.428979 |
| 5 | 6 | 0 | -3.662326 | -0.217113 | -0.390742 |
| 6 | 6 | 0 | -3.322980 | 1.086374 | -1.100458 |
| 7 | 7 | 0 | -2.197252 | 1.790946 | -0.434688 |
| 8 | 6 | 0 | -1.619069 | 2.810220 | -1.348544 |
| 9 | 6 | 0 | -0.745941 | 2.213212 | -2.441317 |
| 10 | 7 | 0 | 0.427696 | 1.439861 | -1.943735 |
| 11 | 6 | 0 | 0.924465 | 0.592097 | -3.061060 |
| 12 | 6 | 0 | 0.051815 | -0.643985 | -3.242785 |
| 13 | 6 | 0 | -2.748920 | -2.248430 | 0.588792 |
| 14 | 6 | 0 | -1.461347 | -2.736182 | 1.260694 |
| 15 | 8 | 0 | -1.558465 | -3.576972 | 2.175546 |
| 16 | 8 | 0 | -0.363001 | -2.184168 | 0.877210 |
| 17 | 6 | 0 | 1.486933 | 2.372815 | -1.490987 |
| 18 | 6 | 0 | 1.226261 | 2.924104 | -0.083345 |
| 19 | 8 | 0 | 1.697186 | 4.015325 | 0.248339 |
| 20 | 8 | 0 | 0.537383 | 2.128815 | 0.683322 |
| 21 | 1 | 0 | -3.291769 | -3.104979 | 0.166893 |
| 22 | 1 | 0 | -3.371956 | -1.841813 | 1.389239 |
| 23 | 1 | 0 | 2.431268 | 1.819813 | -1.442749 |
| 24 | 1 | 0 | 1.623811 | 3.204861 | -2.193924 |
| 25 | 1 | 0 | -0.920060 | -3.229511 | -1.338504 |
| 26 | 1 | 0 | -1.165944 | -2.938141 | -3.066001 |
| 27 | 1 | 0 | -3.245543 | -2.522157 | -1.927081 |
| 28 | 1 | 0 | -2.629562 | -0.989462 | -2.520133 |
| 29 | 1 | 0 | -4.567266 | -0.653924 | -0.837567 |
| 30 | 1 | 0 | -3.876313 | -0.014111 | 0.660421 |
| 31 | 1 | 0 | -4.216906 | 1.728029 | -1.122543 |
| 32 | 1 | 0 | -3.052278 | 0.896367 | -2.141734 |
| 33 | 1 | 0 | -2.422634 | 3.389269 | -1.830064 |
| 34 | 1 | 0 | -1.046986 | 3.511597 | -0.738809 |
| 35 | 1 | 0 | -1.345809 | 1.546713 | -3.064358 |
| 36 | 1 | 0 | -0.399497 | 3.025768 | -3.097240 |
| 37 | 1 | 0 | 1.952522 | 0.299958 | -2.836104 |
| 38 | 1 | 0 | 0.950862 | 1.159078 | -4.002888 |
| 39 | 1 | 0 | -0.974920 | -0.347096 | -3.465883 |
| 40 | 1 | 0 | 0.408622 | -1.217041 | -4.110969 |
| 41 | 6 | 0 | 1.299322 | -2.279792 | -1.971933 |
| 42 | 1 | 0 | 1.104591 | -3.177400 | -1.375825 |
| 43 | 1 | 0 | 1.604608 | -2.611424 | -2.973302 |
| 44 | 6 | 0 | 2.427669 | -1.563220 | -1.271667 |
| 45 | 6 | 0 | 3.774070 | -1.769069 | -1.593796 |
| 46 | 6 | 0 | 3.009153 | -0.391001 | 0.649194 |
| 47 | 6 | 0 | 4.756099 | -1.219541 | -0.766820 |
| 48 | 1 | 0 | 4.040722 | -2.355024 | -2.466710 |
| 49 | 6 | 0 | 4.370623 | -0.542478 | 0.392543 |
| 50 | 1 | 0 | 5.806534 | -1.351990 | -1.005284 |
| 51 | 1 | 0 | 5.087668 | -0.156147 | 1.107058 |
| 52 | 7 | 0 | 2.063666 | -0.834825 | -0.203415 |
| 53 | 6 | 0 | 2.475204 | 0.122008 | 1.974413 |
| 54 | 8 | 0 | 3.265998 | 0.583203 | 2.808839 |
| 55 | 8 | 0 | 1.201175 | -0.053712 | 2.118404 |

| | | | | | |
|----|----|---|-----------|-----------|----------|
| 56 | 6 | 0 | -2.733852 | 2.524110 | 0.737642 |
| 57 | 1 | 0 | -1.904505 | 2.976211 | 1.280510 |
| 58 | 1 | 0 | -3.431976 | 3.310431 | 0.414746 |
| 59 | 1 | 0 | -3.252330 | 1.837478 | 1.405530 |
| 60 | 8 | 0 | -1.546181 | 0.252027 | 2.211111 |
| 61 | 1 | 0 | -1.247266 | 1.107333 | 2.633535 |
| 62 | 1 | 0 | -1.232127 | -0.442165 | 2.863696 |
| 63 | 8 | 0 | -0.365861 | -1.551271 | 3.825413 |
| 64 | 8 | 0 | -0.339164 | 2.458934 | 3.196532 |
| 65 | 1 | 0 | 0.415877 | -1.214806 | 3.331619 |
| 66 | 1 | 0 | -0.590465 | -2.400178 | 3.385973 |
| 67 | 1 | 0 | -0.787269 | 3.312355 | 3.285710 |
| 68 | 1 | 0 | 0.142497 | 2.499153 | 2.327259 |
| 69 | 70 | 0 | -0.244937 | -0.005876 | 0.222848 |

E(RTPSSh) = -1773.2478177 Hartree

Zero-point correction = 0.569448

Thermal correction to Energy = 0.604810

Thermal correction to Enthalpy = 0.605754

Thermal correction to Gibbs Free Energy = 0.507154

Sum of electronic and zero-point Energies = -1772.678369

Sum of electronic and thermal Energies = -1772.643008

Sum of electronic and thermal Enthalpies = -1772.642064

Sum of electronic and thermal Free Energies = -1772.740664