

Supporting Information

Exploring the Relationship between Effective Mass, Transient Photoconductivity, and Photocatalytic Activity of $\text{Sr}_x\text{Pb}_{1-x}\text{BiO}_2\text{Cl}$ ($x = 0\text{--}1$) Oxyhalides

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Methods

Computational details

All periodic boundary condition (PBC) calculations were performed using Perdew–Burke–Ernzerhof (PBE) exchange correlation functional with projector augmented wave (PAW) pseudopotentials, and 600 eV plane-wave cut-off in Vienna ab initio simulation package (VASP) code.^{S1–S7} Note that the use of Heyd-Scuseria-Ernzerhof hybrid functional (HSE06),^{S8} instead of PBE, leads to a small difference in the band dispersion. In order to determine the atomic orbital energies of constituent elements in PbBiO₂Cl and SrBiO₂Cl, *ab initio* atomic orbital calculations were carried out. The orbital energies were estimated by the SOC approach with relativistic Hamiltonian based on ZORA with the PBE exchange correlation functional,^{S9, S10} as implemented in the Amsterdam density functional program package (ADF 2017).^{S11} ZORA triple-zeta + polarized (TZP) was used as basis set.^{S12}

DFT calculations were performed to compare the electron and hole effective masses in the solid solutions (Sr_{0.25}Pb_{0.75}BiO₂Cl, Sr_{0.5}Pb_{0.5}BiO₂Cl, and Sr_{0.75}Pb_{0.25}BiO₂Cl). The most part of the computational method is common to that for PbBiO₂Cl and SrBiO₂Cl which is summarized in main text. For the solid solutions, 4, 6, and 4 types of unit cells were considered for Sr_{0.25}Pb_{0.75}BiO₂Cl, Sr_{0.5}Pb_{0.5}BiO₂Cl, and Sr_{0.75}Pb_{0.25}BiO₂Cl solid solutions, respectively. Because, 4 ion sites of Pb or Sr exist in the unit cell at orthorhombic phase, and the 4, 6, and 4 types of unit cells can be generated for each solid solution according the ratio of Pb and Sr. In this study, geometry optimizations of the ions and lattice constants were performed for the all types of unit cells of each solid solution. The electron and hole effective masses were calculated for the most stable structures in each solid solution. The methodology of density functional theory (DFT) calculations for the solid solutions are the same as that for PbBiO₂Cl and SrBiO₂Cl.

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Table S1. Calculated effective masses (m_0 unit) in x, y, and z directions (m^{*xx} , m^{*yy} , and m^{*zz}) and average effective masses (m^{*avg}) of hole and electron for $\text{Sr}_x\text{Pb}_{1-x}\text{BiO}_2\text{Cl}$ ($x = 0.25, 0.50, 0.75$).

Effective mass	$x = 0.25$		$x = 0.5$		$x = 0.75$	
	Electron	Hole	Electron	Hole	Electron	Hole
m^{*xx}	0.39	3.31	0.54	1.16	0.56	1.19
m^{*yy}	0.36	1.21	1.54	1.34	1.35	10.19
m^{*zz}	1.66	46.48	2.49	4.02	8.57	9.36
m^{*avg}	0.50	2.61	1.03	1.61	1.14	2.87

Table S2. Lattice constants and volumes of $\text{Sr}_x\text{Pb}_{1-x}\text{BiO}_2\text{Cl}$.

x	a (Å)	b (Å)	c (Å)	V (Å ³)
0	5.5797(17)	5.5803(19)	12.4054(2)	386.26(14)
0.02	5.5799(3)	5.5816(3)	12.4137(2)	386.62(14)
0.05	5.5780(18)	5.5803(18)	12.4131(19)	386.38(13)
0.1	5.5806(4)	5.5822(4)	12.4250(2)	387.06(15)
0.15	5.5823(4)	5.5837(4)	12.4366(2)	387.64(14)
0.2	5.5866(3)	5.5881(3)	12.4556(2)	388.84(15)
0.3	5.5893(5)	5.5904(5)	12.4822(4)	390.03(2)
0.4	5.5939(5)	5.5948(4)	12.5095(5)	391.50(3)
0.5	5.603(7)	5.599(7)	12.5181(4)	392.71(3)
0.6	5.6119(5)	5.6025(5)	12.5171(4)	393.55(2)
0.8	5.6545(4)	5.5994(3)	12.4612(8)	394.54(5)
1	5.7011(2)	5.5937(2)	12.4241(7)	396.21(4)

Table S3. Calculated effective masses for a PbBiO₂Cl structure with the obtained lattice constants (Table S2).

Effective mass	Model 1 ^a		Model 2 ^b	
	Electron	Hole	Electron	Hole
m_{xx}^*	0.28	0.94	0.29	1.13
m_{yy}^*	0.27	0.98	0.28	1.00
m_{zz}^*	0.59	8.04	0.74	5.81
m_{avg}^*	0.33	1.36	0.35	1.46

^a The lattice constants were fixed and the ion positions are unfixed during the geometry optimization.

^b Both the lattice constants and the ion positions are unfixed during the geometry optimization.

Table S4. Integral breadths, full width at half maxima, and crystallite sizes for (111) facet peaks in the XRD patterns of Sr_xPb_{1-x}BiO₂Cl.

x	Integral breadth ^a (deg.)	FWHM ^a (deg.)	Crystallite size ^b (Å)
0	0.171(4)	0.137(2)	526
0.02	0.158(3)	0.127(2)	571
0.05	0.172(3)	0.1375(18)	524
0.1	0.173(3)	0.137(2)	520
0.15	0.187(4)	0.1491(18)	482
0.2	0.176(3)	0.142(2)	511
0.3	0.181(3)	0.1449(18)	497
0.4	0.207(4)	0.1643(13)	437
0.5	0.210(4)	0.1687(16)	429
0.6	0.232(4)	0.1837(16)	388
0.8	0.275(5)	0.2169(14)	328
1	0.273(6)	0.2032(19)	330

^aIntegral breadths and full-width at the half maxima (FWHMs) were determined from the split pseudo-Voigt function fitting.

^bCrystallite sizes were estimated by the Scherrer equation ($K = 1$) using the integral breadths.

Table S5. Photocatalytic O₂ evolution rate over Sr_xPb_{1-x}BiO₂Cl ($x = 0, 0.2$) loaded with cocatalysts.

Photocatalyst	Cocatalyst ^a	O ₂ evolution rate (μmol/h)
PbBiO ₂ Cl	none	12.8
PbBiO ₂ Cl	CoO _x	3.9
PbBiO ₂ Cl	IrO _x	4.2
PbBiO ₂ Cl	RuO _x	9.9
Sr _{0.2} Pb _{0.8} BiO ₂ Cl	none	6.2
Sr _{0.2} Pb _{0.8} BiO ₂ Cl	RuO _x	5.7

^aCocatalysts were loaded on the photocatalysts by impregnation method using corresponding precursors (Co(NO₃)₂, Na₂IrCl₆, RhCl₃: 0.5 wt% as metal), followed by calcination in air at 673 K for 30 min.

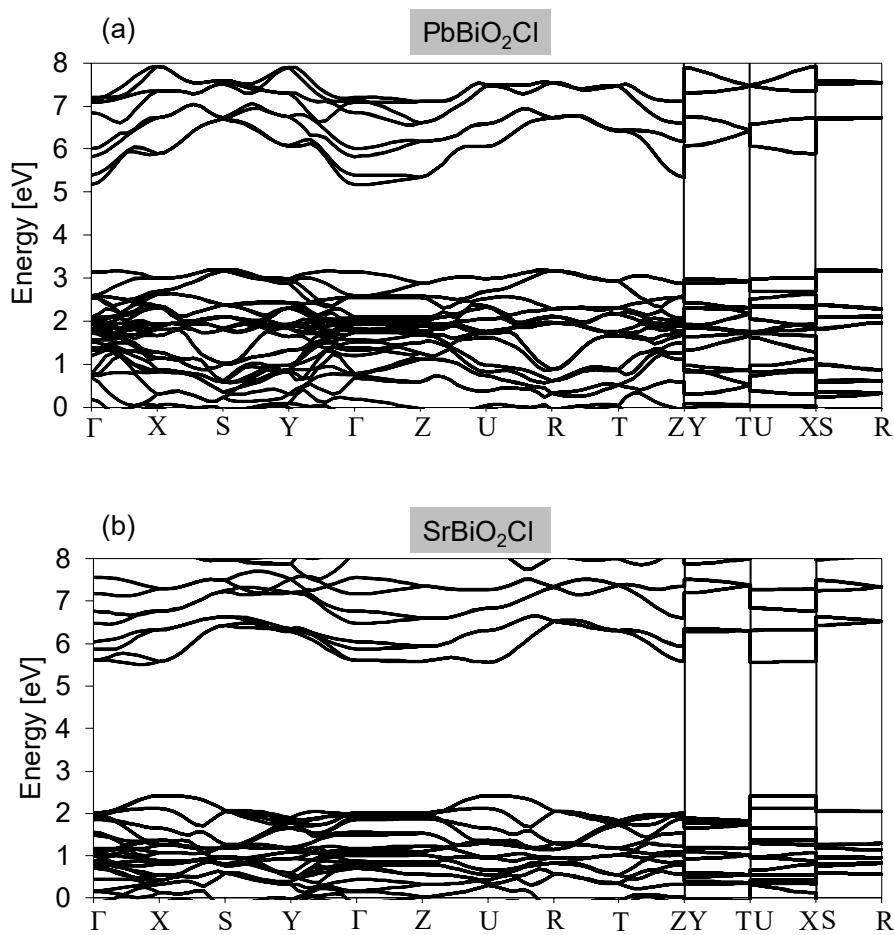


Figure S1. Band structure of (a) PbBiO₂Cl and (b) SrBiO₂Cl.

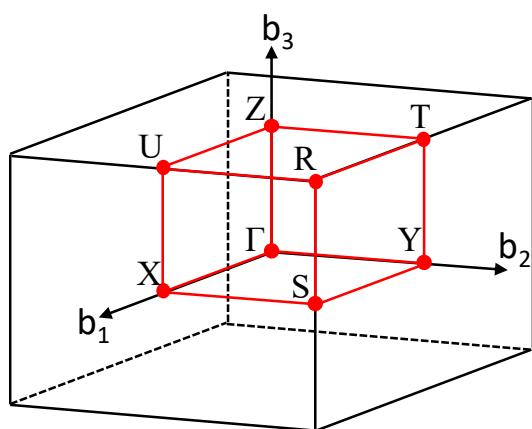


Figure S2. First Brillouin zone of orthorhombic lattice.

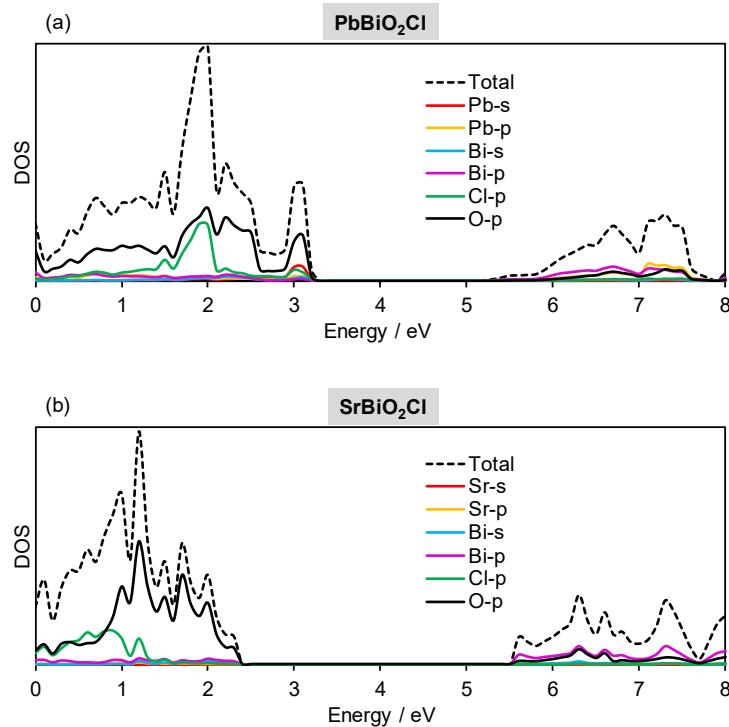


Figure S3. Full range of DOS of (a) PbBiO_2Cl and (b) SrBiO_2Cl .

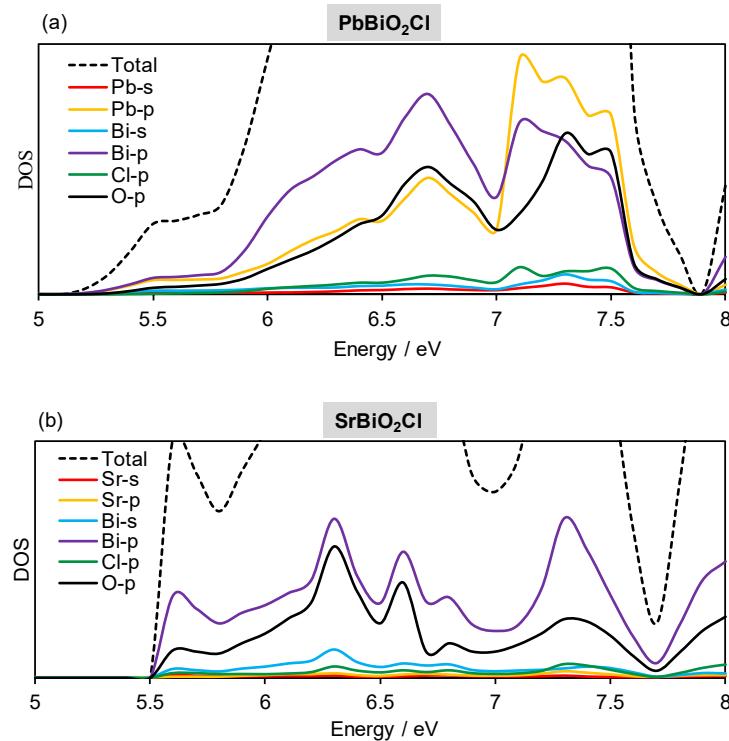


Figure S4. Magnified DOS around conduction bands of (a) PbBiO_2Cl and (b) SrBiO_2Cl .

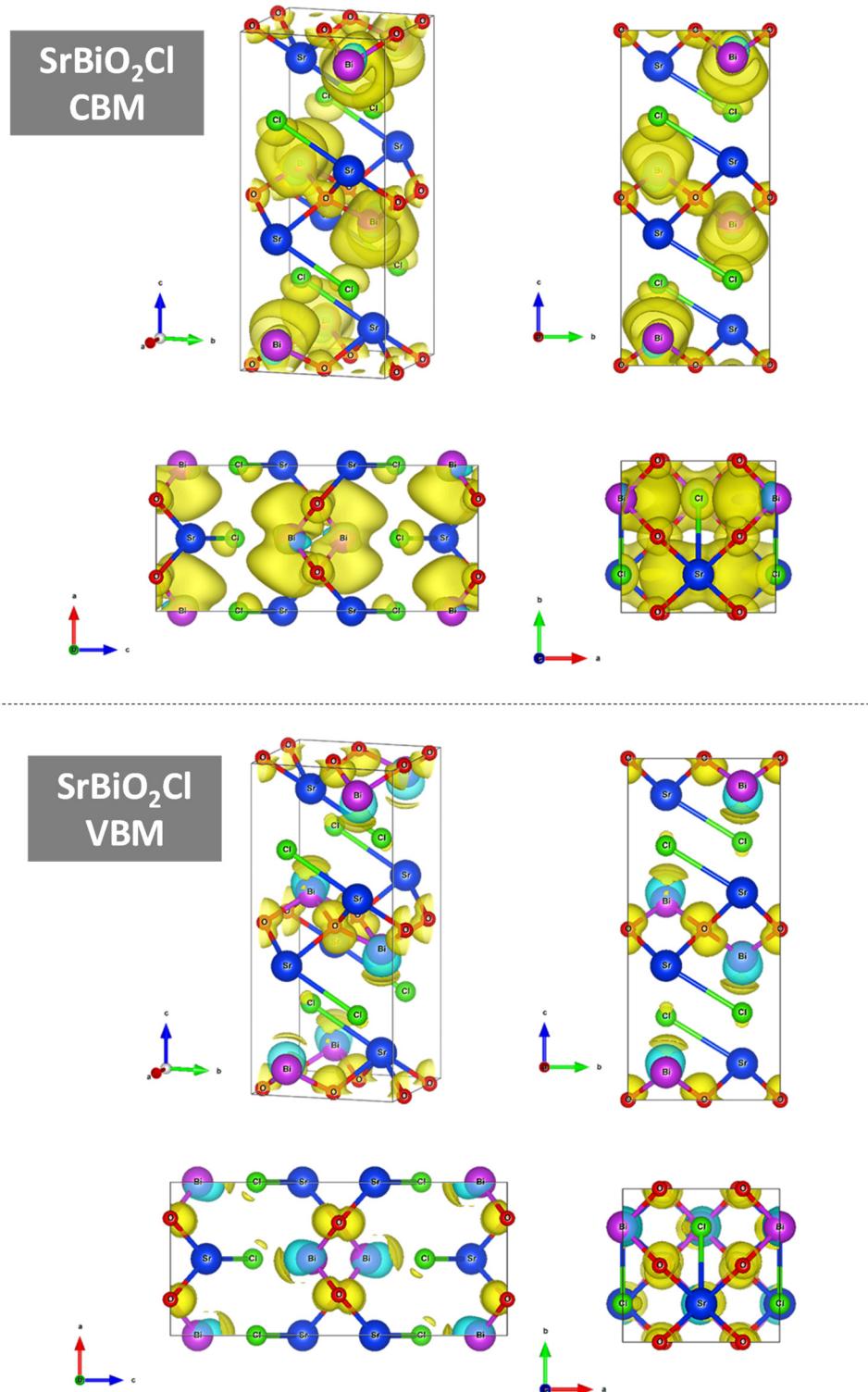


Figure S5. Partial charge densities of the CBM and VBM for SrBiO₂Cl. Blue, purple, red, and green spheres represent Sr, Bi, O, and Cl atoms, respectively.

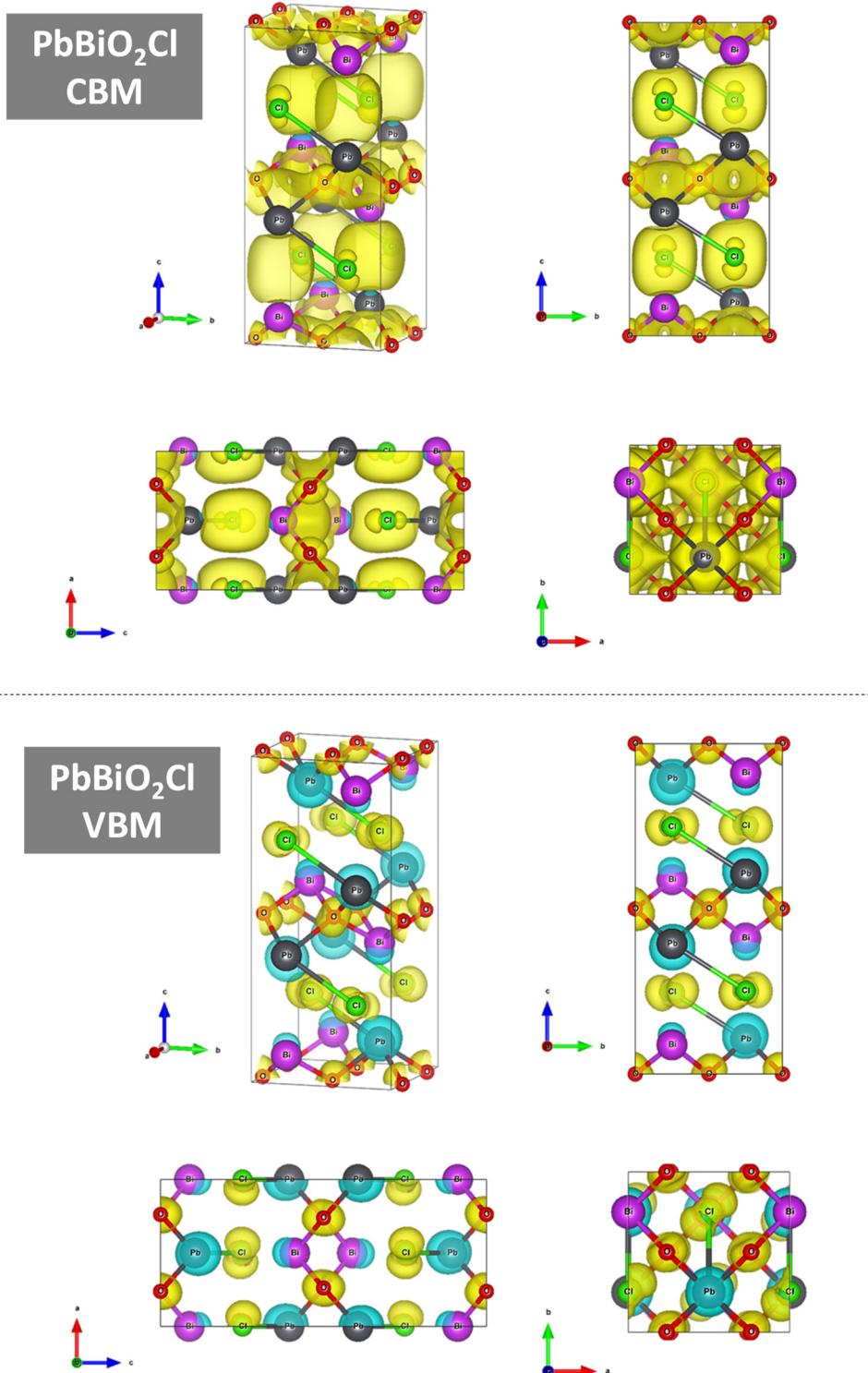


Figure S6. Partial charge densities of the CBM and VBM for PbBiO₂Cl. Gray, purple, red, and green spheres represent Pb, Bi, O, and Cl atoms, respectively.

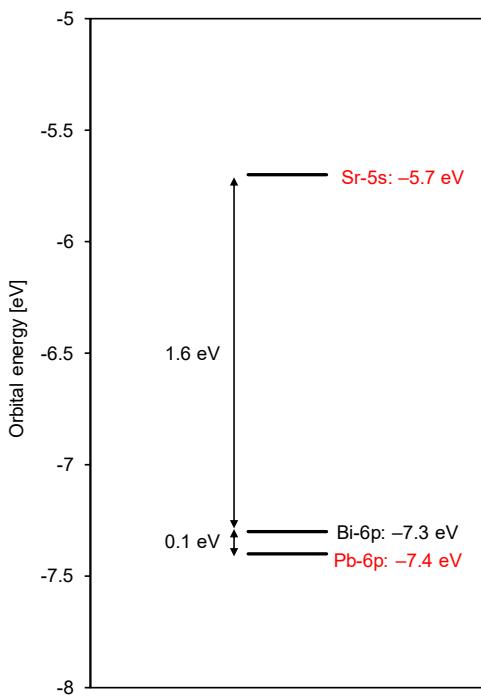


Figure S7. Orbital energies of Sr-5s, Pb-6p, and Bi-6p. The orbital energies were estimated from the first ionization potentials according to the Koopmans' theorem,^{S13} because DFT calculations of these orbital energies were difficult due to the varieties of electron configuration and the electron correlations in the 6p orbitals.

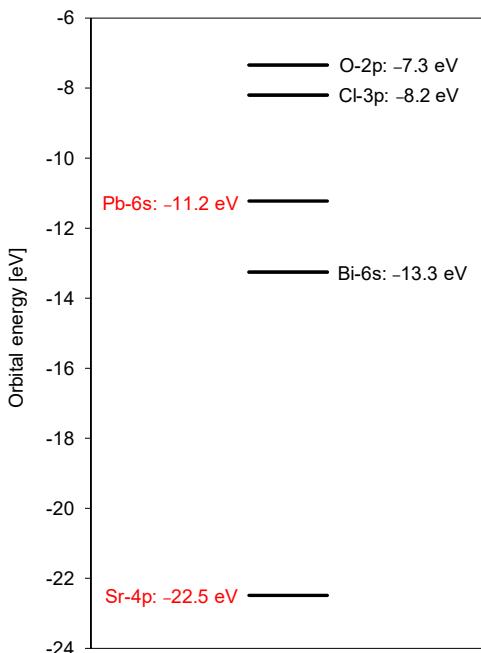


Figure S8. Orbital energies of O-2p, Cl-3p, Pb-6s, Bi-6s, and Sr-4p.

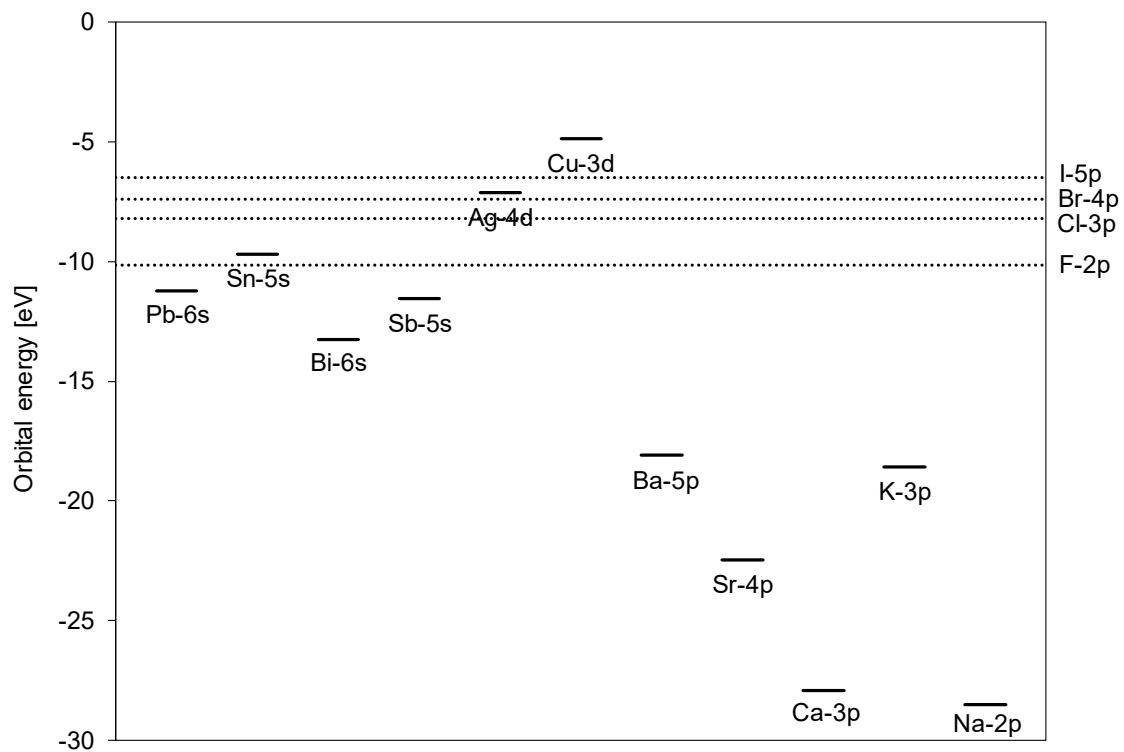


Figure S9. Various orbital energies (Pb-6s, Sn-5s, Bi-6s, Sb-5s, Ag-4d, Cu-3d, Ba-5p, Sr-4p, Ca-3p, K-3p, Na-2p). Note that the energies of d orbitals from DFT calculation generally include some imprecision due to the strong electron correlation.

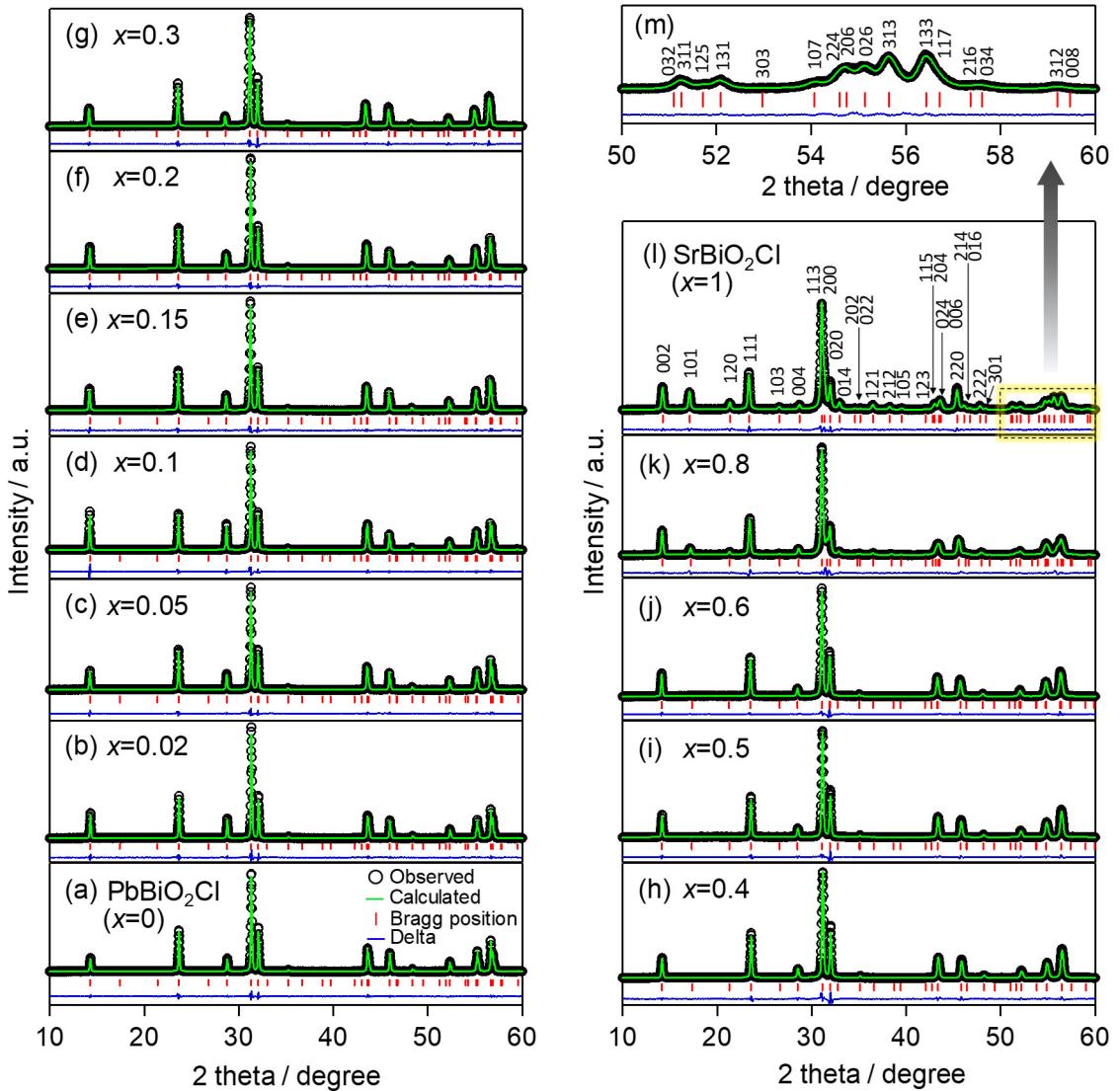


Figure S10. Le Bail refinements of XRD patterns of $\text{Sr}_x\text{Pb}_{1-x}\text{BiO}_2\text{Cl}$ solid solutions using JANA 2006.^{S14}

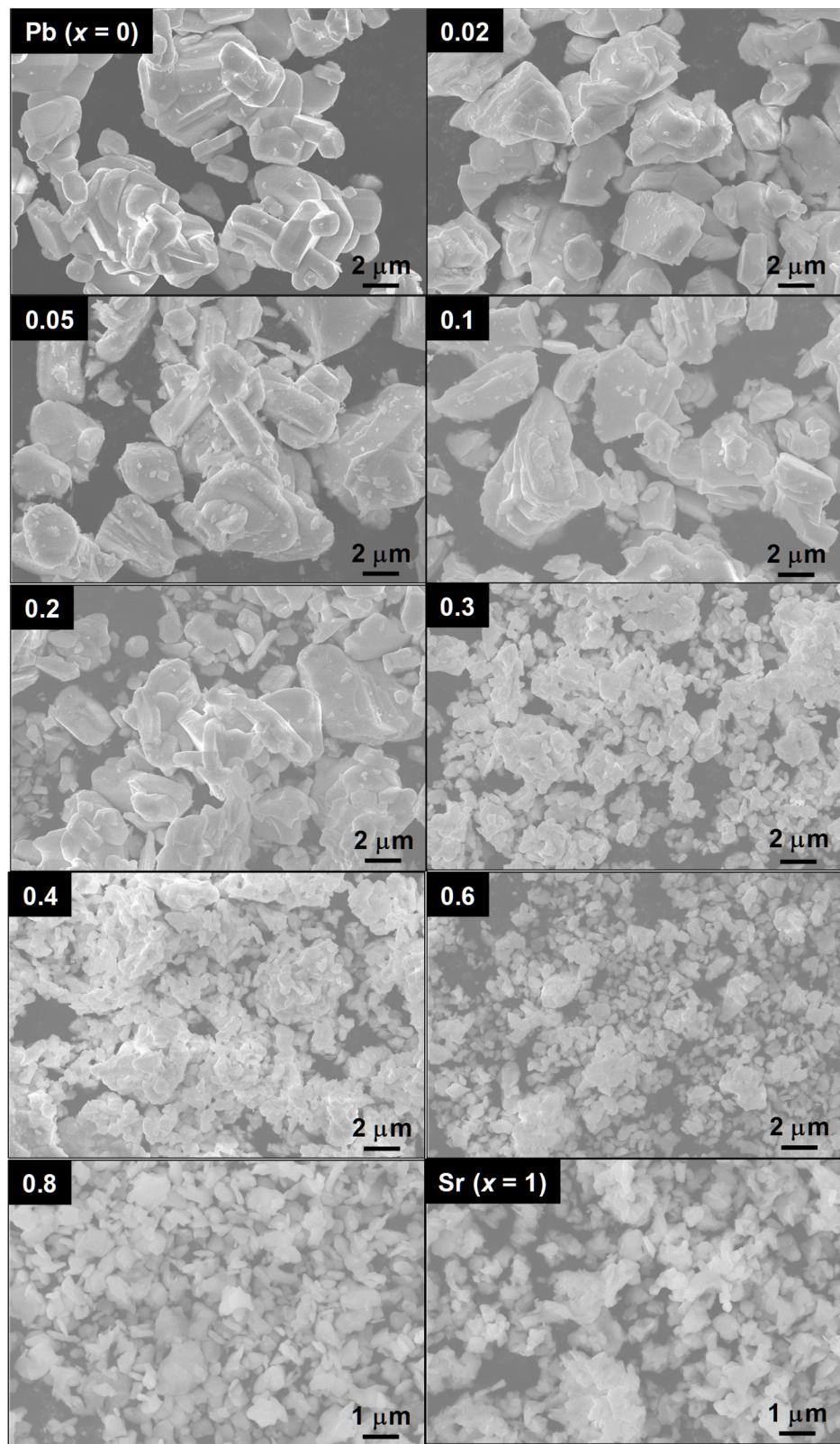


Figure S11. Enlarged SEM images of $\text{Sr}_x\text{Pb}_{1-x}\text{BiO}_2\text{Cl}$ solid solutions ($x = 0\text{--}1$).

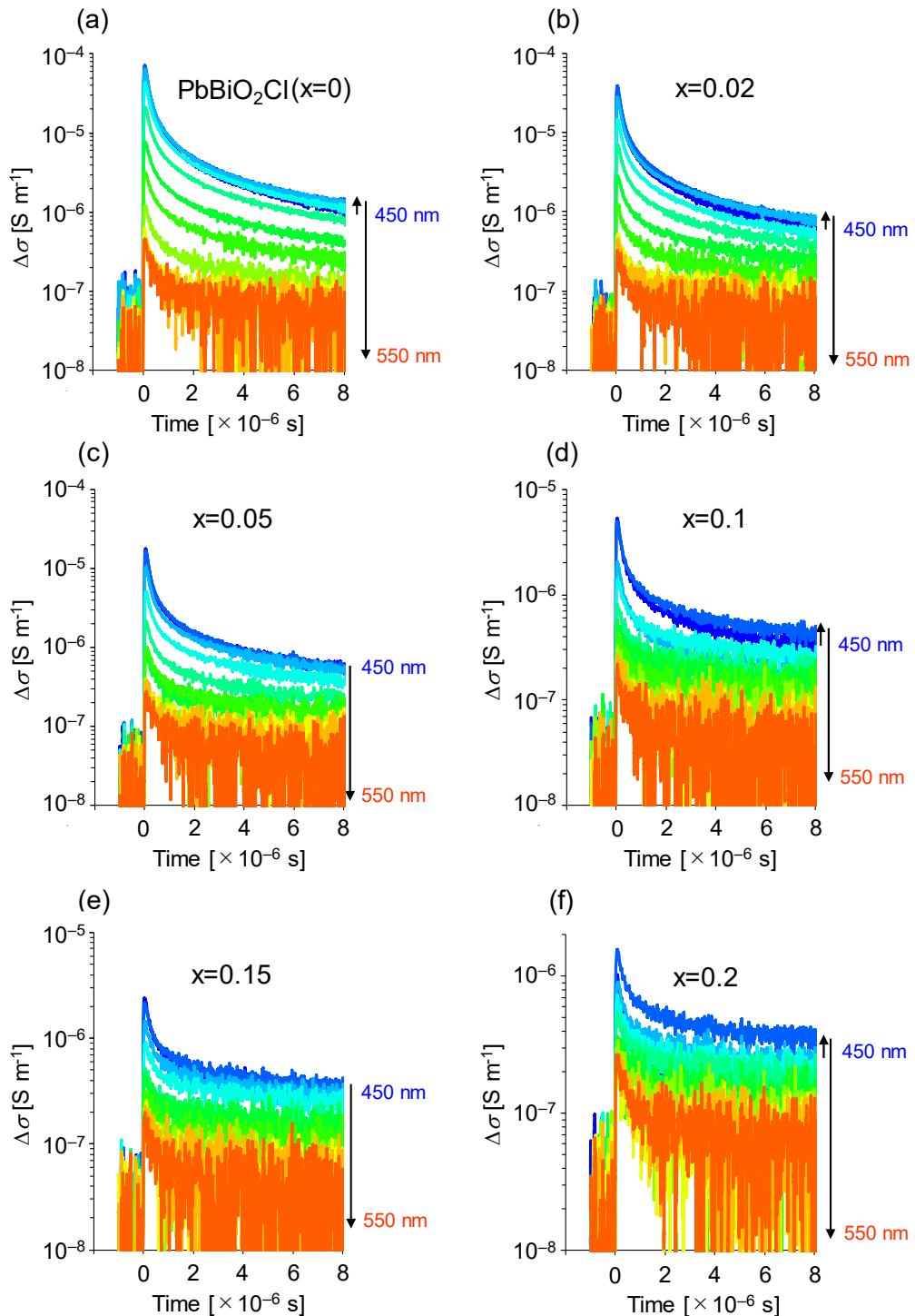


Figure S12. Photoconductivity transients: $\Delta\sigma(\lambda_{ex}=450-550 \text{ nm}, I_0=5.0\times 10^{15} \text{ photons cm}^{-2} \text{ per pulse}^{-1})$ of $\text{Sr}_x\text{Pb}_{1-x}\text{BiO}_2\text{Cl}$ solid solutions ($x=0-0.2$).

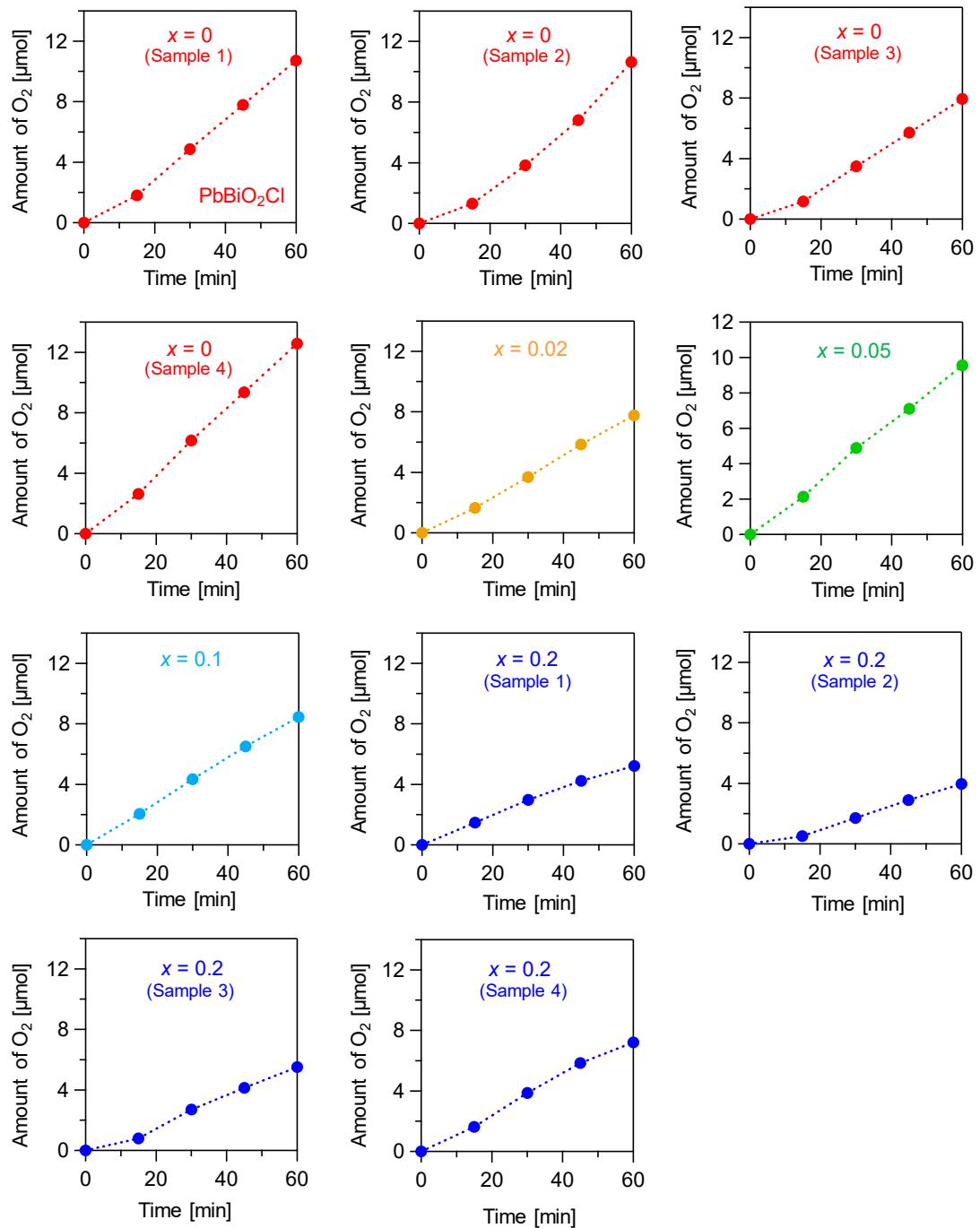


Figure S13. O_2 evolution over $\text{Sr}_x\text{Pb}_{1-x}\text{BiO}_2\text{Cl}$ solid solutions ($x = 0\text{--}0.2$) in the presence of AgNO_3 under UV light ($\lambda = 300\text{--}400\text{ nm}$)

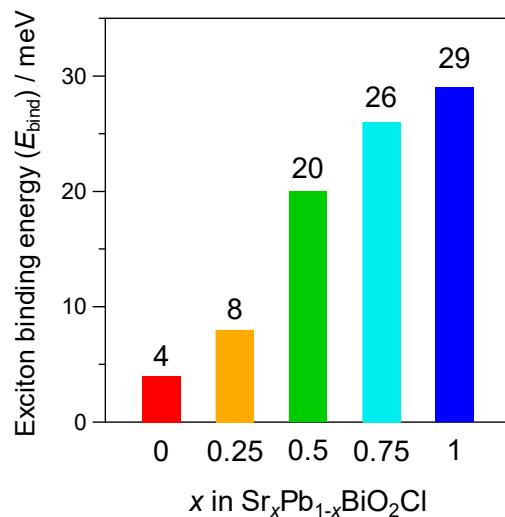


Figure S14. Calculated exciton binding energies of $\text{Sr}_x\text{Pb}_{1-x}\text{BiO}_2\text{Cl}$.

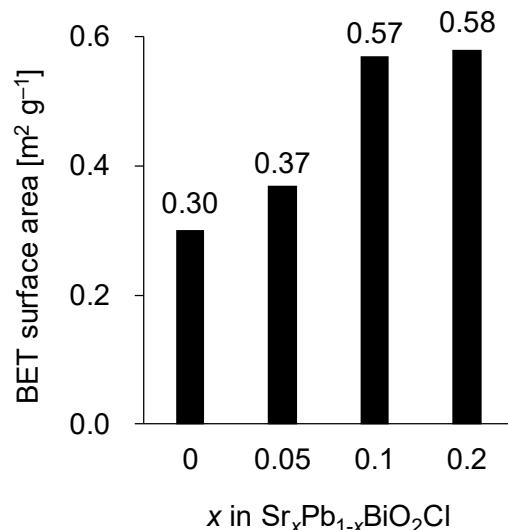


Figure S15. Specific surface area of $\text{Sr}_x\text{Pb}_{1-x}\text{BiO}_2\text{Cl}$ solid solutions ($x = 0\text{--}0.2$)