# Supporting Information on "Revealing Transient Shuttling Mechanism of Catalytic Ion Transport through Liquid-Liquid Interface" 

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The Supporting Information describes the technical details of molecular dynamics (MD) calculations and associated results of calculations.

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## S1 MD Conditions

The present MD simulation investigated the transport of $\mathrm{F}^{-}$through water-dichloromethane (DCM) interface. The ligand to support ion transport is either tetrahexylammonium $\left(\mathrm{N}\left(\mathrm{C}_{6} \mathrm{H}_{13}\right)_{4}^{+}\right.$, $\left.\mathrm{THA}^{+}\right)$or tetrabutylammonium $\left(\mathrm{N}_{\left.\left(\mathrm{C}_{4} \mathrm{H}_{9}\right)_{4}^{+}, \mathrm{TBA}^{+}\right) \text {. The MD simulation was carried out }}^{\text {a }}\right.$ with our in-house code, namely FreeFlex.

## S1.1 Force fields

The force field parameters of constituent molecules/ions employed in the present MD simulation are summarized in Tables S1 and S2. Water is described with the POL3 model, ${ }^{1}$ while DCM with the one developed by Dang et $\mathrm{al.}^{2} \mathrm{~F}^{-}$is treated with the one by Dang et al. ${ }^{3}$ These models have rigid intramolecular geometry and polarizability parameters $\alpha$ at their sites, as the polarizable models are preferred to reproduce the transfer free energies of the ions. ${ }^{4}$ We note that the original paper of the DCM model ${ }^{2}$ includes some errors in parameters, ${ }^{5}$ and the corrected parameters are listed in Table S1.

Table S1: Force field parameters for water, DCM , and $\mathrm{F}^{-}$.

| (a) sites |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| molecule | site | $q(\mathrm{e})$ | $\alpha\left(\AA^{3}\right)$ | $\sigma(\AA)$ | $\varepsilon(\mathrm{kcal} / \mathrm{mol})$ |
| water | H | 0.3650 | 0.170 | 0.000 | 0.000 |
|  | O | -0.7300 | 0.528 | 3.204 | 0.156 |
| DCM | C | -0.2720 | 0.878 | 3.410 | 0.137 |
|  | H | $0.1897^{*}$ | 0.135 | 2.400 | 0.040 |
|  | Cl | $-0.0537^{*}$ | 1.910 | 3.450 | 0.280 |
| $\mathrm{~F}^{-}$ | F | -1.0000 | 1.050 | 3.3587 | 0.100 |

(b) bonds

| molecule | bond | length $(\AA)$ |
| :---: | :---: | :--- |
| water | $\mathrm{H}-\mathrm{O}$ | 1.0 |
|  | $\mathrm{H}-\mathrm{H}$ | 1.63328 |
| DCM | $\mathrm{C}-\mathrm{H}$ | 1.070 |
|  | $\mathrm{C}-\mathrm{Cl}$ | 1.772 |
|  | $\mathrm{H}-\mathrm{Cl}$ | 2.33057 |
|  | $\mathrm{Cl}-\mathrm{Cl}$ | 2.92420 |

* corrected from Ref. [ $\left.{ }^{2}\right] .{ }^{5}$

The force fields of $\mathrm{THA}^{+}$and $\mathrm{TBA}^{+}$were described on the basis of the united atom model of AMBER ff03ua. ${ }^{6}$ The potential functions of internal stretching, bending, and torsional vibrations are given in the following forms, ${ }^{7,8}$

$$
\begin{align*}
V_{\text {bonds }}= & \sum_{i}^{\text {bonds }} k_{r}^{(i)}\left(r^{(i)}-r_{0}^{(i)}\right)^{2},  \tag{S1}\\
V_{\text {angles }}= & \sum_{i}^{\text {angles }} k_{\theta}^{(i)}\left(\theta^{(i)}-\theta_{0}^{(i)}\right)^{2},  \tag{S2}\\
V_{\text {dihederals }}= & \sum_{i}^{\text {dihedrals }}\left[V_{1}^{(i)}\left\{1+\cos \left(\phi^{(i)}-\gamma_{1}^{(i)}\right)\right\}+V_{2}^{(i)}\left\{1+\cos \left(-2 \phi^{(i)}-\gamma_{2}^{(i)}\right)\right\}\right. \\
& \left.+V_{3}\left\{1+\cos \left(-3 \phi^{(i)}-\gamma_{3}^{(i)}\right)\right\}+\frac{1}{2} V_{\mathrm{LJ}}\right],  \tag{S3}\\
V_{\mathrm{LJ}}= & 4 \varepsilon\left[\left(\frac{\sigma}{r}\right)^{12}-\left(\frac{\sigma}{r}\right)^{6}\right] \tag{S4}
\end{align*}
$$

Note that the dihedral potential in Eq. (S3) includes half the nonbonding 1-4 interaction. The models of THA ${ }^{+}$and $\mathrm{TBA}^{+}$include internal flexibility to take account of conformations
of alkyl chains. The force field parameters in Eqs. (S1)-(S4) for $\mathrm{THA}^{+}$and $\mathrm{TBA}^{+}$are summarized in Table S2, with the site labels shown in Figure S1. The parameters for dihedral angles were slightly modified so as to facilitate conformational change of alkyl chains during the equilibration and sampling.

Table S2: Force field parameters for $\mathrm{THA}^{+}$and $\mathrm{TBA}^{+}$.

| (a) sites |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| site | $q(\mathrm{e})$ | $\alpha\left(\AA^{3}\right)$ | $\sigma(\AA)$ | $\varepsilon(\mathrm{kcal} / \mathrm{mol})$ |
| N | 0.0 | 0.0 | 3.250 | 0.170 |
| $\mathrm{C} 2(\mathrm{a})$ | 0.25 | 0.0 | 3.905 | 0.118 |
| $\mathrm{C} 2(\mathrm{~b})$ | 0.0 | 0.0 | 3.905 | 0.118 |
| C 3 | 0.0 | 0.0 | 3.905 | 0.175 |

(b) bonds

| bond | $k_{r}\left(\mathrm{kcal} / \mathrm{mol} \cdot \AA^{2}\right)$ | $r_{0}(\AA)$ |
| :---: | :---: | :---: |
| N-C2 | 367.0 | 1.471 |
| C2-C2 | 310.0 | 1.526 |
| C2-C3 | 310.0 | 1.526 |

(c) angles

| bond | $k_{\theta}\left(\mathrm{kcal} / \mathrm{mol} \cdot\right.$ degree $\left.^{2}\right)$ | $\theta_{0}($ degree $)$ |
| :---: | :---: | :---: |
| C2-N-C2 | 50.0 | 109.50 |
| N-C2-C2 | 80.0 | 111.20 |
| C2-C2-C2 | 40.0 | 109.50 |
| C2-C2-C3 | 40.0 | 109.50 |

(d) dihedral angles

| bond | $V_{n}\left(\mathrm{kcal} / \mathrm{mol} \cdot\right.$ degree $\left.^{2}\right)$ | $\gamma_{n}$ (degree) |
| :---: | :---: | ---: |
| N-C2-C2-C2 | 1.00 | 180.0 |
|  | 0.24 | 180.0 |
| C2-C2-C2-C2 | 1.12 | 0.0 |
|  | 1.00 | 180.0 |
| C2-C2-C2-C3 | 0.24 | 180.0 |
|  | 1.12 | 0.0 |
|  | 1.00 | 180.0 |
|  | 0.24 | 180.0 |
|  | 1.12 | 0.0 |



Figure S1: Schematic of $\mathrm{TBA}^{+}$(left) and $\mathrm{THA}^{+}$(right) molecules with the site labels.

## S1.2 MD cells

The present work adopted four different dimensions of MD cells (A)-(D) for different purposes. The cell (A) was mainly used for the free energy calculations of the water-DCM system, and is illustrated in Figure S2. The dimensions of the cell (A) are $L_{x} \times L_{y} \times L_{z}=$ $50 \AA \times 50 \AA \times 115 \AA$ with the 3 -dimensional periodic boundary conditions. The cell contains one anion $\left(\mathrm{F}^{-}\right)$, one counter ion ( $\mathrm{THA}^{+}$or $\mathrm{TBA}^{+}$), 2091 water, and 2116 DCM molecules. The water and DCM phases form alternating slabs with interfaces normal to the $z$ axis. The thicknesses of water and DCM phases are about $25 \AA$ and $90 \AA$, respectively, along the $z$ axis. We also imposed electric field $E_{z}=0.0,0.1,0.2 \mathrm{~V} / \mathrm{nm}$ along the $z$ axis to mimic experimental electrochemical conditions. Accordingly, a site of partial charge $q$ feels extra force $-q E_{z}$ from the field during the MD simulation.

The other three smaller cells (B)-(D) were employed for auxiliary MD calculations. (B) The transfer of single anion $\left(\mathrm{F}^{-}\right)$or cation $\left(\mathrm{THA}^{+}\right.$or $\mathrm{TBA}^{+}$) was treated using an MD cell of $L_{x} \times L_{y} \times L_{z}=25 \AA \times 25 \AA \times 85 \AA$ with the 3 -dimensional periodic boundary conditions. The cell contains one ion (either anion or cation), 523 water and 353 DCM molecules, and the water and DCM form alternating slabs with thicknesses of $25 \AA$ and 60 $\AA$, respectively. (C) Solvation structures of water around the ions were investigated in an


Figure S2: Geometry of MD cell (A) for $G^{(2)}(z, r)$ calculations.

MD cell of $L_{x} \times L_{y} \times L_{z}=25 \AA \times 25 \AA \times 25 \AA$ with the 3 -dimensional periodic boundary conditions. The cell contains one ion and 523 water molecules. (D) Dissociation between ion and counter ion was investigated in an MD cell of $L_{x} \times L_{y} \times L_{z}=25 \AA \times 25 \AA \times 50 \AA$ with the 3-dimensional periodic boundary conditions. The cell contains one anion, one cation $\left(\mathrm{THA}^{+}\right.$or $\left.\mathrm{TBA}^{+}\right)$and 294 DCM molecules.

In all cases of cells (A)-(D), the long-range electrostatic interactions were treated with the Particle-Mesh Ewald (PME) method. ${ }^{9}$ The Ewald separation parameter $\kappa$ is set to 0.323 $\AA^{-1}$. The dipolar interaction in the PME was treated by the smooth PME (SPME) method of Toukmaji et al. ${ }^{10}$ The 6-th order Cardinal B-splines were employed for the interpolation with grid spacing about $0.7 \AA$.

## S1.3 Coordinates for free energy surfaces

The two-dimensional free energy surface $G^{(2)}(z, r)$ associated to the ion transfer with complex formation is represented by two coordinates, $z$ and $r . z$ is the normal coordinate of the
anion $\left(\mathrm{F}^{-}\right)$from the liquid-liquid interface, where $z=0$ is set at the Gibbs dividing surface of water, and $z<0(z>0)$ indicates the anion in the water (oil) phase. We defined the $z$ coordinate with respect to the Gibbs dividing surface rather than the intrinsic surface, ${ }^{11}$ and the structural fluctuation of interface associated to the ion transfer was accounted for with the water finger coordinate $w$ as discussed below. The second coordinate $r$ denotes the distance between anion and ligand $\left(\mathrm{THA}^{+} / \mathrm{TBA}^{+}\right)$. In the present work, $r$ is defined with the distance between the anion $\left(\mathrm{F}^{-}\right)$and the central nitrogen $(\mathrm{N})$ site of $\mathrm{THA}^{+} / \mathrm{TBA}^{+}$.

The two-dimensional surface $G^{(2)}(z, r)$ was obtained by replica exchange umbrella sampling (REUS). ${ }^{12}$ In the $(z, r)$ surface, bias potentials of the following form were employed,

$$
\begin{equation*}
U^{\mathrm{bias}}\left(z, r ; z_{0}, \sigma_{z}, r_{0}, \sigma_{r}\right)=\frac{k_{B} T}{2}\left\{\frac{\left(z-z_{0}\right)^{2}}{\sigma_{z}^{2}}+\frac{\left(r-r_{0}\right)}{\sigma_{r}^{2}}\right\} \tag{S5}
\end{equation*}
$$

where $\left(z_{0}, r_{0}\right)$ is the center of the umbrella potential, and $\sigma_{z}$ and $\sigma_{r}$ denote the widths along the $z$ and $r$ directions, respectively. We prepared 480 sets of umbrella potentials with different $\left(z_{0}, r_{0}\right)$ values as shown in Table S3, and performed parallel MD simulations with different bias potentials. In the stage of equilibration, we set $\sigma_{z}=0.5 \AA$ and $\sigma_{r}=0.25 \AA$, and then in the sampling stage $\sigma_{z}=1.0 \AA$ and $\sigma_{r}=0.5 \AA$. During the sampling stage, the exchange of umbrella potentials was carried out by the Metropolis criteria. The exchange of umbrella potential was tried every 1000 MD steps among a pair of potentials that differ by one column and/or row in Table S3. The set of trajectories were analyzed by using the Weighted Histogram Analysis Method (WHAM) ${ }^{13}$ to derive the free energy surface.

We also calculated the one-dimensional free energy $G^{(1)}(z)$ for a single anion or cation through the liquid-liquid interface. The $z$ coordinate of the cation is defined with the position of the nitrogen (N) site. The MD calculation of $G^{(1)}(z)$ surface may suffer from the hysteresis problem associated to water finger. ${ }^{4}$ The problem arises from the fact that both connected and disconnected structures of water finger at a certain $z$ are hard to be properly sampled due to rare structural transition of water finger during MD simulation. To overcome this sampling
problem, we first calculated two-dimensional free energy surface $G^{(2)}(z, w)$ as a function of $z$ and the water finger coordinate $w^{4,14}$ and then integrated over the $w$ coordinate to obtain $G^{(1)}(z)$ by

$$
\begin{equation*}
G^{(1)}(z)=-k_{B} T \ln \int d w \exp \left(-\frac{G^{(2)}(z, w)}{k_{B} T}\right) \tag{S6}
\end{equation*}
$$

The calculation of two-dimensional free energy $G^{(2)}(z, w)$ ensures proper sampling of both connected and disconnected water finger structures. The $G^{(2)}(z, w)$ was also calculated with the REUS method after our previous work. ${ }^{4,14}$ The umbrella potentials are either twodimensional,

$$
\begin{equation*}
U^{\mathrm{bias}, 2 \mathrm{D}}\left(z, w ; z_{0}, \sigma_{z}, w_{0}, \sigma_{w}\right)=\frac{k_{B} T}{2}\left\{\frac{\left(z-z_{0}\right)^{2}}{\sigma_{z}^{2}}+\frac{\left(w-w_{0}\right)}{\sigma_{w}^{2}}\right\} \tag{S7}
\end{equation*}
$$

or one-dimensional,

$$
\begin{equation*}
U^{\text {bias,1D }}\left(z ; z_{0}, \sigma_{z}\right)=\frac{k_{B} T}{2} \frac{\left(z-z_{0}\right)^{2}}{\sigma_{z}^{2}} \tag{S8}
\end{equation*}
$$

Table S 4 shows the parameters $z_{0}$ and $w_{0}$ in Eqs. (S7) and (S8). In these potentials, $\sigma_{z}$ and $\sigma_{w}$ were set to $0.25 \AA$ for the equilibration, and $\sigma_{z}=\sigma_{w}=0.5 \AA$ for the sampling. The scheme of the replica exchange is same as that in our previous work. ${ }^{4,14}$

The one-dimensional free energy $G^{(1)}(r)$ as a function of the cation-anion distance $r$ in the DCM phase was evaluated to discuss the association and dissociation of the ion pair. The calculation was performed with the REUS method with different umbrella potentials defined in the $r$ coordinate. The umbrella potentials for the purpose are in the following form,

$$
\begin{equation*}
U^{\mathrm{bias}, 1 \mathrm{D}}\left(r ; r_{0}, \sigma_{r}\right)=\frac{k_{B} T}{2} \frac{\left(r-r_{0}\right)^{2}}{\sigma_{r}^{2}} \tag{S9}
\end{equation*}
$$

The parameters $r_{0}$ in Eq. (S9) are summarized in Table S5. $\sigma_{r}$ was determined in the same manner as in Eq. (S5).
Table S3：Table of umbrella potentials with different $\left(z_{0}, r_{0}\right)$ values in Eq．（S5）．A total of 480 different potentials are numbered
from 1 to 480 ．The colored cells illustrate the pair of replica exchange；the counterparts of a red cell are colored in yellow．

|  |  |  |
| :---: | :---: | :---: |
|  | 蒜䓍等 <br>  <br>  <br>  <br>  <br>  <br>  <br>  N <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  |  |
|  |  | ？ |

Table S4：Table of 160 umbrella potentials with different $\left(z_{0}, w_{0}\right)$ values in Eq．（S7）or $z_{0}$ values in Eq．（S8）．The umbrella potentials numbered $1 \sim 24$ labelled with $w_{0}=$ free indicate the one－dimensional potential of Eq．（S8），while $25 \sim 160$ indicate the two－dimensional potential of Eq．（S7）．The colored cells illustrate the pair of replica exchange；the counterparts of a red cell are colored in yellow．

| §近 |  |
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|  |  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br> R荗孚～ <br> 呙躱合 <br> 子： <br> $\stackrel{\text { ® }}{\sim}$ |
|  |  |

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\]

## S1.4 MD procedures

We describe the procedures to prepare initial configurations, equilibration, and sampling of MD simulation. In either case MD calculations were performed with $N V T$ ensemble with the temperature $T$ set to 300 K by using Nosé-Hoover thermostat. ${ }^{15,16}$ The time development was carried out with the velocity Verlet algorithm with a time step of 1 fs , with the RATTLE constraint algorithm. ${ }^{17-19}$

## S1.4.1 $G^{(2)}(z, r)$ for ion pair

The calculations of $G^{(2)}(z, r)$ including an anion $\left(\mathrm{F}^{-}\right)$and a counter ion $\left(\mathrm{THA}^{+} / \mathrm{TBA}^{+}\right)$ were carried out with the large MD cell (A) (Figure S2) in Sec. S1.2. Initial configurations of MD simulation were prepared by randomly putting 2091 water molecules in the region of $-25 \AA<z<0 \AA$ of the MD cell and 2116 DCM molecules in $0 \AA<z<90 \AA$. We also initially put one anion $\left(\mathrm{F}^{-}\right)$at $(x, y, z)=(0 \AA, 0 \AA,-5 \AA)$ and the N site of $\mathrm{THA}^{+}$or $\mathrm{TBA}^{+}$ at $(x, y, z)=(0 \AA, 0 \AA, 15 \AA)$. Then the steepest descent relaxation was adopted to remove unphysical molecular overlap, and subsequently MD equilibration was carried out for 100 ps .

Then we carried out parallel simulation using parallel computers of 480 nodes. We impose 480 different bias potential functions of Table S3 on these respective replicas, and further equilibrate these replicas with different bias potentials for 100 ps independently in parallel. During the equilibration, the electric field $E_{z}$ along the $z$ axis is incremented every 10 ps by $1 / 10$ of the target value $E_{z}(=0 \sim 0.2 \mathrm{~V} / \mathrm{nm})$. After the parallel equilibration is finished as such, the production run was carried out for 200 ps with the replica exchange umbrella sampling (REUS). The resultant set of MD trajectories were treated with the weighted histogram analysis method (WHAM) to calculate $G^{(2)}(z, r)$. The derivation of the free energy $G^{(2)}(z, r)$ from the probability distributions takes account of the volume element of the $z$ and $r$ coordinates.

## S1.4.2 Radial distribution functions

Next, radial distribution functions (RDFs) between the solute ions and water molecules in bulk water were calculated to estimate the contact distances of the solute and water molecules. They are needed for applying the water finger coordinate $w$ to the present systems in Sec. S1.4.3 to judge the connectivity based on the water-water and solute-water distances. ${ }^{4}$ We initially put one $\mathrm{F}^{-}$, $\mathrm{THA}^{+}$or $\mathrm{TBA}^{+}$ion and 523 water molecules randomly in the MD cell (C) in Sec. S1.2. The steepest descent relaxation was adopted to remove unphysical molecular overlap, and subsequently MD equilibration was carried out for 100 ps . Then the sampling calculations of RDFs were performed for 300 ps for each solute ion.

## S1.4.3 Free energy profile for single ion

The free energy profile $G^{(1)}(z)$ of a single anion $\left(\mathrm{F}^{-}\right)$or cation $\left(\mathrm{THA}^{+} / \mathrm{TBA}^{+}\right)$over the waterDCM interface was obtained. Since $G^{(1)}(z)$ is derived from $G^{(2)}(z, w)$ by Eq. (S6), $G^{(2)}(z, w)$ for the single anion or cation was calculated using the MD cell (B) in Sec. S1.2. We randomly put 523 water molecules in $-25 \AA<z<0 \AA, 353$ DCM molecules in $0 \AA<z<60 \AA$, and one ion at $(x, y, z)=(0 \AA, 0 \AA, 5 \AA)$. (The position of $\mathrm{THA}^{+} / \mathrm{TBA}^{+}$means that of the N site.) The steepest descent relaxation and subsequent MD equilibration for 100 ps were carried out in the same manner as in Sec. S1.4.1. Then we prepared a total of 160 replicas with different umbrella potentials of Eqs. (S7) or (S8), which are summarized in Table S4. These replicas were equilibrated in parallel for 100 ps using parallel computers of 160 nodes, each of which has different umbrella potential, with gradually imposing the electric field $E_{z}$ from $E_{z}=0$ to the target value. After the equilibration was completed, the REUS calculations were performed for 200 ps for each node in the same manner as in our previous works, ${ }^{4,14}$ and the results were analyzed by WHAM to obtain $G^{(2)}(z, w)$. The calculated $G^{(2)}(z, w)$ was reduced to $G^{(1)}(z)$ by Eq. (S6).

## S1.4.4 Dissociation of ion pair in oil phase

The free energy profile of $G^{(1)}(r)$ as a function of the distance $r$ between anion $\left(\mathrm{F}^{-}\right)$and cation ( $\mathrm{THA}^{+} / \mathrm{TBA}^{+}$) in the bulk DCM phase was calculated using the REUS sampling along the $r$ coordinate. We initially put one $\mathrm{F}^{-}$anion at $(x, y, z)=(0 \AA, 0 \AA, 15 \AA)$, the N site of $\mathrm{THA}^{+}$or $\mathrm{TBA}^{+}$at $(x, y, z)=(0 \AA, 0 \AA, 5 \AA)$, and $294 \mathrm{DCM}^{2}$ molecules randomly in the cell (B) in Sec. S1.2, and the steepest descent relaxation was adopted. Then we prepared 20 umbrella potentials of Eq. (S9) in Table S5. The MD equilibrations with 20 different potentials were carried out for 100 ps independently using parallel computers of 20 nodes. During the equilibration the electric field $E_{z}$ is gradually imposed from $E_{z}=0$ to the target value. The REUS calculations were performed for 1 ns , and the results were analyzed by WHAM to obtain $G^{(1)}(r)$. The derivation of $G^{(1)}(r)$ from the probability distributions takes account of the volume element of the $r$ coordinate.

## S2 Supporting Results

## S2.1 $G^{(2)}(z, r)$ for $\mathbf{F}^{-}$- $^{-}{ }^{+}{ }^{+} /$TBA $^{+}$

Here we display the whole calculated free energy surfaces $G^{(2)}(z, r)$ for the $\mathrm{F}^{-}-\mathrm{THA}^{+} / \mathrm{TBA}^{+}$ at $E_{z}=0.0,0.1,0.2 \mathrm{~V} / \mathrm{nm}$ in Figures S 3 and S 4 . Note that Figures S 3 (a) and (c) are same as Figure 2 (a) and (b) of the main text, and Figures S 4 (a) and (c) are same as Figure 3 (a) and (b) of the main text.

## S2.2 Transport of ion pair

We discuss the interfacial transport of ion pairs, $\mathrm{F}^{-}-\mathrm{THA}^{+}$and $\mathrm{F}^{-}-\mathrm{TBA}^{+}$. To estimate the free energy profiles for the ion pairs, we tentatively restrict the $(z, r)$ surface to $r<10$
(a)

(b)

(c)


Figure S3: Calculated $G^{(2)}(z, r)$ of $\mathrm{F}^{-}-\mathrm{THA}^{+}$at water/DCM interface with different values of electric field, (a) $E_{z}=0.0 \mathrm{~V} / \mathrm{nm}$, (b) $0.1 \mathrm{~V} / \mathrm{nm}$, (c) $0.2 \mathrm{~V} / \mathrm{nm}$. The contour lines are drawn with $2 \mathrm{kcal} / \mathrm{mol}$ interval. The panel (c) illustrates two exit paths (A) and (B) in yellow and red, respectively.
(a)

(b)

(c)


Figure S4: Calculated $G^{(2)}(z, r)$ of $\mathrm{F}^{-}-\mathrm{TBA}^{+}$at water/DCM interface with different values of electric field, (a) $E_{z}=0.0 \mathrm{~V} / \mathrm{nm}$, (b) $0.1 \mathrm{~V} / \mathrm{nm}$, (c) $0.2 \mathrm{~V} / \mathrm{nm}$. The contour lines are drawn with $2 \mathrm{kcal} / \mathrm{mol}$ interval. The panel (c) illustrates two exit paths (A) and (B) in yellow and red, respectively, and $\times$ denotes the transition state of $(B)$.
$\AA$, and reduced the $G^{(2)}(z, r)$ surface to the 1-D profile for the coordinate $z$ by

$$
\begin{equation*}
G^{(1), \mathrm{IP}}(z)=-k_{B} T \ln \int_{0 \AA}^{10 \AA} 4 \pi r^{2} d r \exp \left(-\frac{G^{(2)}(z, r)}{k_{B} T}\right) \tag{S10}
\end{equation*}
$$

We note that the result of $G^{(1), \mathrm{IP}}(z)$ is rather insensitive to the upper bound of the integral, $r=10 \AA$, since the integrated Boltzmann factor in Eq. (S10) is actually dominant in the region of stable ion pair state. The results of free energy profiles for the ion pairs are shown in Figure S5.


Figure S5: 1-D free energy surface $G^{(1), \mathrm{IP}}(z)$ for the ion pairs, $\mathrm{F}^{-}-\mathrm{THA}^{+}$(purple) and $\mathrm{F}^{-}-\mathrm{TBA}^{+}$(green), in Eq. (S10) under $E_{z}=0.2 \mathrm{~V} / \mathrm{nm}$.

The $G^{(1), \mathrm{IP}}(z)$ profiles show that the $\mathrm{F}^{-}-\mathrm{THA}^{+}$and $\mathrm{F}^{-}-\mathrm{TBA}^{+}$ion pairs have asymptotic free energies of about $2 \mathrm{kcal} / \mathrm{mol} 10 \mathrm{kcal} / \mathrm{mol}$, respectively, under the electric field $E_{z}$. The considerable difference in asymptotic free energy by $8 \mathrm{kcal} / \mathrm{mol}$ is attributed to the difference in hydrophobicity of $\mathrm{THA}^{+}$and $\mathrm{TBA}^{+}$. The difference will have a significant consequence to determine the transport mechanism, as we discuss later.

## S2.3 Radial distribution functions of THA ${ }^{+} / \mathrm{TBA}^{+}$

Before calculating the free energy profiles $G^{(1)}(z)$ for single ions in Sec. S2.4, we need to define the water finger coordinate $w$ for these ions, since $G^{(1)}(z)$ profiles are derived from the calculated results of $G^{(2)}(z, w)$ by Eq. (S6). The water finger coordinate $w$ is given on
the basis of a graph of instantaneous molecular configuration by regarding the ion and water molecules as vertices, and it corresponds to the threshold of edge distance to make the ion reachable to the bulk water. ${ }^{4,14}$ To compare the edge distances of water-water and water-ion properly, we need to take account of the difference in molecular size between water and ion. Therefore, we examine the water-ion contact distances in comparison with water-water. The calculated RDFs in bulk water are shown in Figure S6, which includes O-O (purple), F-O (green), $\mathrm{N}\left(\mathrm{THA}^{+}\right)-\mathrm{O}$ (light blue), and $\mathrm{N}\left(\mathrm{TBA}^{+}\right)-\mathrm{O}$ (yellow).

One notices that the $\mathrm{N}\left(\mathrm{THA}^{+}\right)-\mathrm{O}$ and $\mathrm{N}\left(\mathrm{TBA}^{+}\right)-\mathrm{O}$ RDFs do not show conspicuous first solvation peak, in contrast to the $\mathrm{O}-\mathrm{O}$ or $\mathrm{F}-\mathrm{O}$ RDFs. Therefore, the contact distance for $\mathrm{N}-\mathrm{O}$ was evaluated with the difference in the rise distances of $\mathrm{N}\left(\mathrm{THA}^{+} / \mathrm{TBA}^{+}\right)-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ (see the inset of Figure S6). Therefore, the offset value $\Delta R=-1.0 \AA$ was used for $\mathrm{N}-\mathrm{O}$ distances to calculate the water finger coordinate $w$ associated to the ions.


Figure S6: Calculated radial distribution functions: $\mathrm{O}\left(\mathrm{H}_{2} \mathrm{O}\right)-\mathrm{O}\left(\mathrm{H}_{2} \mathrm{O}\right)$ (purple), $\mathrm{F}-\mathrm{O}\left(\mathrm{H}_{2} \mathrm{O}\right)$ (green), $\mathrm{N}\left(\mathrm{THA}^{+}\right)-\mathrm{O}\left(\mathrm{H}_{2} \mathrm{O}\right)$ (light blue), $\mathrm{N}\left(\mathrm{TBA}^{+}\right)-\mathrm{O}\left(\mathrm{H}_{2} \mathrm{O}\right)$ (yellow) in liquid water. The inset shows a magnified picture for the rise distances.

## S2.4 Free energy profiles for single ions

Calculated 1-dimensional free energy profile $G^{(1)}(z)$ of the $\mathrm{F}^{-}$anion over the water-DCM interface is displayed in Figure S7. The transfer free energy of $\mathrm{F}^{-}$at no field is calculated to be $18 \mathrm{kcal} / \mathrm{mol}$, which is comparable to the experimental value, $14.0 \mathrm{kcal} / \mathrm{mol} .{ }^{20}$ Figure S 7 shows that the free energy profile of $\mathrm{F}^{-}$is sensitive to the imposed electric field $E_{z}$. With increasing electric field $E_{z}$, the asymptotic free energy of the $\mathrm{F}^{-}$ion decreases in the bulk oil phase $(z \gg 0)$ due to the electrostatic force on the negative charge, and accordingly the barrier height of the $\mathrm{F}^{-}$transfer along the $G^{(1)}(z)$ profile decreases. The present barrier height, $14 \mathrm{kcal} / \mathrm{mol}$, at $E_{z}=0.2 \mathrm{~V} / \mathrm{nm}$ for the $\mathrm{F}^{-}$alone is essentially equivalent to the barrier ( $\sim 14 \mathrm{kcal} / \mathrm{mol}$ ) at the transition state X for the $\mathrm{F}^{-}-\mathrm{TBA}^{+}$system in Figure S 4 (c), where $\mathrm{TBA}^{+}$forms no transient ion pair during the transport.


Figure S7: Calculated $G^{(1)}(z)$ profiles of $\mathrm{F}^{-}$over water-DCM interface. $E_{z}=0.0$ (purple), 0.1 (green), $0.2 \mathrm{~V} / \mathrm{nm}$ (blue).

Figure S 8 displays the 1-dimensional free energy $G^{(1)}(z)$ of the cations ( $\mathrm{THA}^{+}, \mathrm{TBA}^{+}$) alone with varying electric field. Under the electric field $E_{z}=0.2 \mathrm{~V} / \mathrm{nm}$, both $\mathrm{THA}^{+}$and $\mathrm{TBA}^{+}$show increasing free energy $G^{(1)}(z)$ with increasing $z$ in the oil phase, which is in contrast to $\mathrm{F}^{-}$(Figure S7) due to the opposite charge. Under the condition of no field
$E_{z}=0.0 \mathrm{~V} / \mathrm{nm}$, the $G^{(1)}(z)$ profiles of both $\mathrm{THA}^{+}$and $\mathrm{TBA}^{+}$have minimum near the water-DCM interface $z \approx 2 \AA$, indicating slight interface activity of $\mathrm{THA}^{+}$and $\mathrm{TBA}^{+}$.

## S2.5 Dissociation of ion pair in oil phase

We also investigate the free energy associated to the formation/break of ion pair in the bulk DCM phase. The break process of the ion pair in the oil phase is involved in the shuttling mechanism of path (B-1). The calculated 1-D free energy surfaces $G^{(1)}(r)$ with respect to the distance between $\mathrm{F}^{-}$and $\mathrm{THA}^{+} / \mathrm{TBA}^{+}$are displayed in Figure S9. The minima of $G^{(1)}(r)$ at $r \approx 3.5 \AA$ indicates the ion pair, and the free energy barrier for dissociation is evaluated with the maxima of $G^{(1)}(r)$ at $r \approx 6 \AA$. We notice that the barrier heights are nearly same between $\mathrm{THA}^{+}$and $\mathrm{TBA}^{+}$within $1 \mathrm{kcal} / \mathrm{mol}$.

Comparing the panel (a) $E_{z}=0.0 \mathrm{~V} / \mathrm{mn}$ (no field) with (b) $E_{z}=0.2 \mathrm{~V} / \mathrm{nm}$, we notice that the electric field reduces the dissociation barrier by about $1 \mathrm{kcal} / \mathrm{mol}$ commonly for both THA ${ }^{+}$and $\mathrm{TBA}^{+}$cases. The reduced barrier is readily understood with the electrostatic energy of the ion pair. The electric field $E_{z}$ tends to align the ion pair along the direction of the field, and consequently the structural change from the ion pair ( $r=3.7 \AA$ ) to the barrier position ( $r=6.0 \AA$ ) accompanies the change in the electrostatic energy of the ion pair. The change in the electrostatic energy under the field $E_{z}=0.2 \mathrm{~V} / \mathrm{nm}$ is estimated to

$$
\begin{equation*}
E_{z} \cdot \Delta r \simeq 0.2 \mathrm{~V} / \mathrm{nm} \times(6.0-3.7) \AA \times 23.06 \mathrm{kcal} / \mathrm{mol} / \mathrm{eV} \simeq 1 \mathrm{kcal} / \mathrm{mol} \tag{S11}
\end{equation*}
$$

## S3 Discussion - Criteria of Shuttling Mechanism

The essential factor to determine whether the catalytic shuttling mechanism takes place or not is the relative free energy barriers of two possible paths (B-1) shuttling and (B-2) no shuttling. We have argued the relative free energies with Figure 4 of the main text. Here we quantitatively discuss the free energy of each elementary step involved in these paths
(a)

(b)


Figure S8: Calculated $G^{(1)}(z)$ profiles over water-DCM interface for (a) THA ${ }^{+}$and (b) TBA ${ }^{+}$.
(a)

(b)


Figure S9: Calculated $G^{(1)}(r)$ as a function of the distance $r$ between $\mathrm{F}^{-}$and N site of THA ${ }^{+}$ (purple) or $\mathrm{TBA}^{+}$(green) in the bulk DCM phase. Panel (a) shows the results at no field $E_{z}=0.0 \mathrm{~V} / \mathrm{nm}$, and (b) at $E_{z}=0.2 \mathrm{~V} / \mathrm{nm}$.
to discuss the net barriers and transport mechanism. In this section we deal with the free energies of $\mathrm{F}^{-}$transport under the electric field $E_{z}=0.2 \mathrm{~V} / \mathrm{nm}$, unless otherwise noted.

The scheme of elementary kinetic steps involved in the two possible paths (B-1) and (B-2) is shown in Figure S10. The (B-1) path is considered as a two-step route; first the ion pair is formed and transported in the oil phase, and then the ion pair breaks to allow the ion to enter the bulk oil phase. On the other hand, (B-2) is a one-step route that the $\mathrm{F}^{-}$transfers from water to oil phase alone with virtually little role of the ligand.

In the (B-1) path, the first stage of the transport of ion pair over the interface is illustrated in the free energy profile $G^{(1)}(z)$ in Figure $S 5$. The transport of the ion pair has a slight barrier near the interface, and the free energy of transport is estimated to be $2 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{F}^{-}-\mathrm{THA}^{+}$and $10 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{F}^{-}-\mathrm{TBA}^{+}$. The $\mathrm{F}^{-}-\mathrm{THA}^{+}$complex is stabler in the oil phase, since THA ${ }^{+}$is more hydrophobic than $\mathrm{TBA}^{+}$. (Note that the barrier in the first stage is not associated to the rate-determining step, as we show below.) Then the ion pair eventually breaks in the oil phase toward the final state, and this latter stage is illustrated in the free energy profile $G^{(1)}(r)$ in Figure S9. The barrier for dissociation is estimated to be $9.5 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{F}^{-}-\mathrm{THA}^{+}$and $9.0 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{F}^{-}-\mathrm{TBA}^{+}$from Figure $\mathrm{S} 9(\mathrm{~b})$. The barrier for the dissociation is found to be nearly unchanged between $\mathrm{THA}^{+}$and $\mathrm{TBA}^{+}$. The net transition state (TS) of the path (B-1) is located in the latter stage to break the transient ion pair.

On the other hand, the (B-2) path involves no transient ion pair, and is equivalent to the transport of $\mathrm{F}^{-}$alone. The barrier height of (B-2) is essentially equivalent to that of $G^{(1)}(z)$ profile of single $\mathrm{F}^{-}$in Figure S 7 , and estimated to be $14 \mathrm{kcal} / \mathrm{mol}$ under $E_{z}=0.2$ $\mathrm{V} / \mathrm{nm}$. In fact, this barrier height $\sim 14 \mathrm{kcal} / \mathrm{mol}$ agrees with that of the transition state X in Figure $\mathrm{S} 4(\mathrm{c})$, where the TS of (B-2) path is well defined in the $\mathrm{F}^{-}-\mathrm{TBA}^{+}$case.

Based on the above estimations in Figure S10, we compare the free energies of two possible paths (B-1) and (B-2). The total barrier in the (B-1) path is estimated to be $2+9.5 \simeq 11.5$ $\mathrm{kcal} / \mathrm{mol}$ for $\mathrm{F}^{-}-\mathrm{THA}^{+}$and $10+9 \simeq 19 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{F}^{-}-\mathrm{TBA}^{+}$. On the other hand, the
barrier in the (B-2) path is estimated to be $14 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{F}^{-}-\mathrm{THA}^{+}$and $\mathrm{F}^{-}-\mathrm{TBA}^{+}$, irrespective of the ligand. By comparing the total barrier heights of (B-1) and (B-2), we understand that $\mathrm{F}^{-}-\mathrm{THA}^{+}$prefers the ( $\mathrm{B}-1$ ) shuttling path while $\mathrm{F}^{-}-\mathrm{TBA}^{+}$prefers the (B-2) no shuttling path. The distinct behavior is mostly attributed to the difference in hydrophobicity of $\mathrm{THA}^{+}$and $\mathrm{TBA}^{-}$which governs the stability of the transient ion pair in the oil phase.


Figure S10: Kinetic scheme of interfacial transport of $\mathrm{F}^{-}$with $\mathrm{THA}^{+} / \mathrm{TBA}^{+}$. Two paths (B-1: shuttle) and (B-2: no shuttle) are illustrated with their intermediate and transition states. Two figures associated to an arrow (e.g. $2 / 10$ ) mean the estimated free energy costs at each kinetic step for the $\mathrm{F}^{-}$transfer assisted with $\mathrm{THA}^{+}$and $\mathrm{TBA}^{+}$, respectively, in kcal/mol.

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