

Supporting Information

3D Printed Microdroplet Curing: Unravelling the Physics of On-spot Photopolymerization

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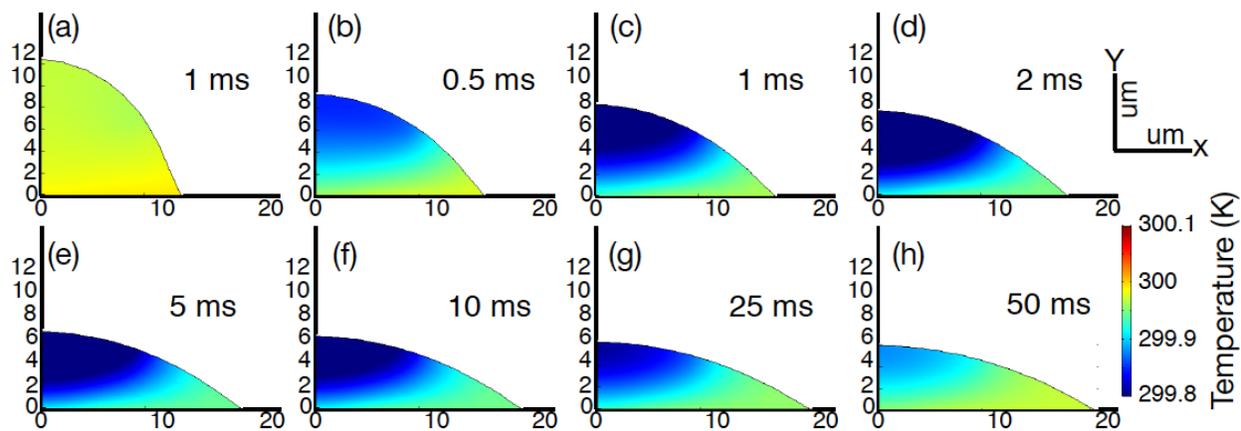


Figure S1(a-h): Temperature distribution within the spreading polymer drop (radius 0.01 mm)

at different time instants for case 1 ($\tau_s \ll \tau_p$). Here we have $\tau_s \approx 1.1$ ms and $\tau_p \approx 66$ ms.

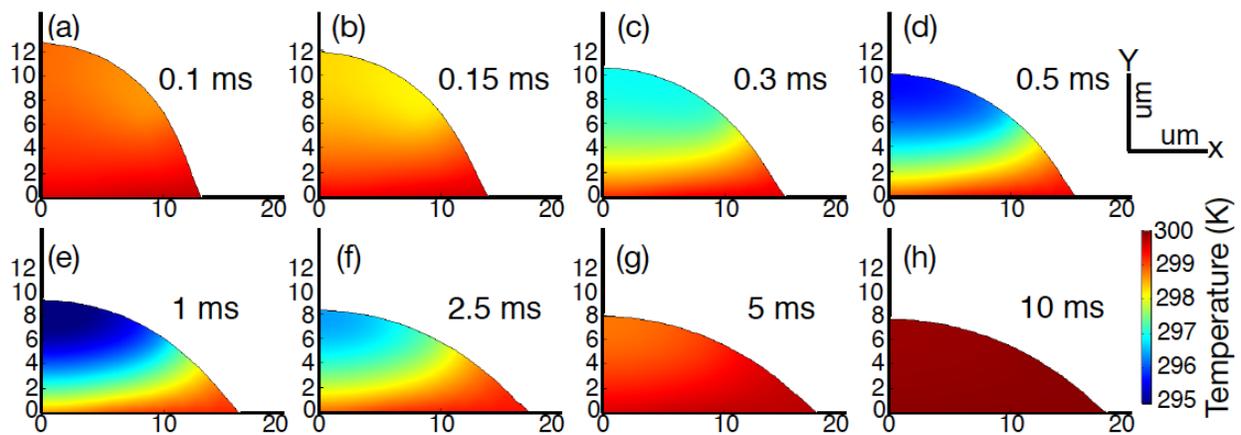


Figure S2(a-h): Temperature distribution within the spreading polymer drop (radius 0.01 mm) at

different time instants for case 2 ($\tau_s \sim \tau_p$). Here we have $\tau_s \approx 1.1$ ms and $\tau_p \approx 3.3$ ms.

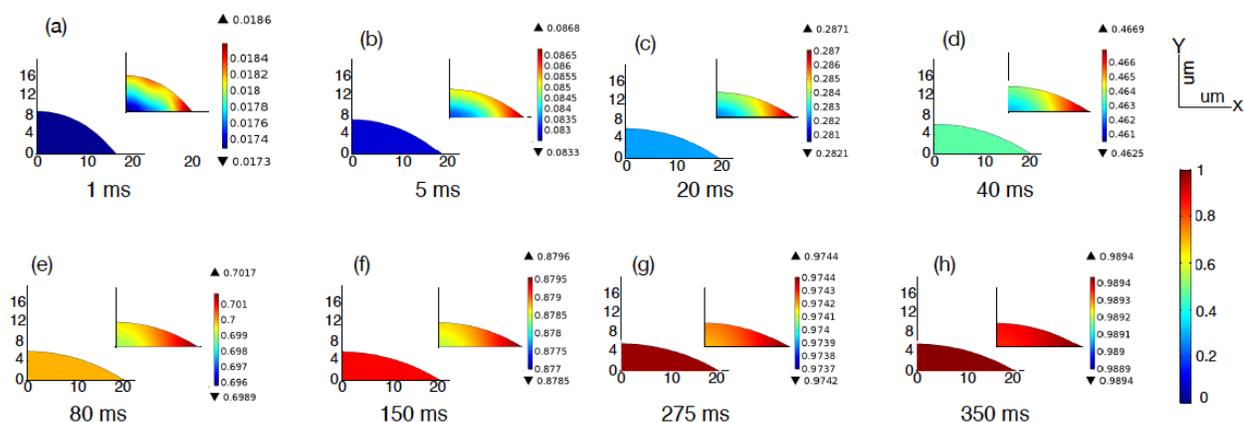


Figure S3(a-h): Curing profiles within the spreading polymer drop (radius 0.01 mm) at different time instants for case 1 ($\tau_s \ll \tau_p$). Here we have $\tau_s \approx 1.1$ ms and $\tau_p \approx 66$ ms. In the inset of each subfigure, we plot the variation of the curing profile with a much smaller range of the color bar for highlighting the curing profiles (or equivalently, a distribution of the monomer concentration) within the drop itself at a given time instant.

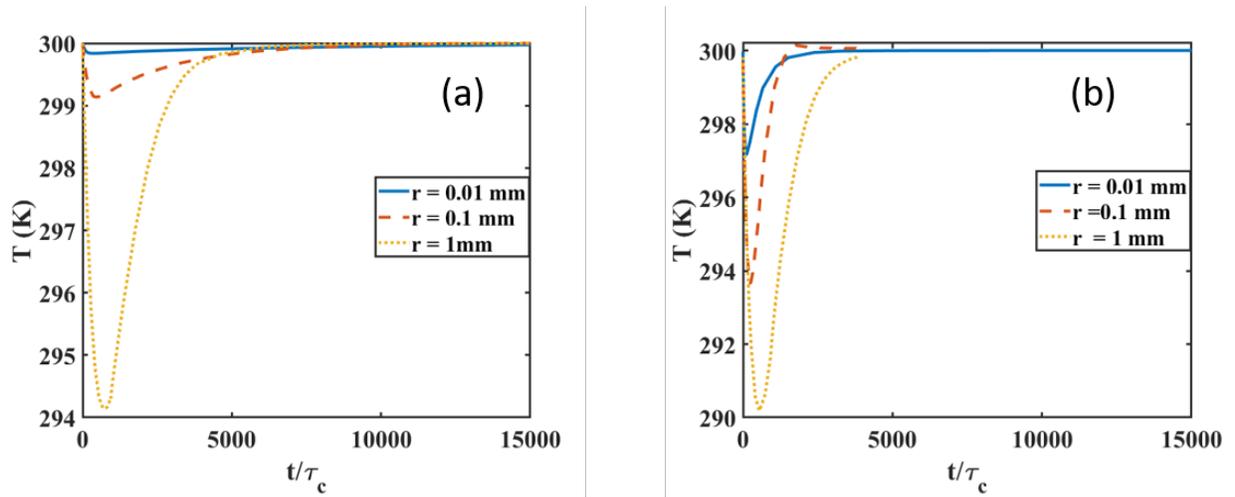


Figure S5: Variation of the average temperature of the drop with t/τ_c for (a) Case 1 and (b) Case 2 for the drops of three different sizes. The different parameters have been summarized in the caption of Fig. 8 of the main paper.

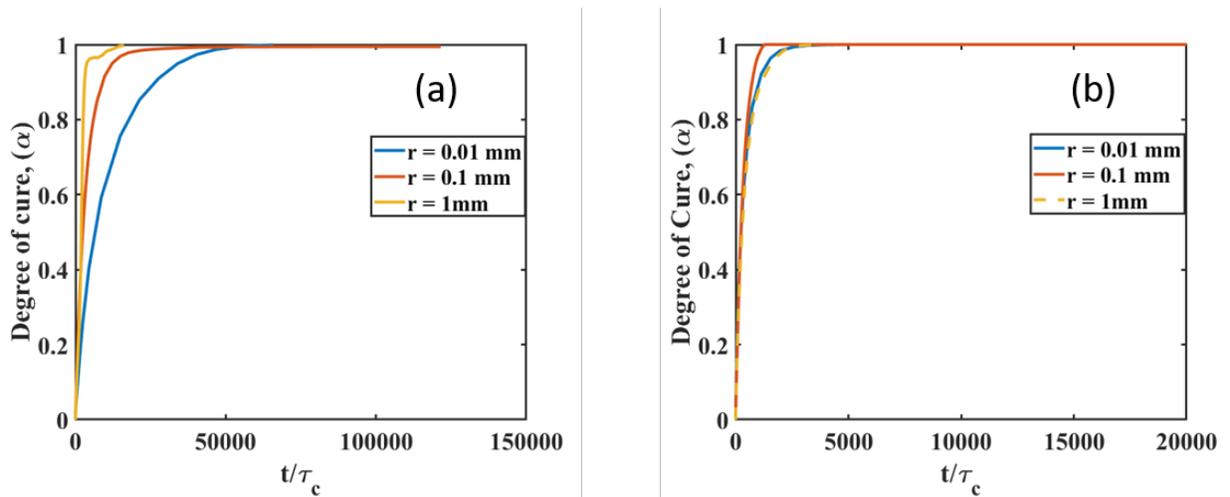


Figure S6: Variation of the average degree of cure for the drop with t/τ_c for (a) Case 1 and (b) Case 2 for the drops of three different sizes. The different parameters have been summarized in the caption of Fig. 8 of the main paper.

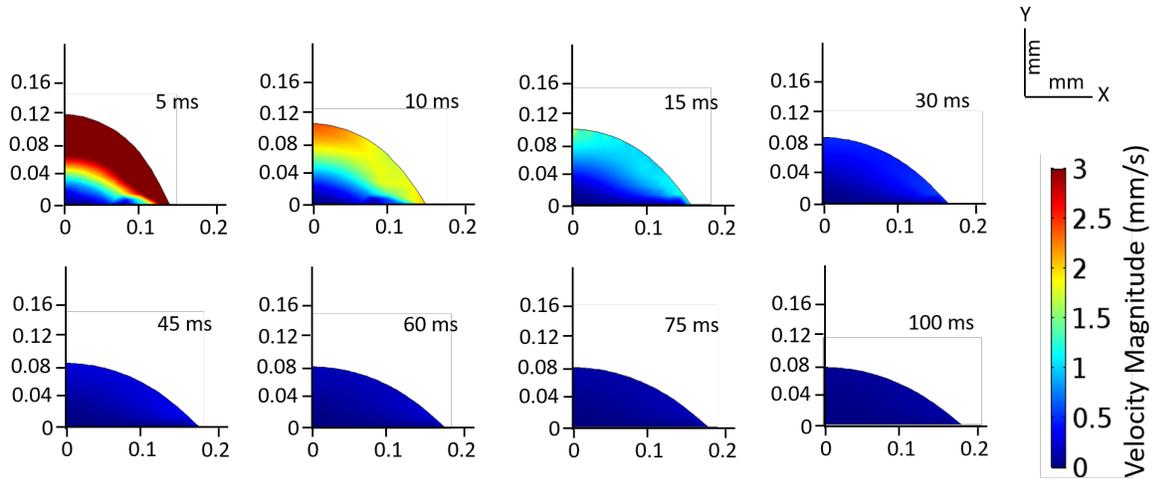


Figure S7: Velocity distribution within the spreading polymer drop at different time instants for case 1 ($\tau_s \ll \tau_p$) for a drop of radius 0.1 mm. Here we have $\tau_s \approx 10.2$ ms and $\tau_p \approx 660$ ms. Velocity profiles within the air have not been shown for the sake of clarity.

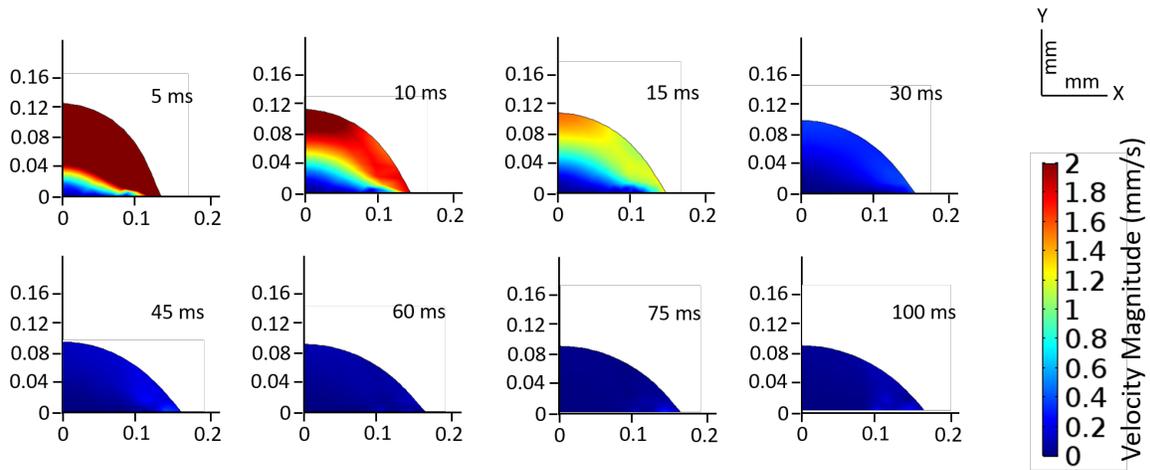


Figure S8: Velocity distribution within the spreading polymer drop at different time instants for case 2 ($\tau_s \sim \tau_p$) for a drop of radius 0.1 mm. Here we have $\tau_s \approx 10.2$ ms and $\tau_p \approx 66$ ms. Velocity profiles within the air have not been shown for the sake of clarity.

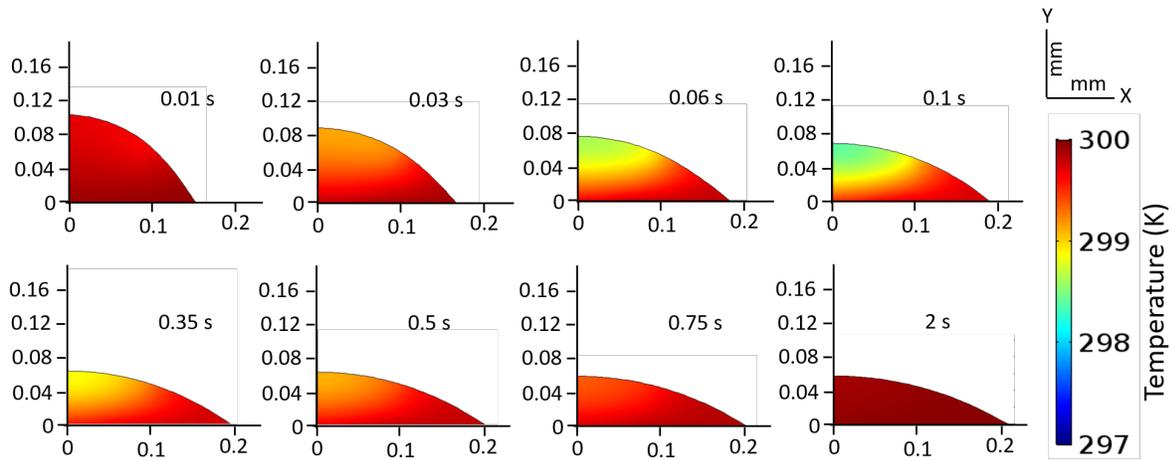


Figure S9: Temperature distribution within the spreading polymer drop at different time instants at different time instants for case 1 ($\tau_s \ll \tau_p$) for a drop of radius 0.1 mm. Here we have $\tau_s \approx 10.2$ ms and $\tau_p \approx 660$ ms.

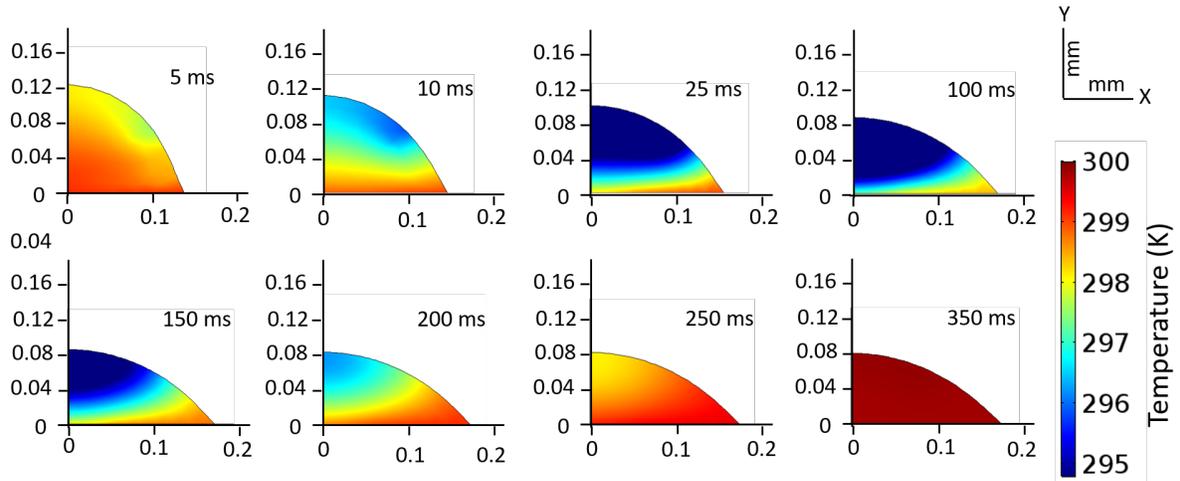


Figure S10: Temperature distribution within the spreading polymer drop at different time instants at different time instants for case 2 ($\tau_s \sim \tau_p$) for a drop of radius 0.1 mm. Here we have $\tau_s \approx 10.2$ ms and $\tau_p \approx 66$ ms.

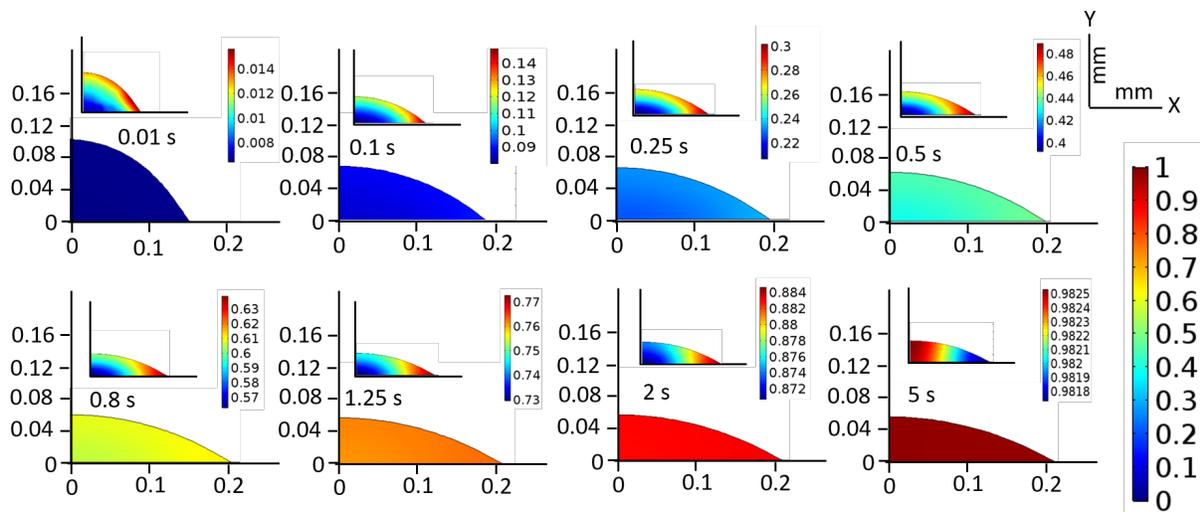


Figure S11: Curing profiles within the spreading polymer drop at different time instants for case 1 ($\tau_s \ll \tau_p$) for a drop of radius 0.1 mm. Here we have $\tau_s \approx 10.2$ ms and $\tau_p \approx 660$ ms.

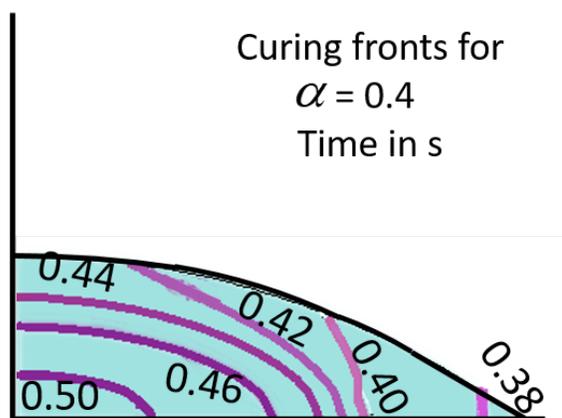


Figure S12: Progression of the curing front (corresponding to $\alpha=0.4$) within the spreading polymer drop at different time instants for case 1 ($\tau_s \ll \tau_p$) for a drop of radius 0.1 mm. Here we have $\tau_s \approx 10.2$ ms and $\tau_p \approx 660$ ms.

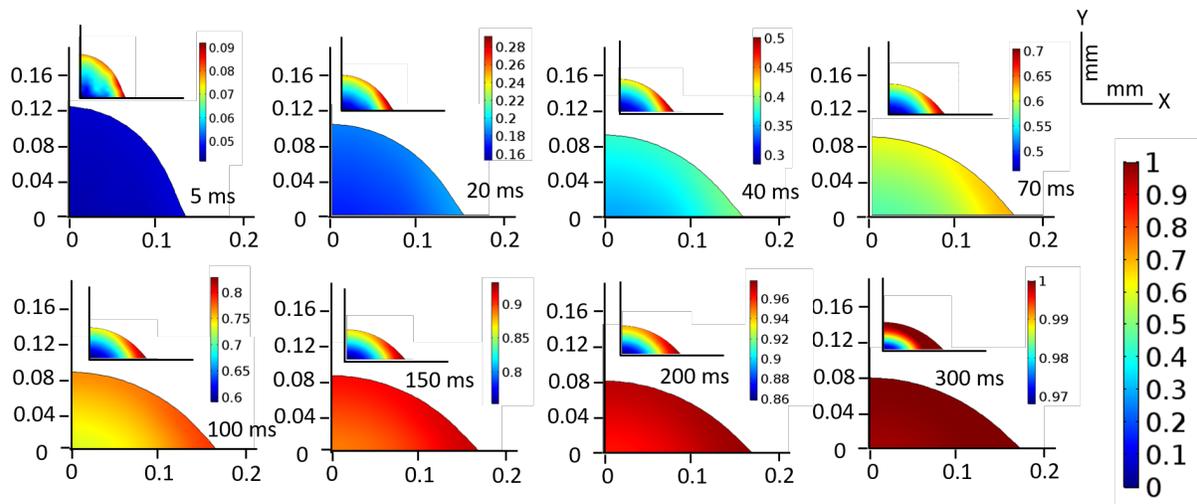


Figure S13: Curing profiles within the spreading polymer drop at different time instants for case 2 ($\tau_s \sim \tau_p$) for a drop of radius 0.1 mm. Here we have $\tau_s \approx 10.2$ ms and $\tau_p \approx 66$ ms. Here we have $\tau_s \approx 10.2$ ms and $\tau_p \approx 66$ ms.

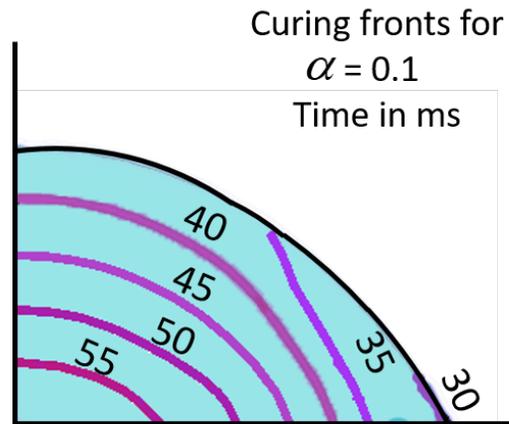


Figure S14: Progression of the curing front (corresponding to $\alpha=0.1$) within the spreading polymer drop at different time instants for case 2 ($\tau_s \sim \tau_p$) for a drop of radius 0.1 mm. Here we have $\tau_s \approx 10.2$ ms and $\tau_p \approx 66$ ms.

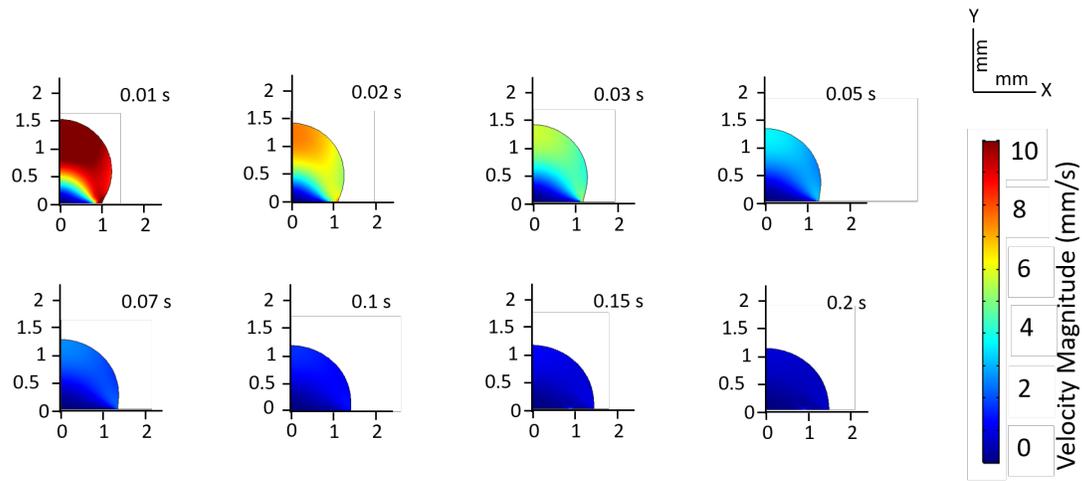


Figure S15: Velocity distribution within the spreading polymer drop at different time instants for case 1 ($\tau_s \ll \tau_p$) for a drop of radius 1 mm. Here we have $\tau_s \approx 107$ ms and $\tau_p \approx 1200$ ms. Velocity profiles within the air have not been shown for the sake of clarity.

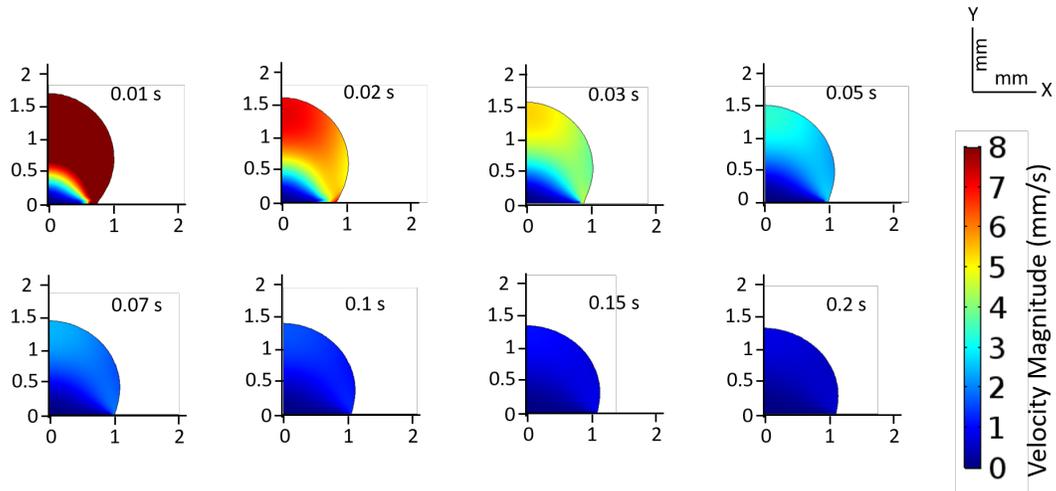


Figure S16: Velocity distribution within the spreading polymer drop at different time instants for case 1 ($\tau_s \sim \tau_p$) for a drop of radius 1 mm. Here we have $\tau_s \approx 107$ ms and $\tau_p \approx 660$ ms. Velocity profiles within the air have not been shown for the sake of clarity.

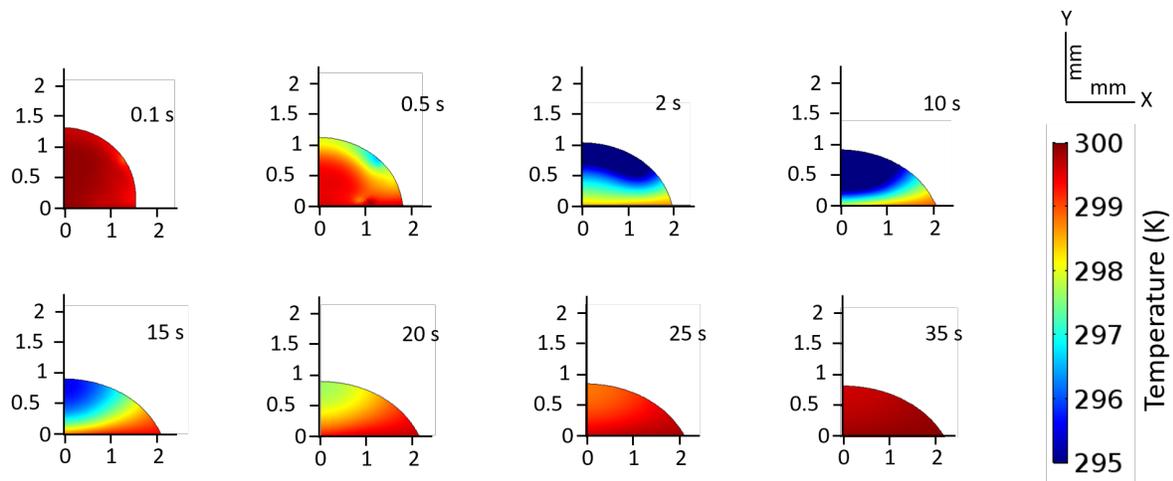


Figure S17: Temperature distribution within the spreading polymer drop at different time instants at different time instants for case 1 ($\tau_s \ll \tau_p$) for a drop of radius 1 mm. Here we have $\tau_s \approx 107$ ms and $\tau_p \approx 1200$ ms.

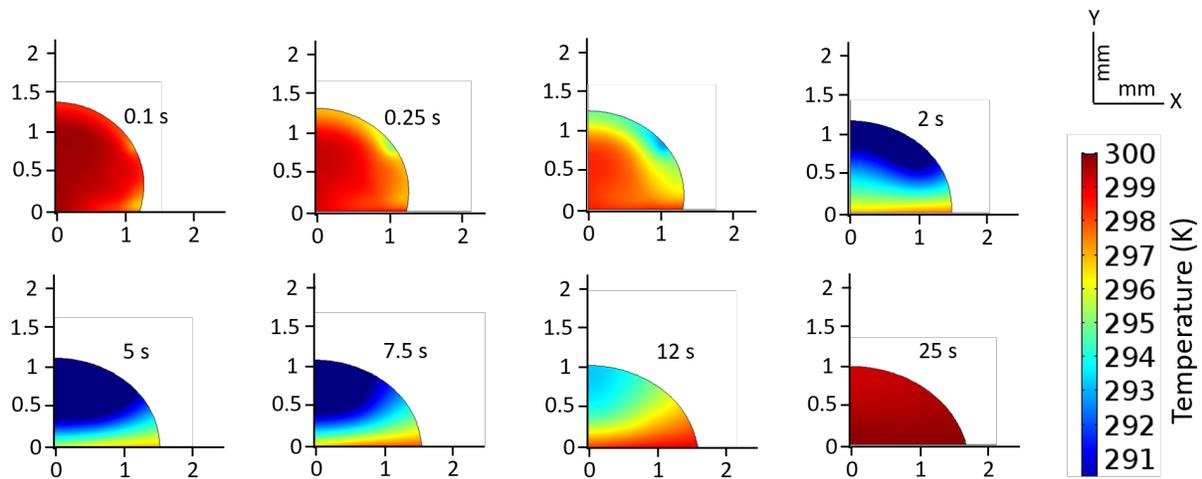


Figure S18: Temperature distribution within the spreading polymer drop at different time instants at different time instants for case 1 ($\tau_s \sim \tau_p$) for a drop of radius 1 mm. Here we have $\tau_s \approx 107$ ms and $\tau_p \approx 660$ ms.

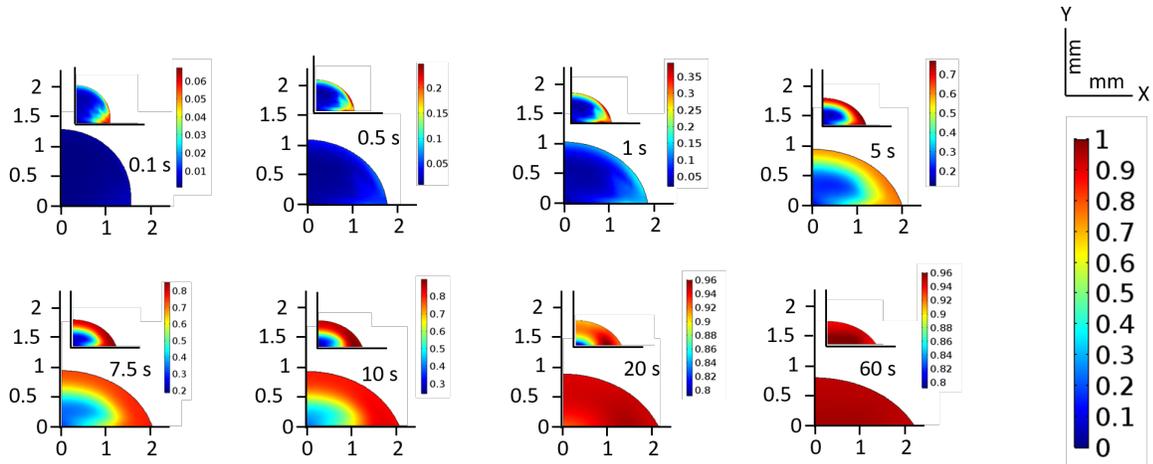


Figure S19: Curing profiles within the spreading polymer drop at different time instants for case 1 ($\tau_s \ll \tau_p$) for a drop of radius 1 mm. Here we have $\tau_s \approx 107$ ms and $\tau_p \approx 1200$ ms.

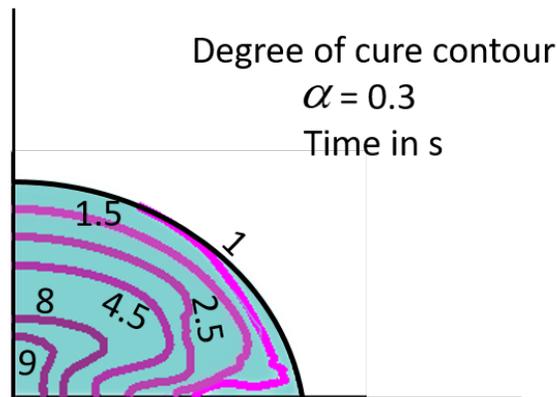


Figure S20: Progression of the curing front (corresponding to $\alpha=0.3$) within the spreading polymer drop at different time instants for case 1 ($\tau_s \ll \tau_p$) for a drop of radius 1 mm. Here we have $\tau_s \approx 107$ ms and $\tau_p \approx 1200$ ms.

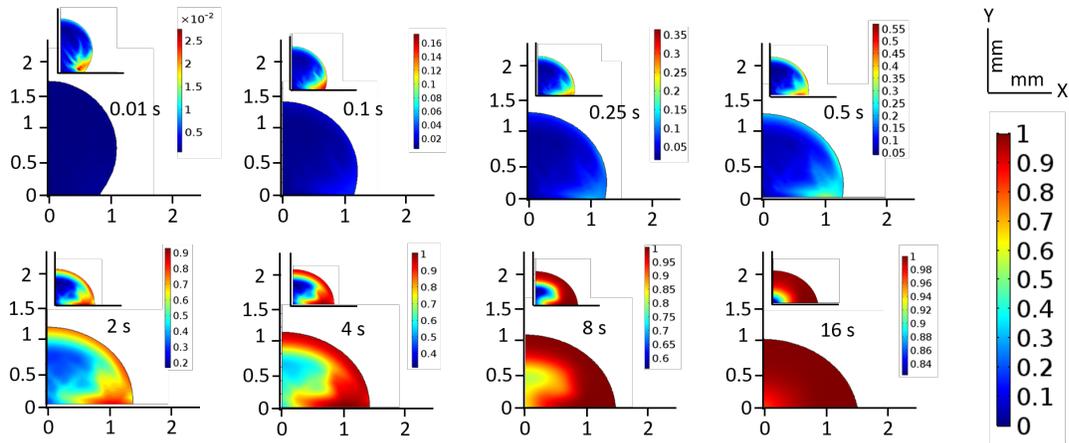


Figure S21: Curing profiles within the spreading polymer drop at different time instants for case 2 ($\tau_s \sim \tau_p$) for a drop of radius 1 mm. Here we have $\tau_s \approx 107$ ms and $\tau_p \approx 660$ ms.

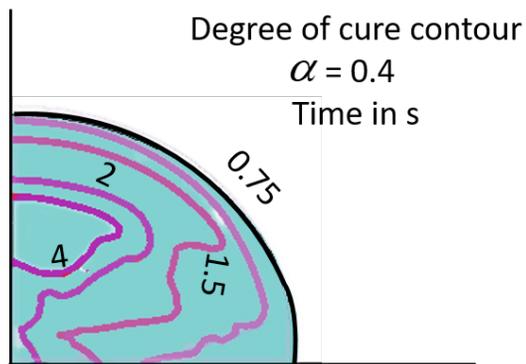


Figure S22: Progression of the curing front (corresponding to $\alpha=0.4$) within the spreading polymer drop at different time instants for case 2 ($\tau_s \sim \tau_p$) for a drop of radius 1 mm. Here we have $\tau_s \approx 107$ ms and $\tau_p \approx 660$ ms.

Table S1: Different Timescales for Drops of Different Sizes

Drop radius (mm)	τ_c (milliseconds)	τ_s (milliseconds)	τ_p (milliseconds) for Case 1	τ_p (milliseconds) for Case 2
1	7.21	107	660	1200
0.1	0.228	10.2	66	660
0.01	7.21×10^{-3}	1.1	66	3.3

Table S2: Definition and values of the different parameters used for simulating the the 1-mm drop of 1 wt % of carboxymethylcellulose (CMC) solution (those that are not reported are identical to those reported in Table 1 in the main paper) (Here we don't have the literature for the values that dictate the polymerization process of the CMC drop; therefore, we have chosen these values to be such that ensures that $\tau_s \ll \tau_p$. Under such conditions, the exact values of these parameters don't matter as long as they ensure $\tau_s \ll \tau_p$)

Parameter	Definition	Value	Reference
ρ_m	Density of monomer	1590 [kg/m ³]	Ref. 48 (in the main paper) and using the condition that the Density variation between monomer and polymer is usually less than 10% (Refs. 31,33 in the mian paper)
ρ_p	Density of polymer	1750 [kg/m ³]	
m	Consistency index	7.234	
n	Power law index	0.5088	
σ	Surface tension of the drop/air interface	0.039 [N/m]	
θ	Contact angle	20 ⁰	
k_1	Thermal conductivity of drop	0.603 [W/m/K]	Ref. 49 (in the main paper)
C_{p1}	Heat capacity (at constant pressure) of the drop	4250[J/kg/K]	Ref. 50 (in the main paper)
H_r	Heat of polymerization reaction	-50 [kJ/mol]	
E_p	Activation energy for the propagation reaction	29.7 [kJ/mol]	

E_t	Activation energy for the termination reaction	22.2 [kJ/mol]	Ref. 32 (in the main paper)
A_{p^*}	Frequency factor for the propagation reaction for case 1 ($\tau_s \ll \tau_p$)	2.5×10^9 [L/mol/s]	
A_{t^*}	Frequency factor for the termination reaction	10^{11} [L/mol/s]	