

Supplementary Information

Computational Studies of Intrinsically Disordered Proteins

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Cumulative Averaging of Observables:

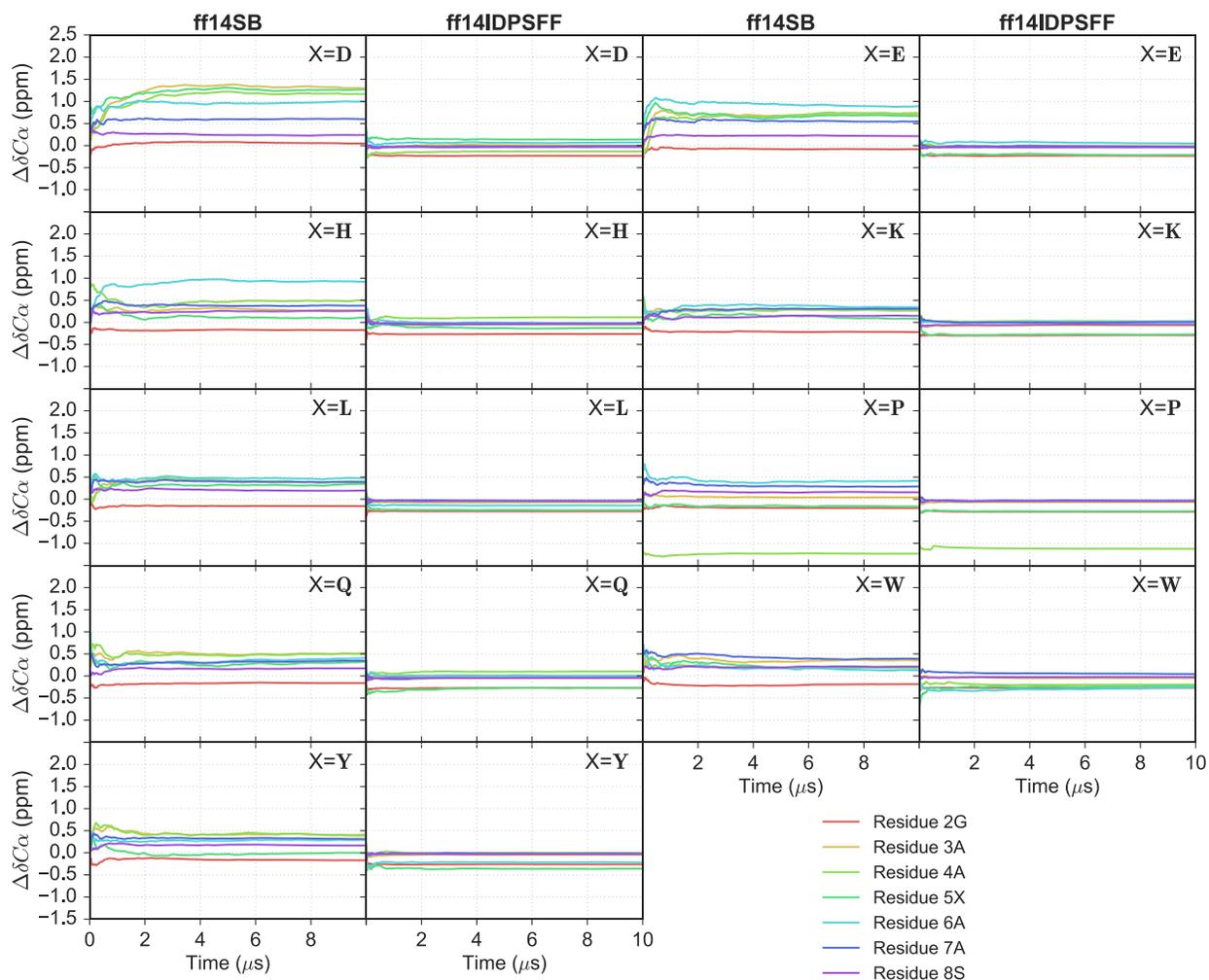


Figure S1. The $\Delta\delta C^\alpha$ -derived cumulative averages per EGAAXAASS peptide and force field type were calculated and averaged between the 10 simulations. The first/third column is populated with short peptides simulated using the *ff14SB* and the second/fourth column is populated by the corresponding peptide simulated using the *ff14IDPSFF*. Each row represents an EGAAXAASS (X = D, E, H, K, L, P, Q, W, Y) peptide.

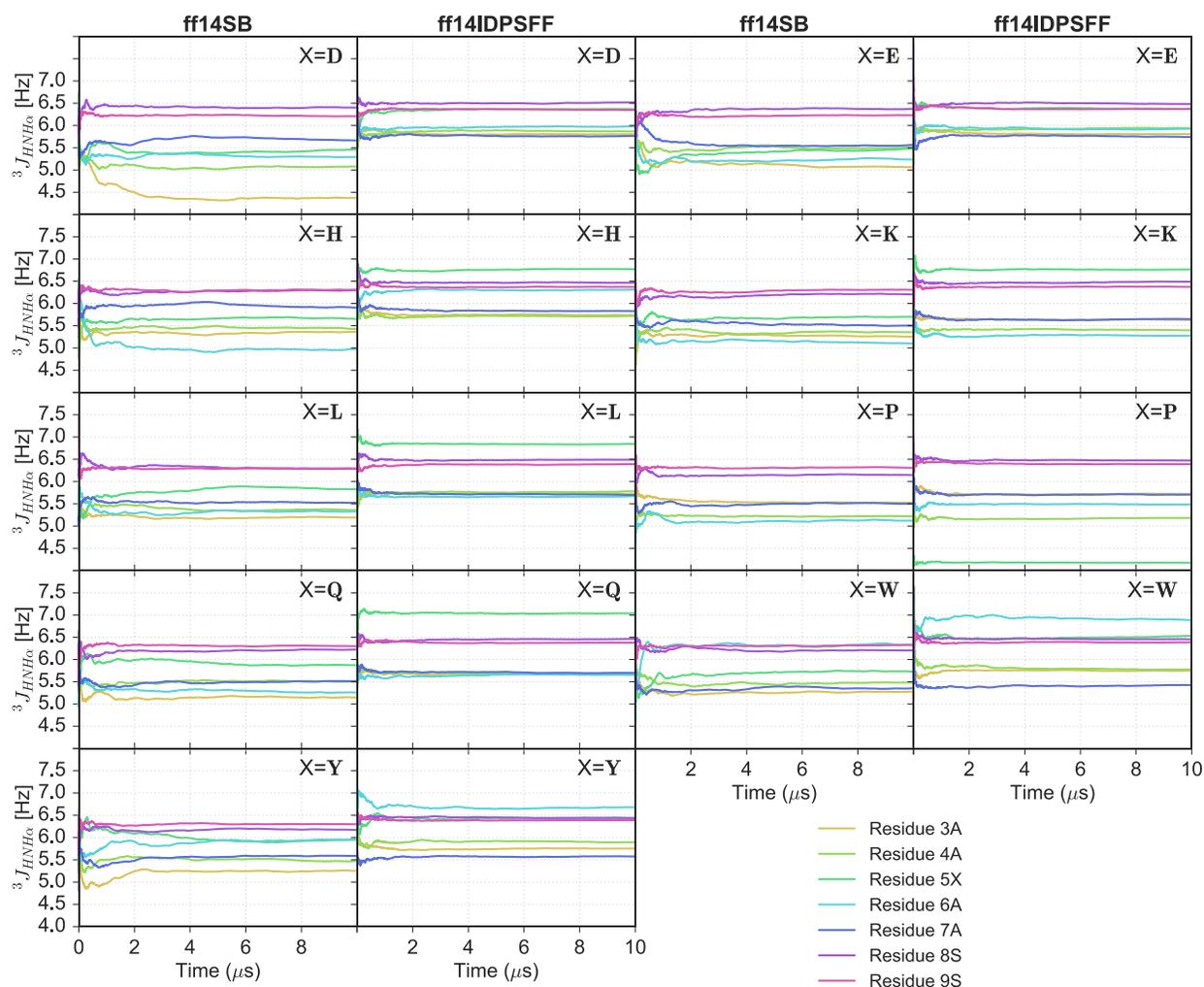


Figure S2. The $^3J_{HNH\alpha}$ -derived cumulative averages per EGAAXAASS peptide and force field type were calculated and averaged between the 10 simulations. The first/third column is populated with short peptides simulated using the *ff14SB* and the second/fourth column is populated by the corresponding peptide simulated using the *ff14IDPSFF*. Each row represents an EGAAXAASS (X = D, E, H, K, L, P, Q, W, Y) peptide.

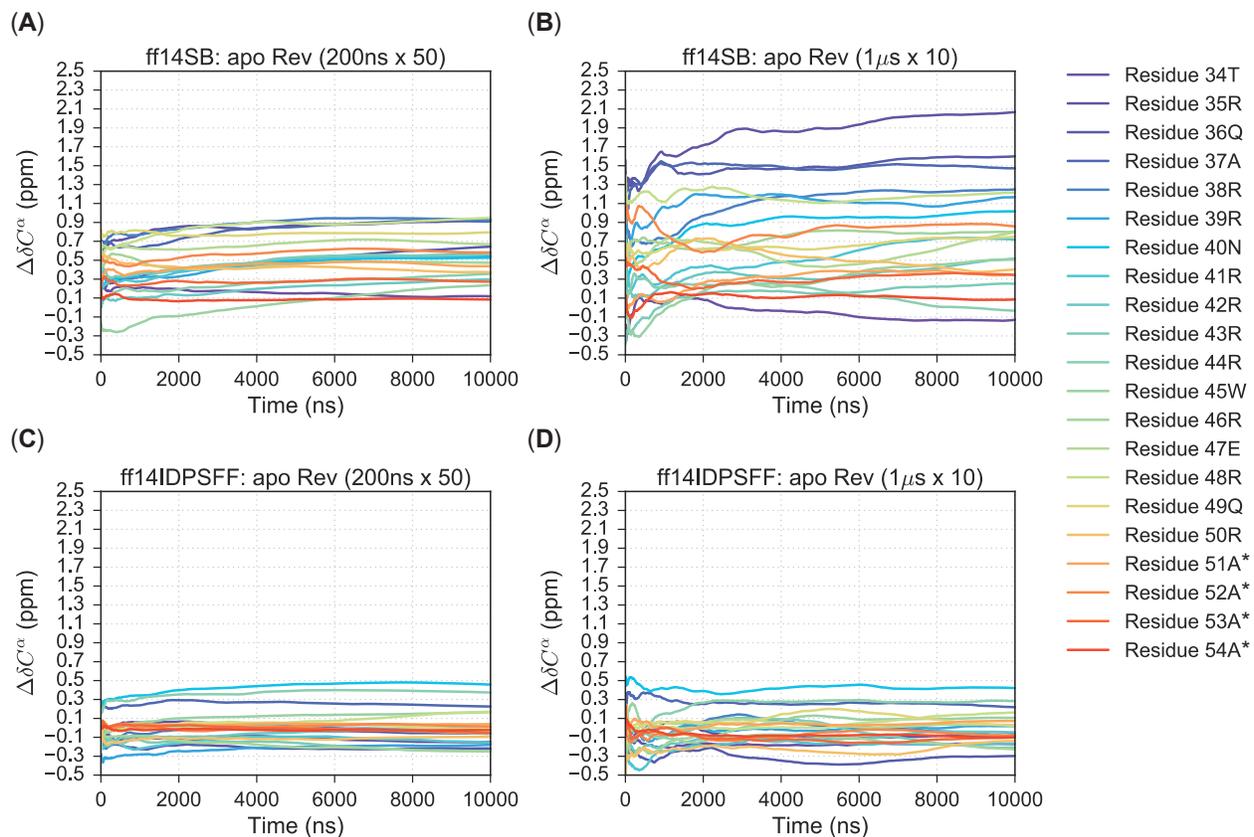


Figure S3. The $\Delta\delta C^\alpha$ -derived cumulative averages per apo Rev peptide and force field type were calculated and averaged between the 10/50 simulations. Two simulation types were generated: fifty 200ns simulations using (A) *ff14SB* (B) and *ff14IDPSFF*, (C) and ten 1 μ s simulations using *ff14SB* (D) and *ff14IDPSFF*. Residues are colored according to the legend with an asterisk (*) indicating non-native residues.

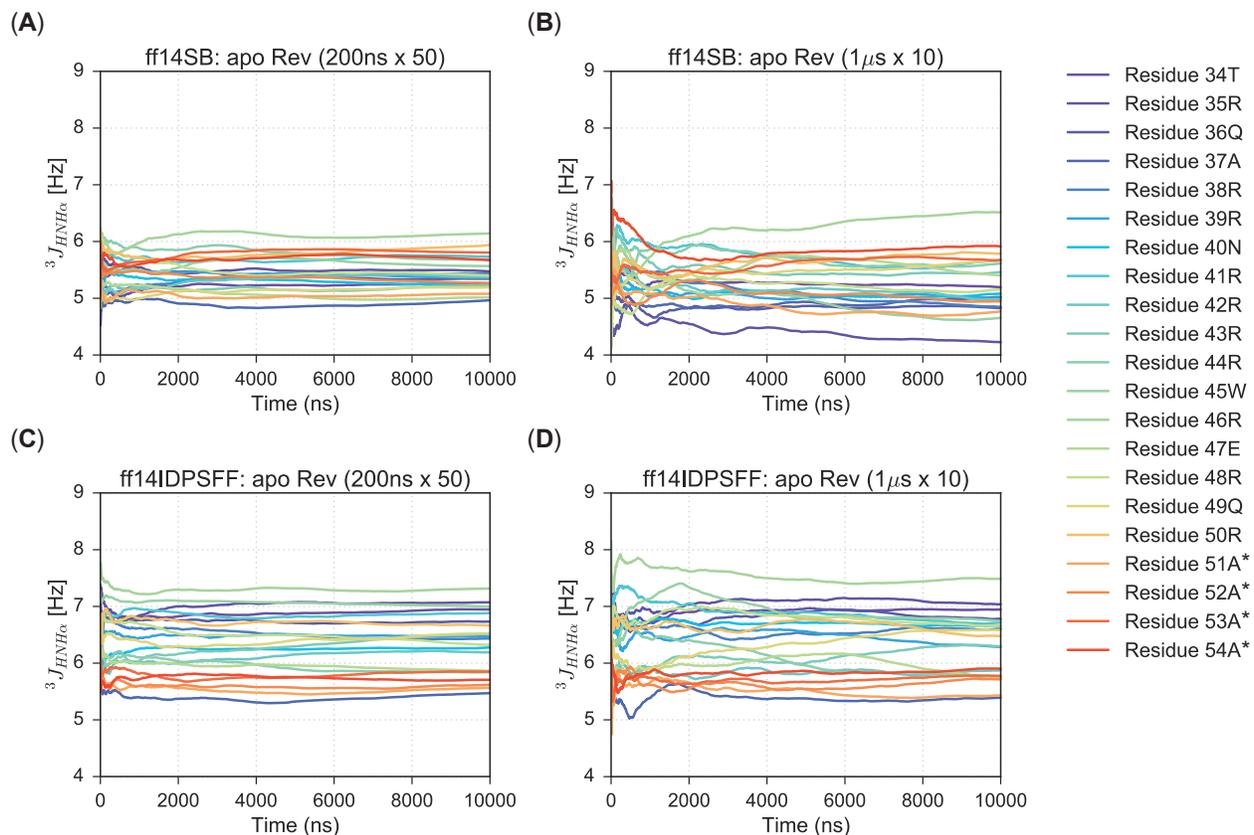


Figure S4. The $^3J_{HNH\alpha}$ -derived cumulative averages per apo Rev peptide and force field type were calculated and averaged between the 10/50 simulations. Two simulation types were generated: fifty 200ns simulations using (A) *ff14SB* (B) and *ff14IDPSFF*, (C) and ten 1 μ s simulations using *ff14SB* (D) and *ff14IDPSFF*. Residues are colored according to the legend with an asterisk (*) indicating non-native residues.

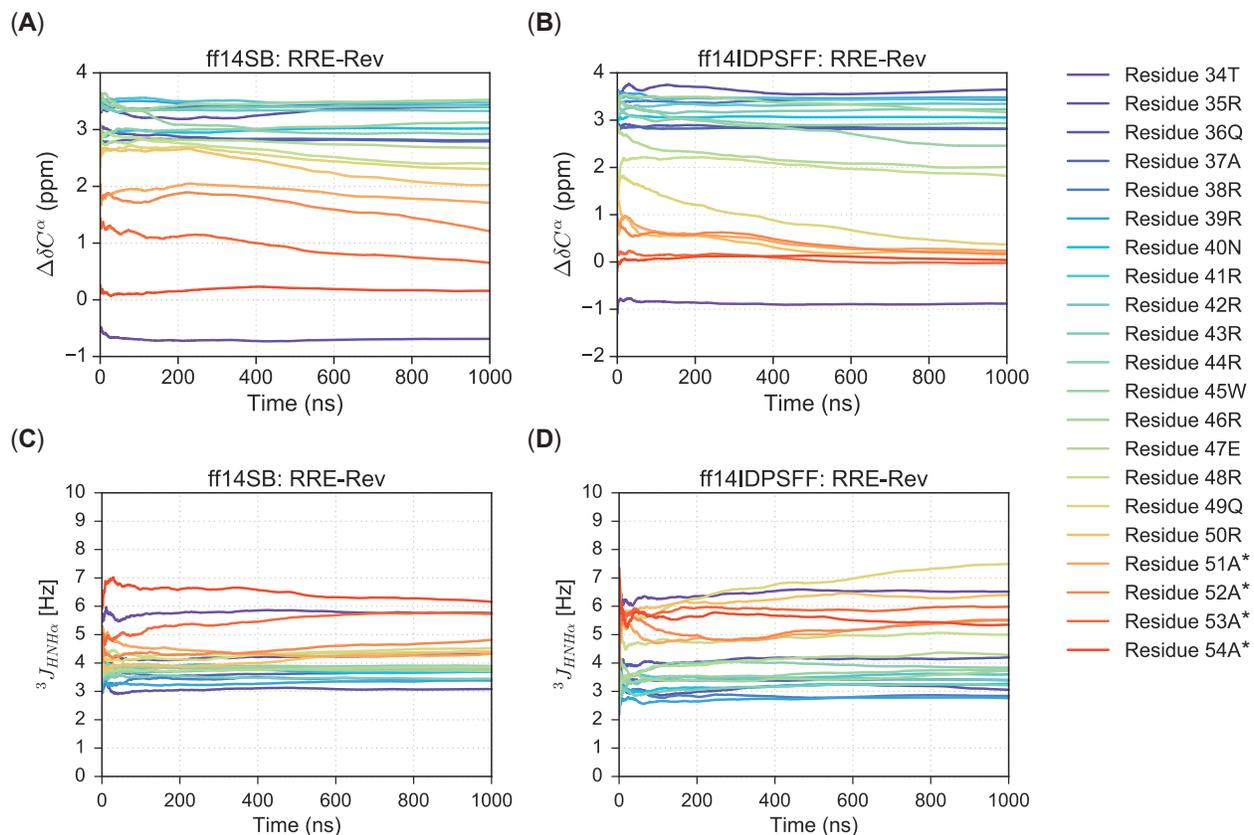


Figure S5. The $\Delta\delta C^\alpha$ - and $^3J_{HNH\alpha}$ -derived cumulative averages per RRE-Rev complex and force field type were calculated and averaged between the 5 simulations. Secondary chemical shifts occupy the first row from (A) *ff14SB*-generated simulations and (B) *ff14IDPSFF*-generated simulations. $^3J_{HNH\alpha}$ -coupling constants occupy the second row from (C) *ff14SB*-generated simulations and (D) *ff14IDPSFF*-generated simulations. Residues are colored according to the legend with an asterisk (*) indicating non-native residues.

Biphasic Exponential Fitting of $\Delta\Delta\delta C^\alpha$ Datasets:

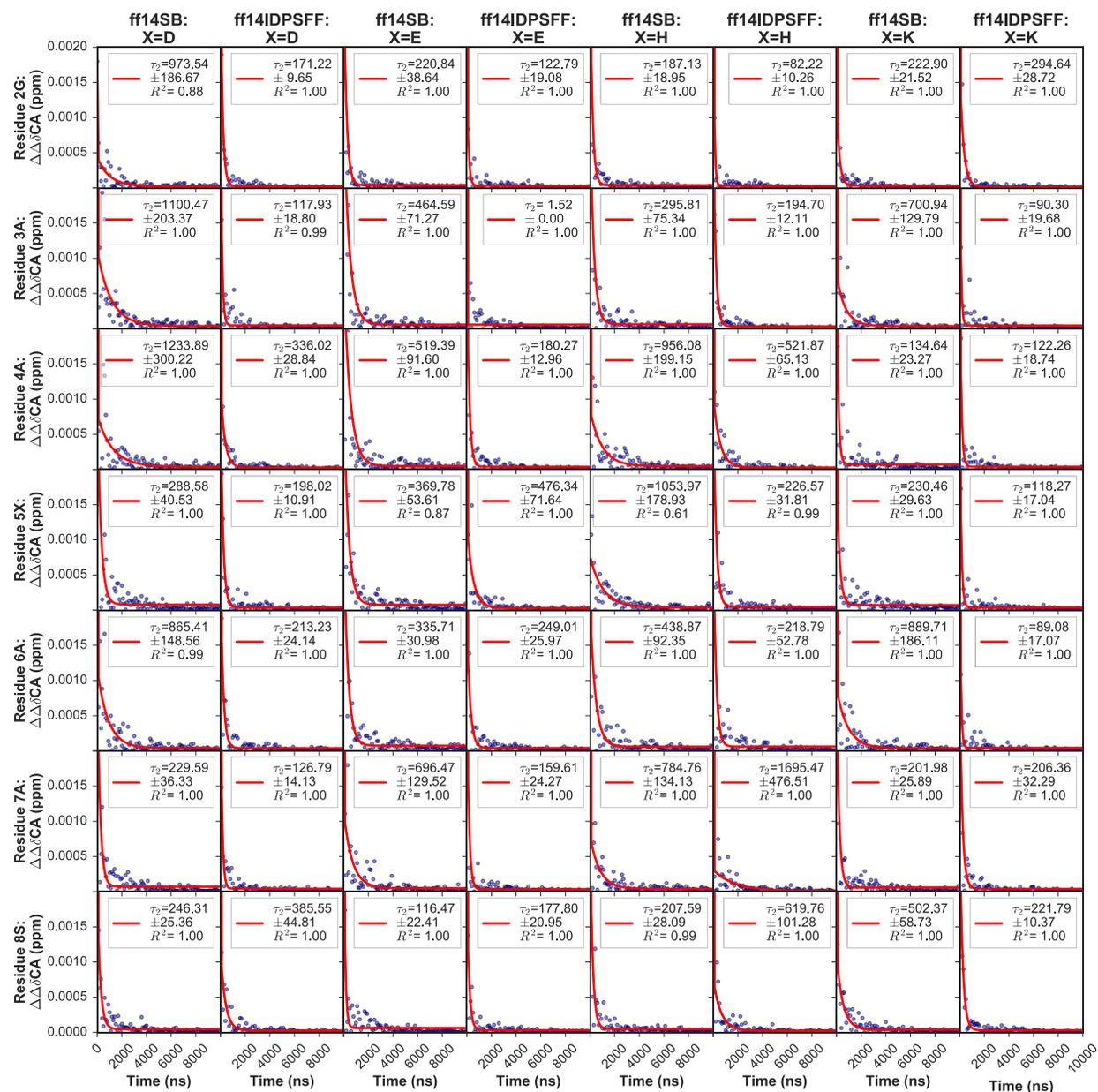


Figure S6. Biphasic exponential fittings were generated using $\Delta\Delta\delta C^\alpha$ from cumulative average data in Figure S1 for EGAAXAASS (X= D, E, H, K) peptides and force field types. Each average cumulative $\Delta\Delta\delta C^\alpha$ (blue dots) 100-ns increment was plotted per residue. Datasets were fitted to the following exponential decay function: $\Delta\Delta\delta C^\alpha = A_1 e^{-\frac{x}{\tau_1}} + A_2 e^{-\frac{x}{\tau_2}} + c$ (red line). Each column represents a peptide and force field, and each row represents a single residue. Only residues 2G-8S are fitted.



Figure S7. Biphasic exponential fittings were generated using $\Delta\Delta\delta_{CA}$ from cumulative average data in Figure S1 for EGAAXAASS (X= L, P, Q, W, Y) peptides and force field types. Each average cumulative $\Delta\Delta\delta_{CA}$ (blue dots) 100-ns increment was plotted per residue. Datasets were fitted to the following exponential decay function: $\Delta\Delta\delta_{CA} = A_1 e^{-\frac{x}{\tau_1}} + A_2 e^{-\frac{x}{\tau_2}} + c$ (red line). Each column represents a peptide and force field, and each row represents a single residue. Only residues 2G-8S are fitted.

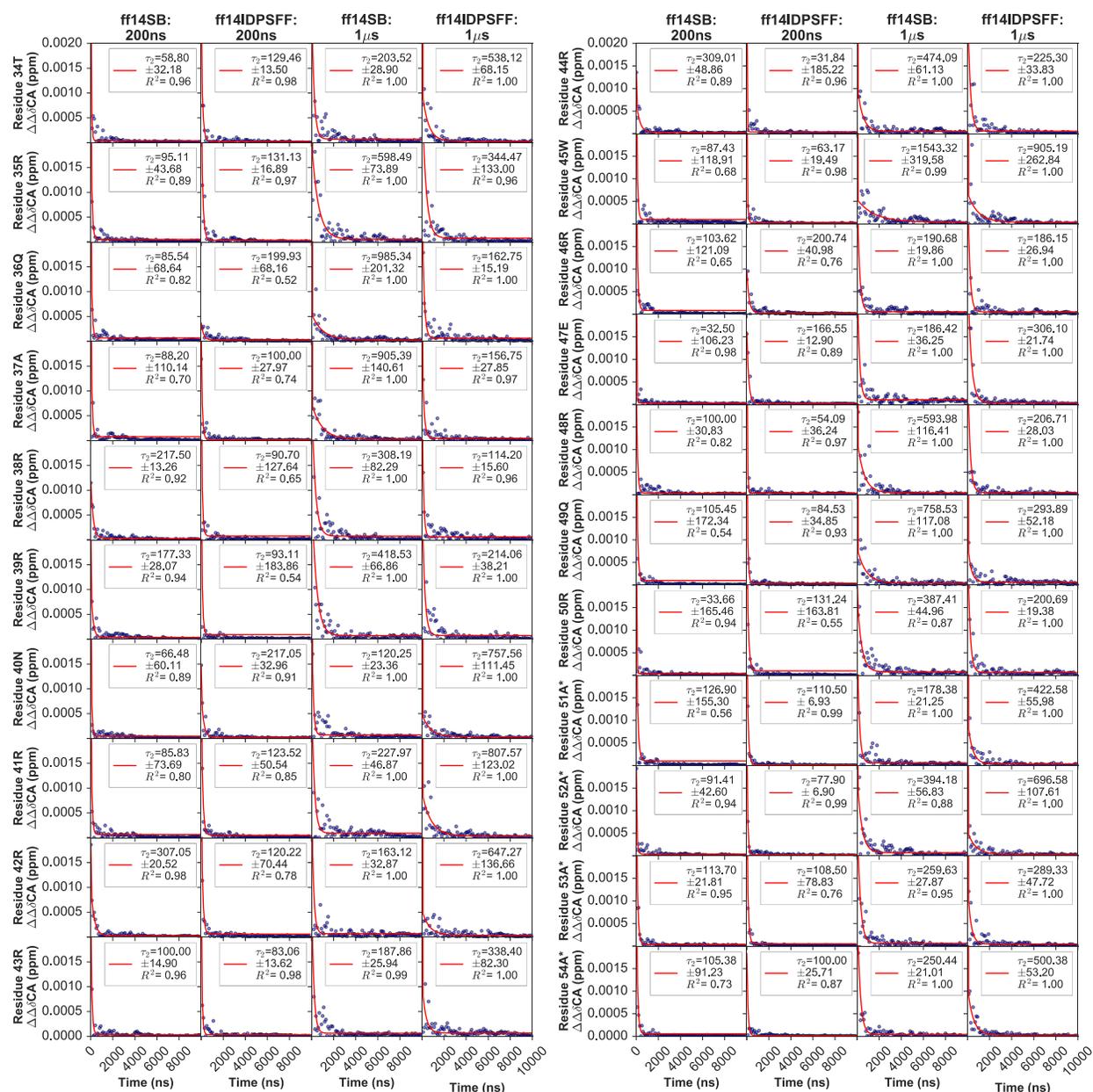


Figure S8. To evaluate cumulative average convergence of apo Rev simulations from Figure S3, a scatter plot of $\Delta\Delta\delta C^\alpha$ values (blue dots) and corresponding biphasic exponential fit were generated for each simulation (long, short) and force field (*ff14SB*, *ff14IDPSFF*) types. Datasets were fitted to the following exponential decay function: $\Delta\Delta\delta C^\alpha = A_1 e^{-\frac{x}{\tau_1}} + A_2 e^{-\frac{x}{\tau_2}} + c$ (red line). The above subplot columns are titled according to simulation and force field type and rows labeled according to residue, with non-native residues marked with an asterisk (*) on the y-axis.

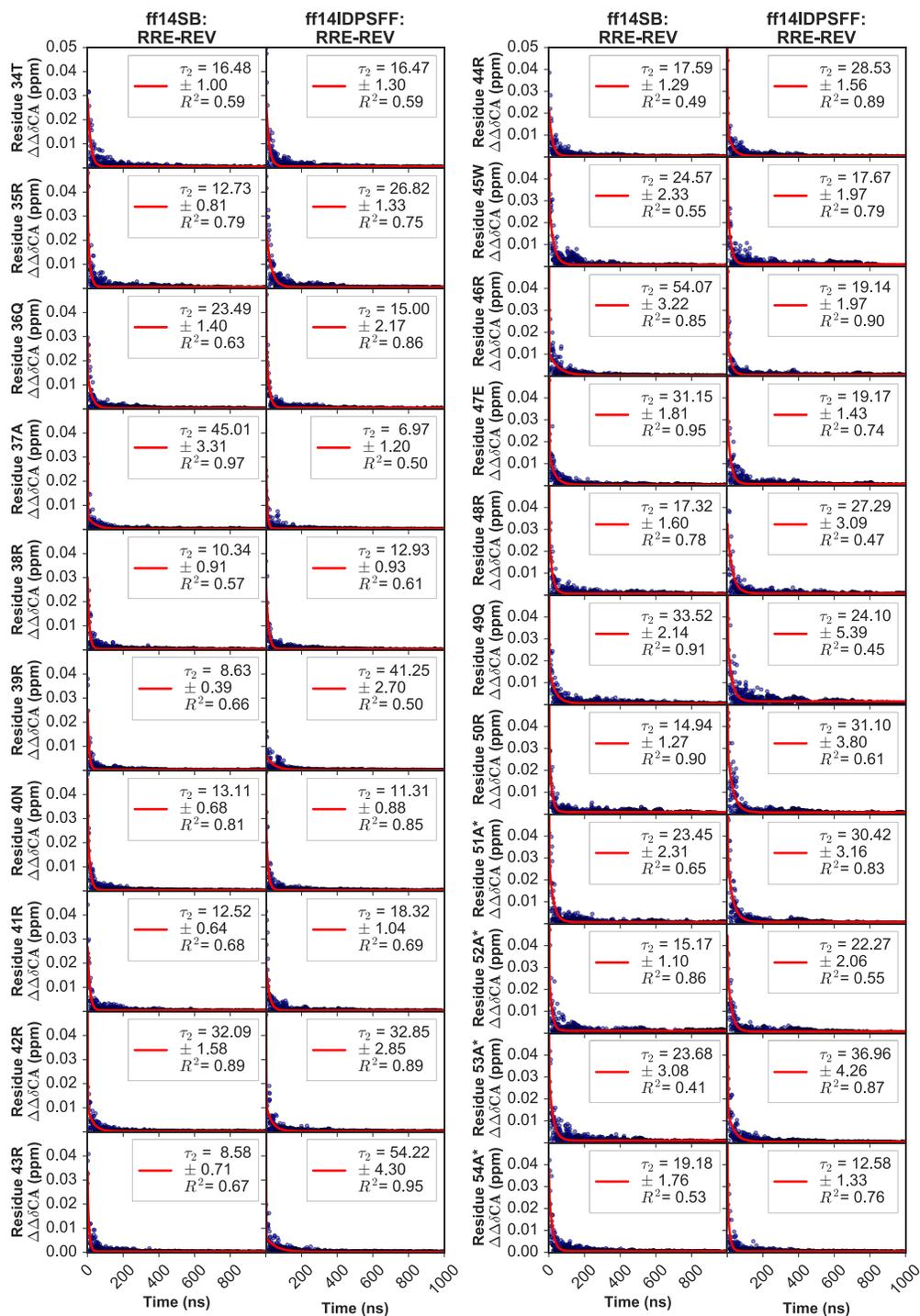


Figure S9. Biphasic exponential fittings were generated using $\Delta\Delta\delta C^\alpha$ from cumulative average data in Figure S5 for RRE-Rev complexes and force field types. We applied the same fitting to the following exponential decay function: $\Delta\Delta\delta C^\alpha = A_1 e^{-\frac{x}{\tau_1}} + A_2 e^{-\frac{x}{\tau_2}} + c$ (red line). Each average cumulative $\Delta\Delta\delta C^\alpha$ (blue dots) 1-ns increment was plotted per residue. Each column represents a peptide and force field, each row is labeled to its corresponding residue, and non-native residues marked with an asterisk (*).

Biphasic Exponential Fitting of $\Delta^3 J_{\text{HNH}\alpha}$ Datasets:

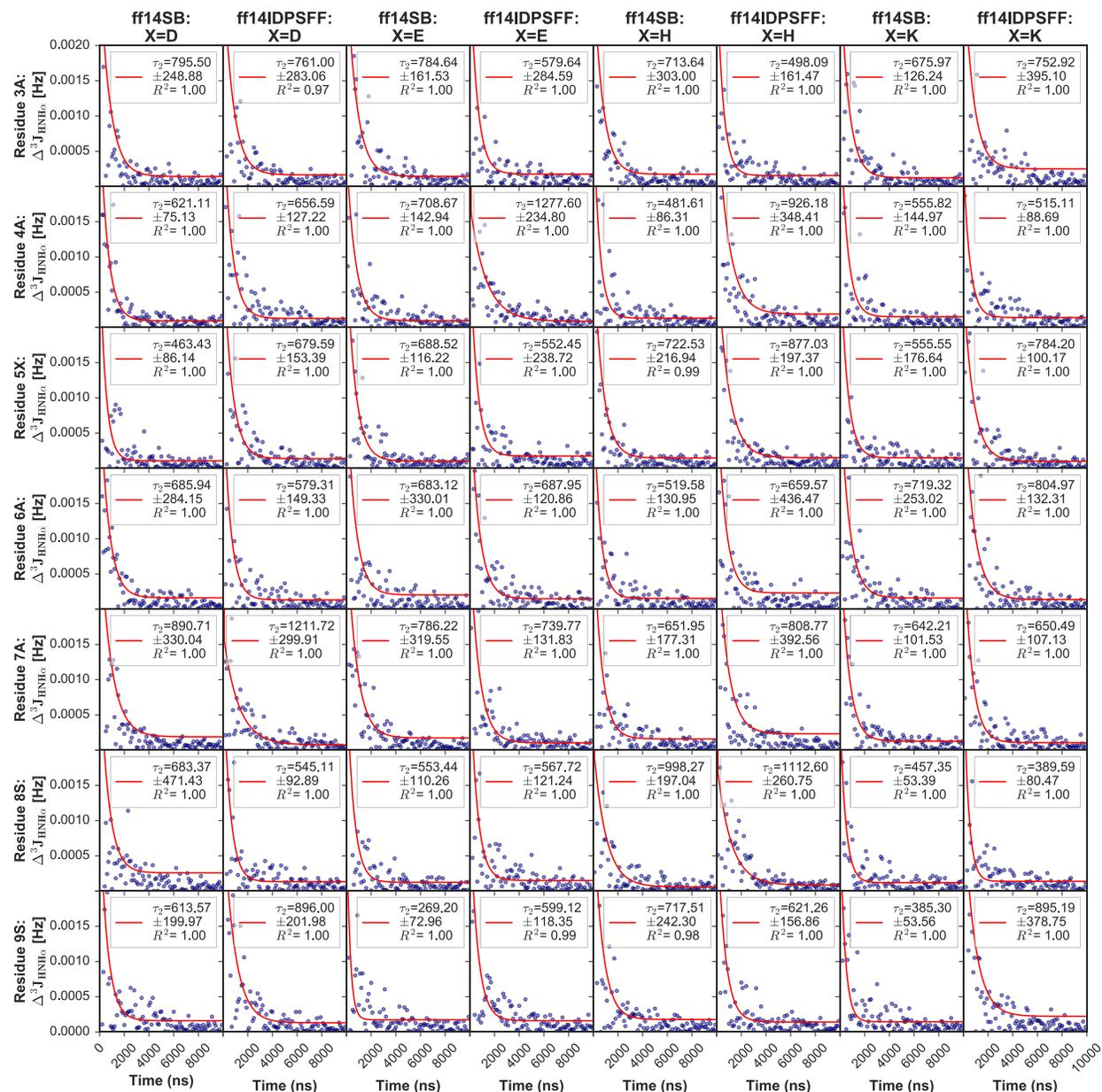


Figure S10. Biphasic exponential fittings were generated using $\Delta^3 J_{\text{HNH}\alpha}$ from cumulative average data in Figure S2 for EGAAXAASS (X= D, E, H, K) peptides and force field types. Each average cumulative $\Delta^3 J_{\text{HNH}\alpha}$ (blue dots) 100-ns increment was plotted per residue. Datasets were fitted to the following exponential decay function: $\Delta^3 J_{\text{HNH}\alpha} = A_1 e^{-\frac{x}{\tau_1}} + A_2 e^{-\frac{x}{\tau_2}} + c$ (red line). Each column represents a peptide and force field and each row represents individual residues. Only residues 3A-9S are fitted.

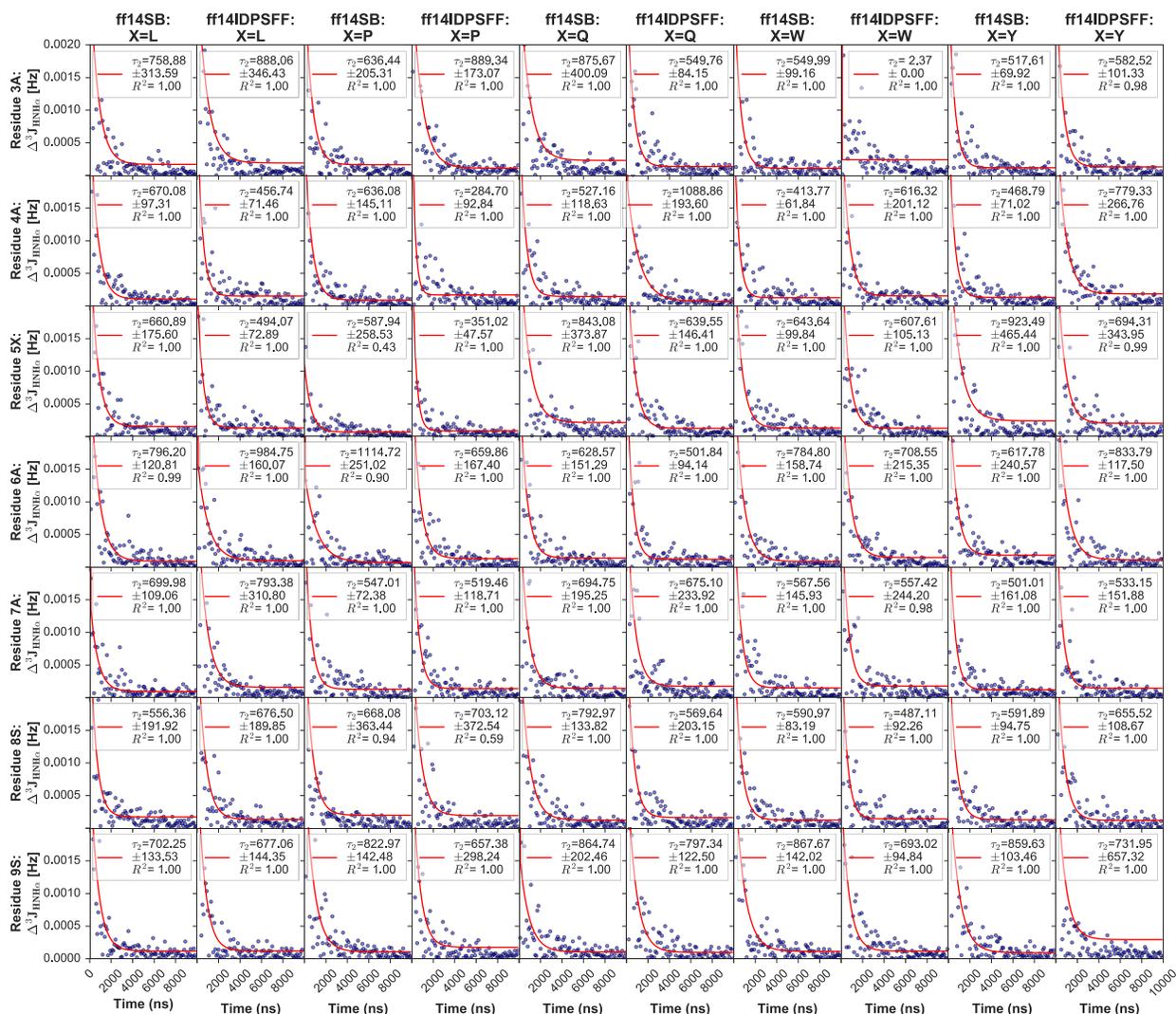


Figure S11. Biphasic exponential fittings were generated using $\Delta^3 J_{HNH\alpha}$ from cumulative average data in Figure S2 for EGAAXAASS (X= L, P, Q, W, Y) peptides and force field types. Each average cumulative $\Delta^3 J_{HNH\alpha}$ (blue dots) 100-ns increment was plotted per residue. Datasets were fitted to the following exponential decay function: $\Delta^3 J_{HNH\alpha} = A_1 e^{-\frac{x}{\tau_1}} + A_2 e^{-\frac{x}{\tau_2}} + c$ (red line). Each column represents a peptide and force field, and each row represents individual residues. Only residues 3A-9S are fitted.

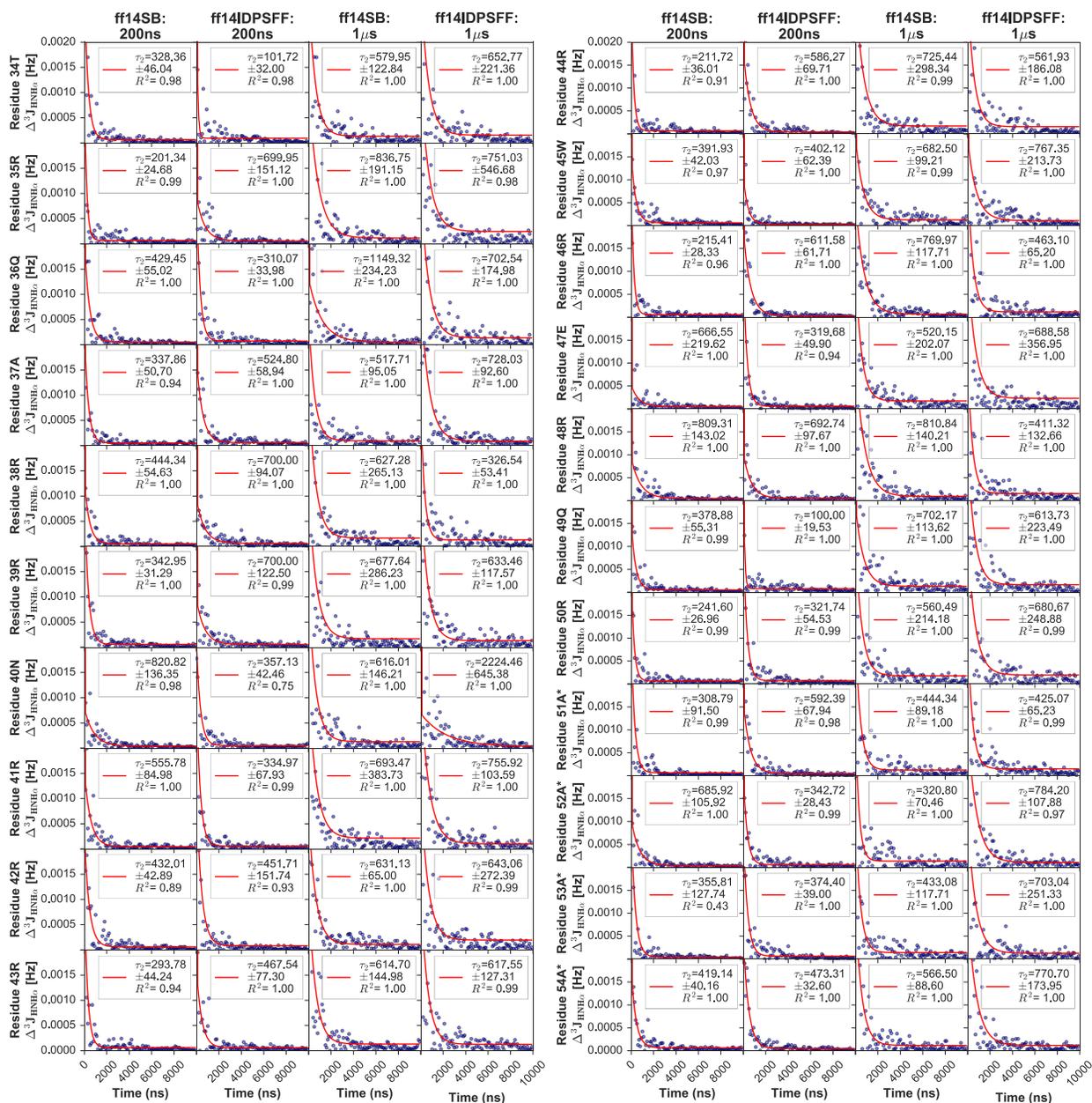


Figure S12. To evaluate cumulative average convergence of apo Rev simulations from Figure S4, a scatter plot of $\Delta^3 J_{\text{HNH}\alpha}$ values (blue dots) and corresponding biphasic exponential fit were generated for each simulation (long, short) and force field (*ff14SB*, *ff14IDPSFF*) types. Datasets were fitted to the following exponential decay function $\Delta^3 J_{\text{HNH}\alpha} = A_1 e^{-\frac{x}{\tau_1}} + A_2 e^{-\frac{x}{\tau_2}} + c$. The above subplots are titled according to simulation and force field type. Each column represents a peptide and force field, each row is labeled to its corresponding residue, and non-native residues marked with an asterisk (*).

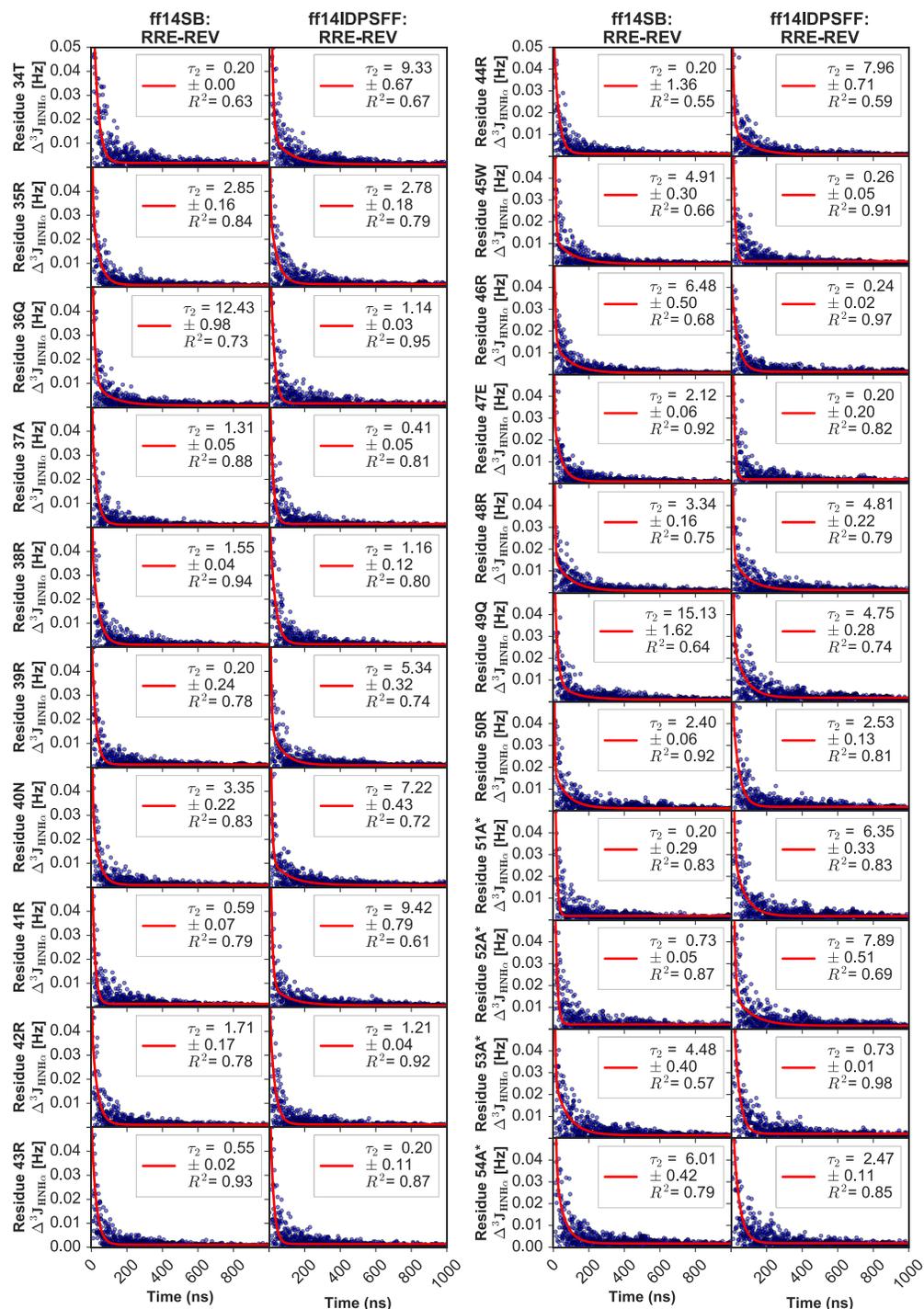


Figure S13. Biphasic exponential fittings were generated using $\Delta^3 J_{H\text{NH}\alpha}$ from cumulative average data in Figure S5 for RRE-Rev complexes and force field types. We applied the same fitting to the following exponential decay function: $\Delta^3 J_{H\text{NH}\alpha} = A_1 e^{-\frac{x}{\tau_1}} + A_2 e^{-\frac{x}{\tau_2}} + c$ (red line). Each average cumulative $\Delta^3 J_{H\text{NH}\alpha}$ (blue dots) 1-ns increment was plotted per residue. Each column represents a peptide and force field, each row is labeled to its corresponding residue, and non-native residues marked with an asterisk (*).

Clustering (apo Rev):

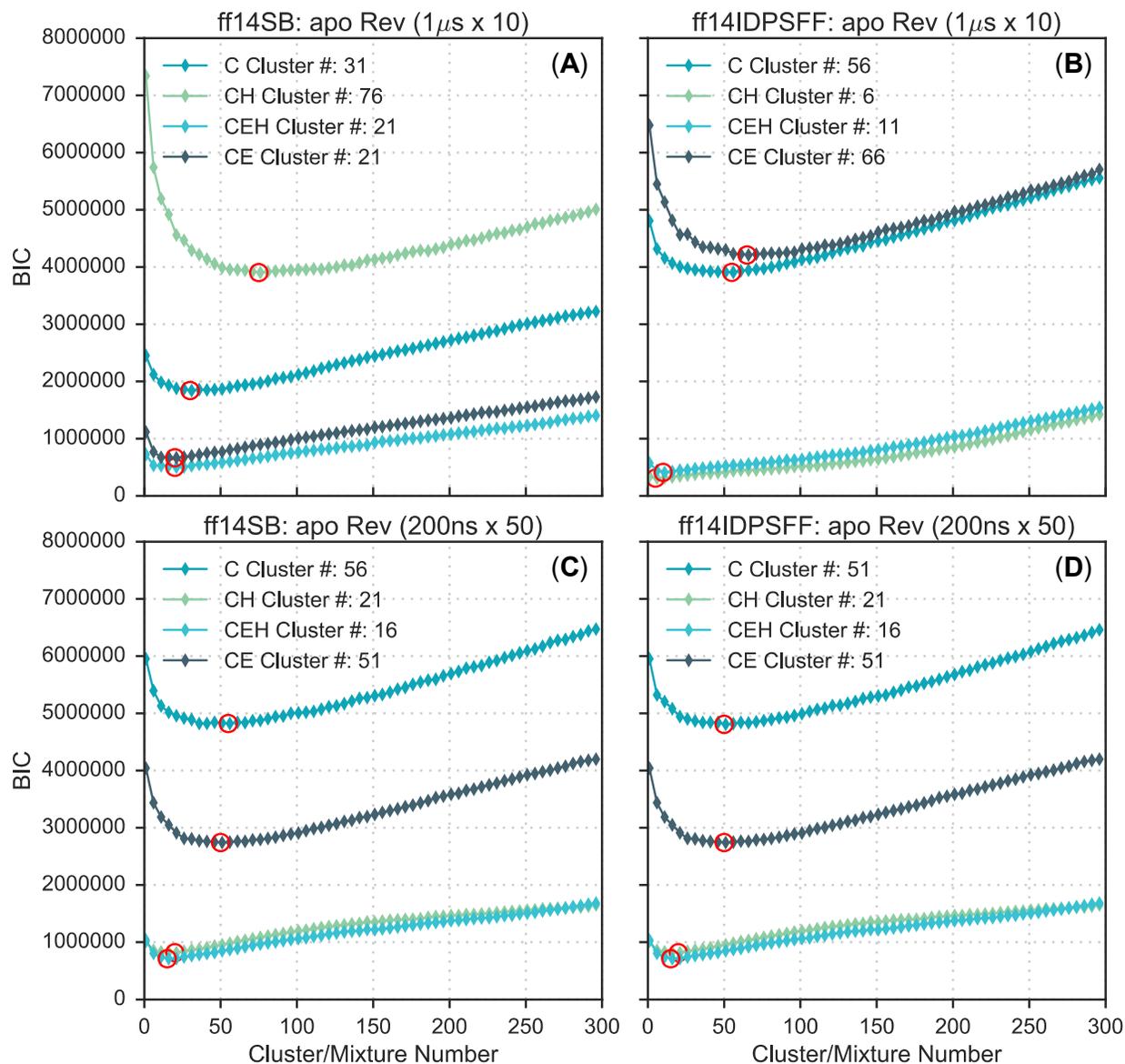


Figure S14. Determination of appropriate cluster/mixture number using the Bayesian information criterion (BIC) for apo Rev simulations. We calculated the BIC score between 1 to 300 mixtures, and the mixture/cluster number with the lowest BIC was selected for GMM generation. Chosen cluster numbers are indicated in the legend according to secondary structure categories from DSSP pre-clustering. (A) BIC plot of ten $1\mu\text{s}$ simulations using the *ff14SB* force field. (B) BIC of ten $1\mu\text{s}$ simulations using the *ff14IDPSFF* force field. (C) BIC plot of fifty 200ns simulations using the *ff14SB* force field. (D) BIC plot of fifty 200ns simulations using the *ff14IDPSFF* force field.



(C1) 2.49%



(C2) 2.48%



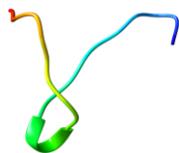
(C3) 2.22%



(C4) 2.19%



(C5) 1.87%



(C6) 1.86%



(C7) 1.81%



(C8) 1.51%



(C9) 1.48%



(C10) 1.46%

Figure S15. Top 10 clusters of *ff14SB*-parameterized simulations (200ns x 50) encompass 19.36% of all frames. Clusters are labeled C1-C10 and colored according to N- to C-termini sequence (red to blue).

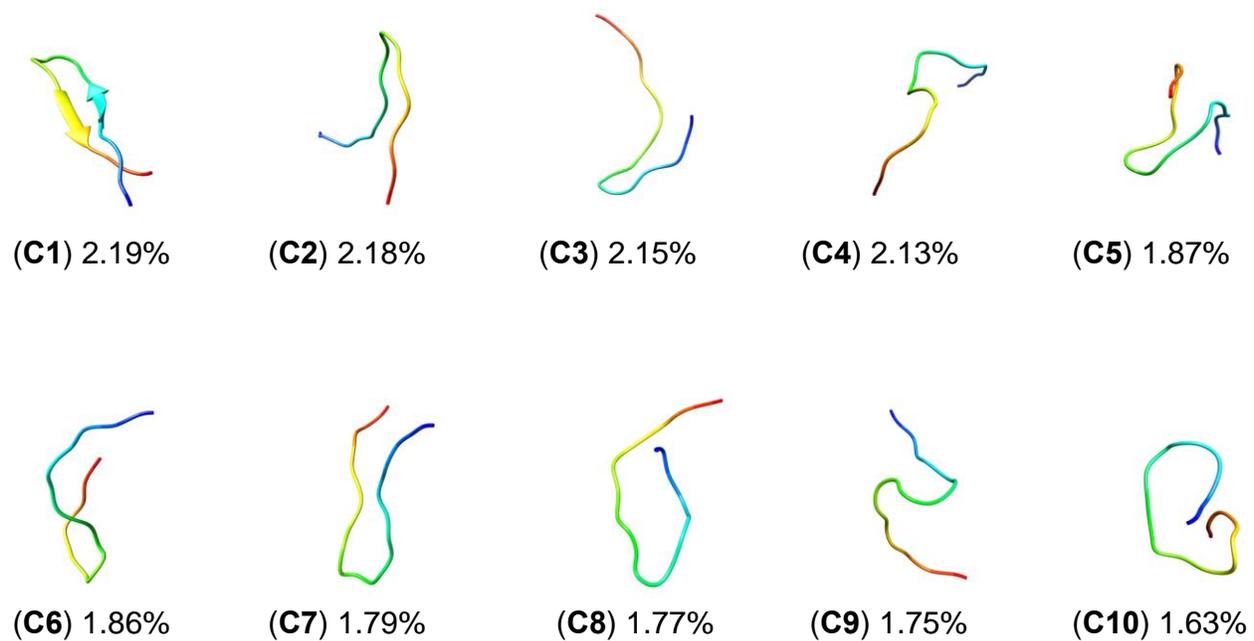


Figure S16. Top 10 clusters of *ff14IDPSFF*-parameterized simulations (200ns x 50) encompass 19.32% of all frames. Clusters are labeled C1-C10 and colored according to N- to C-termini sequence (red to blue).

DSSP:

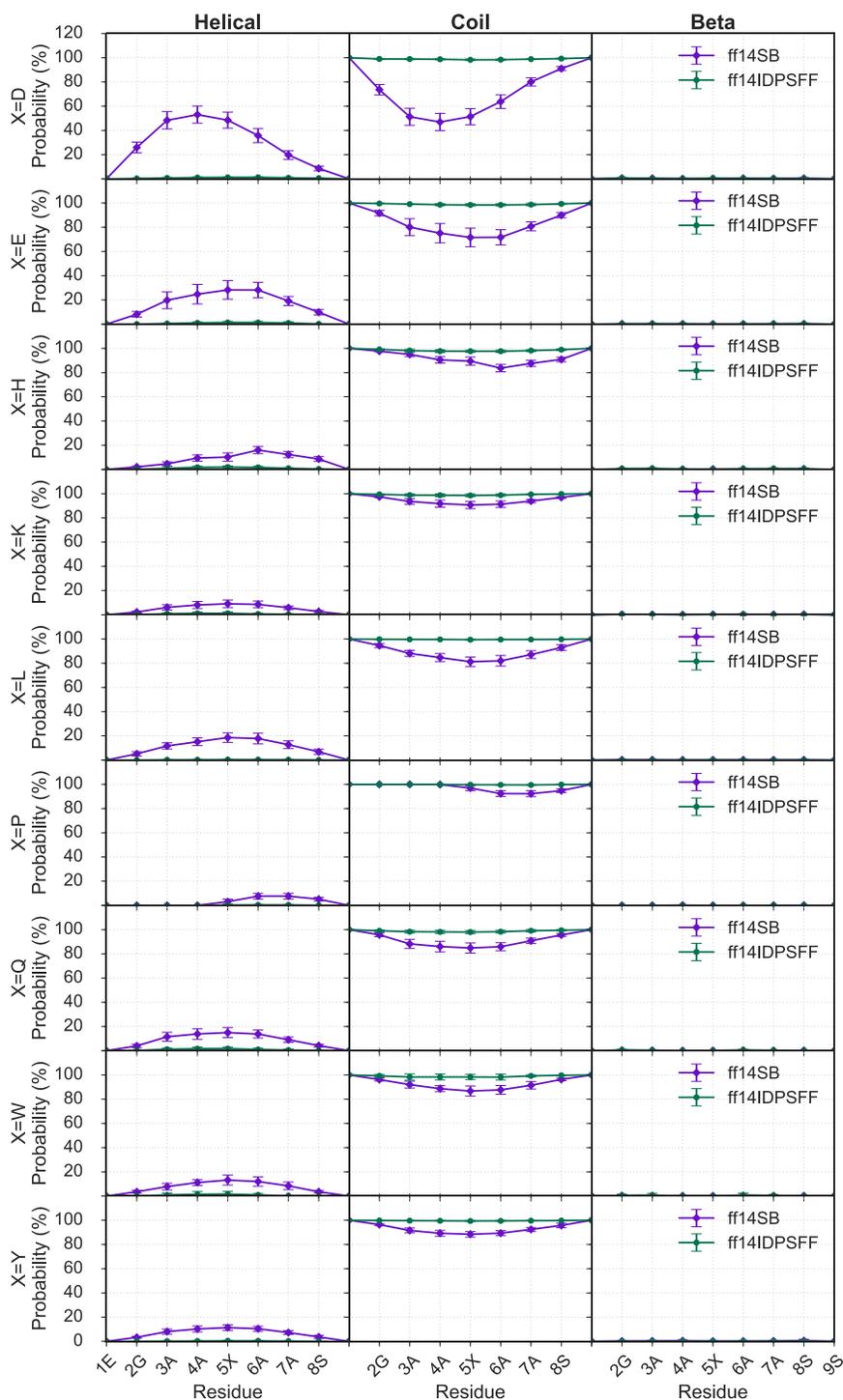


Figure S17. The average secondary structure propensity of each disordered short peptide. Colors correspond to force fields: purple – *ff14SB*, green – *ff14IDPSFF*. All values were calculated using the DSSP¹ program and MDtraj.² Rows indicate peptide (X = D, E, H, K, L, P, Q, W, Y) and columns indicate one of the three generalized secondary structures (helical, coiled, beta).

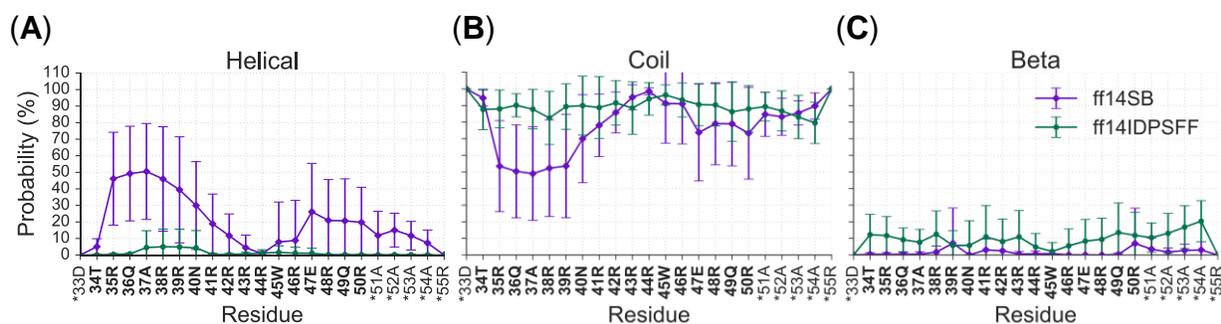


Figure S18. The average secondary structure propensity of each apo Rev residue was quantified from long simulation ($1\mu\text{s} \times 10$) datasets. Colors correspond to force fields: purple – *ff14SB*, green – *ff14IDPSFF*. All values were calculated using the DSSP¹ program and MDtraj.² (A) The probability of a residue exhibiting helical content. (B) Probability of coil content per residue. (C) Displays the beta-sheet helical propensity per residue. Non-native residues are indicated with an asterisk (*).

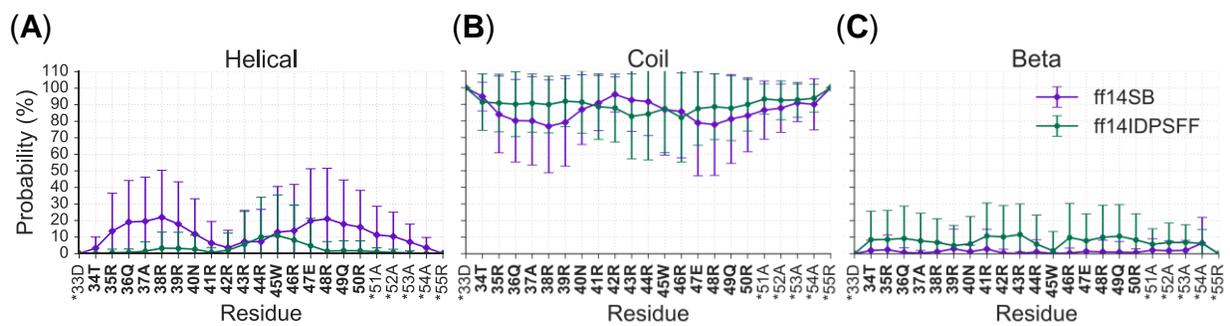


Figure S19. The average secondary structure propensity of each apo Rev residue was quantified from short simulation (200ns x 50) datasets. Colors correspond to force fields: purple – *ff14SB*, green – *ff14IDPSFF*. All values were calculated using the DSSP¹ program and MDtraj.² (A) The probability of a residue exhibiting helical content. (B) Probability of coil content per residue. (C) Displays the beta-sheet helical propensity per residue. Non-native residues are indicated with an asterisk (*).

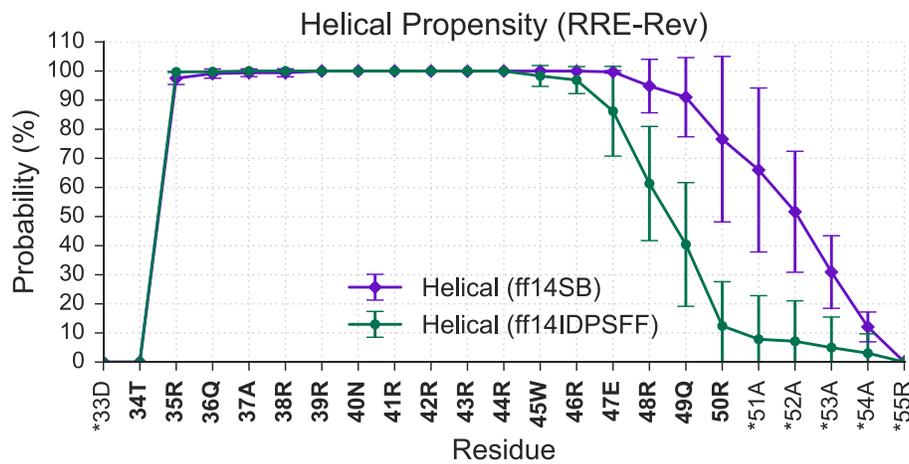


Figure S20. Average helical propensity of Rev from bound RRE-Rev simulations using the DSSP¹ program. Colors indicate force field: purple – *ff14SB*, green – *ff14IDPSFF*.

RMSF

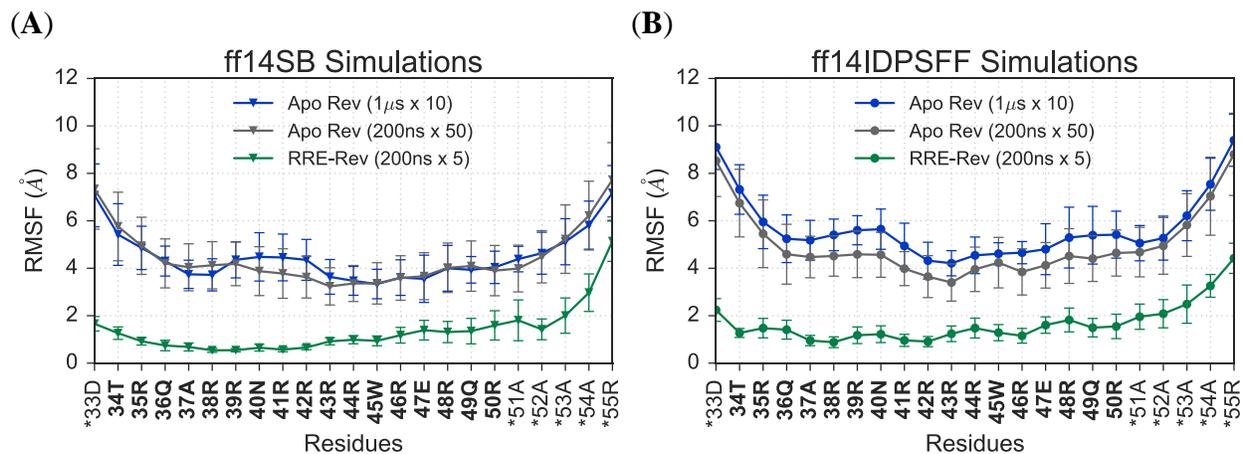


Figure S21. RMSF analyses of backbone C α atoms Rev-related simulations. (A) Average RMSF of backbone atoms in apo and bound Rev *ff14SB*-parameterized simulations. (B) Average RMSF of backbone atoms in apo and bound Rev *ff14IDPSFF*-parameterized simulations. Non-native residues contain an asterisk (*).

References:

1. Kabsch, W.; Sander, C., Dictionary of protein secondary structure: pattern recognition of hydrogen-bonded and geometrical features. *Biopolymers* **1983**, 22 (12), 2577-637.
2. McGibbon, R. T.; Beauchamp, K. A.; Harrigan, M. P.; Klein, C.; Swails, J. M.; Hernandez, C. X.; Schwantes, C. R.; Wang, L. P.; Lane, T. J.; Pande, V. S., MDTraj: A Modern Open Library for the Analysis of Molecular Dynamics Trajectories. *Biophys J* **2015**, 109 (8), 1528-32.